



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Volume: 11 Issue: V Month of publication: May 2023

DOI: https://doi.org/10.22214/ijraset.2023.52661

www.ijraset.com

Call: © 08813907089 E-mail ID: ijraset@gmail.com



ISSN: 2321-9653; IC Value: 45.98; SJ Impact Factor: 7.538

Volume 11 Issue V May 2023- Available at www.ijraset.com

A Review on Second Degree Homogeneous **Diophantine Equation with ThreeUnknowns** $x^2+y^2=122z^2$

K Hema¹, Ammineni Deepak Teja², Giri Kollati³

Abstract: The homogeneous ternary second degree equation given by $x^2+y^2=122z^2$ is analysed for its non-zero distinctintegral points on that. Completely various patterns of the equation into consideration are obtained by using python. Keywords: Ternary, quadratic, Integer solutions, Homogeneous, Diophantine, python.

INTRODUCTION I.

It is acknowledge that the quadratic Diophantine equations with 3 unknowns (homogeneous or non-homogeneous) are made in selection[1,2,]. Significantly, one might refer [3-17] for homogeneous or non-homogeneous ternary second degree Diophantine equations that are analysed for getting their corresponding non-zero distinct integer solutions. During this communication, one more attention-grabbing homogeneous ternary quadratic Diophantine equation given by $x^2 \Box y^2 \Box 122z^2$ is analysed for its nonzero distinct integer results through fully different strategies with simple python programs. One may gain different values for the input of their programs.

II. STYLES OF ANALYSIS	
The ternary second degree equation to be answered for its integer results is	
$x^2 \Box y^2 \Box 122z^2$	
	(1)
A. Pattern I	
Write 122 as	
122=(11+i)(11-i)	(2)
Assume	
$z \Box a^2 \Box b^2$	
	(3)
Thus we tend to get,	, ,
$x \Box 11a^2 \Box 11b^2 \Box 2aby \Box a^2 \Box b^2 \Box 22ab$	
$z \square a^2 \square b^2$	
We are going to see this by simple python code as follows:	
import math	
a=int(input("enter the value of a"))	
b=int(input("enter the value of b"))	
x=(11*a**2)-(11*b**2)-2*a*b;	
y=(a**2)-(b**2)+22*a*b;	
z=(a**2)+(b**2);	
print("the value of x is",x);	
print("the value of y is",y);	
print("the value of z is",z);	

¹Assistant Professor, Department of Mathematics, School of Engineering and Technology, Dhanalakshmi SrinivasanUniversity, Trichy, Tamil Nadu, India.

^{2, 3}B.Tech Student, Department of Computer Science Engineering, Dhanalakshmi Srinivasan University, Trichy – 621 112, TN, India.



International Journal for Research in Applied Science & Engineering Technology (IJRASET)

ISSN: 2321-9653; IC Value: 45.98; SJ Impact Factor: 7.538 Volume 11 Issue V May 2023- Available at www.ijraset.com

ATT 1000.	
ouput:	
enter the value of a 5	
5	
enter the value of b 5	
5	
the value of x is -50	
the value of y is 550	
the value of z is 50	
B. Pattern 2	
Equation (1) can also be written as	
$x^2 \square y^2 \square 121z^2 \square z^2$	
$\Box x^2 \Box 121z^2 \Box z^2 \Box y^2$	(4)
	(.)
Applying the tactic of cross-multiplication to the on-top system of equations, note that	
Applying the factic of cross-multiplication to the on-top system of equations, note that $x \Box 11\Box^2 \Box 11\Box^2 \Box 2\Box\Box$	
$y \square \square \square^2 \square \square^2 \square 22\square\square z \square \square^2 \square \square^2$	
Applying python codes and considering alpha and beta as a and b we get,	
import math	
a=int(input("enter the value of a"))	
b=int(input("enter the value of b"))	
x=(11*a**2)-(11*b**2)+2*a*b;	
y=(-a**2)+(b**2)+22*a*b;	
z=(a**2)+(b**2);	
print("the value of x is",x);	
print("the value of y is",y);	
print("the value of z is",z);	
Output:	
enter the value of a 5	
5	
enter the value of b 5	
5	
the value of x is 50	
the value of y is 550	
the value of z is 50	
the value of L is 50	
C. Pattern III	
One can also be written as	
$x^2 \square y^2 \square 122z^2 \square 1$	
Write 1 as	
$1 \square $ $\square 3 \square 4i \square \square 3 \square 4i \square 25$	(5)
(6)	
(6) As our interest is on finding integer solutions replacing a by 5A & b by 5B, we get	
As our interest is on finding integer solutions replacing a by 5A & b by 5B, we get	
$x \square 29A^2 \square 29B^2 \square 94AB$	
$y \square 47A^2 \square 47B^2 \square 58AB$	
$z \square 5A^2 \square 5B^2 \tag{7}$	



International Journal for Research in Applied Science & Engineering Technology (IJRASET)

ISSN: 2321-9653; IC Value: 45.98; SJ Impact Factor: 7.538 Volume 11 Issue V May 2023- Available at www.ijraset.com

```
Considering A,B as a,b we are following results:
  import math
  a=int(input("enter the value of a"))
  b=int(input("enter the value of b"))
  x=(29*a**2)-(29*b**2)-94*a*b;
  y=(47*a**2)-(47*b**2)+58*a*b;
  z=(5*a**2)+(5*b**2);
  print("the value of x is",x);
  print("the value of y is",y);
  print("the value of z is",z);
  Output:
  enter the value of a 5
  5
  enter the value of b 5
  the value of x is -2350
  the value of y is 1450
  the value of z is 250
D. Pattern IV
  Introduction of the direct metamorphoses
  x=u+v,y=u-v,z=2w
                                                                                                                  (8)
  in (1) leads to
  u^2 \square v^2 \square 244w^2
  Assume
  w \square c^2 \square d^2
Thereby we are getting these following results
   (10)
 (11)
we are getting these following results:
 x \square 22c^2 \square 22d^2 \square 4cd
 y \square \square 2c^2 \square 2d^2 \square 44cd
 z \square 2c^2 \square 2d^2
 import math
  c=int(input("enter the value of c"))
  d=int(input("enter the value of d"))
  x=(22*c**2)-(22*d**2)-4*c*d;
  y=(-2*c**2)+(2*d**2)-44*c*d;
  z=(2*c**2)+(2*d**2);
  print("the value of x is",x);
  print("the value of y is",y);
  print("the value of z is",z);
```



International Journal for Research in Applied Science & Engineering Technology (IJRASET)

ISSN: 2321-9653; IC Value: 45.98; SJ Impact Factor: 7.538 Volume 11 Issue V May 2023- Available at www.ijraset.com

Output:

enter the value of c 5 5 enter the value of d 5 5 the value of x is -100 the value of z is 100

III. CONCLUSION

In this paper, an bid has been created to get non-zero distinct integer results to the ternary quadratic Diophantine equation $x^2 \Box y^2$ $\Box 122 z^2$ representing homogeneous cone with python canons. As there are kinds of cones, the compendiums might rummage around for indispensable kinds of cones to get integer results for the corresponding cones with python codes.

REFERENCES

- [1] L.E. Dickson, History of theory of Numbers, Vol. 2, Chelsea publishing Company, Newyork, 1952.
- [2] Mordel, Diophantine Equations, Academic press, Newyork, 1969.
- [3] Gopalan M.A., Geetha D,Lattice points on the hyperbola of two sheets $x^2 \square 6xy \square y^2 \square 6x \square 2y \square 5 \square z^2 \square 4$, Impact J Sci Tech:4:23-32,2010.
- [4] Gopalan M.A., Vidhyalakshmi S,Kavitha A, Integral points on the homogeneous coneDiophantine J Math; 1(2):127-136, 2012. $z^2 \square 2x^2 \square 7y^2$, The
- [5] Gopalan M.A., Vidhyalakshmi S, Sumathi G,Lattice points on the hyperboloid of one sheet $4z^2 \Box 2x^2 \Box 3y^2 \Box 4$, Diophantine J Math; 1(2): 109-115, 2012.
- [6] Gopalan M.A., Vidhyalakshmi S, Lakshmi K, Integral points on the hyprerboloid of two sheets $3y^2 \Box 7x^2 \Box z^2 \Box 21$, Diophantine J Math; 1(2):99-107, 2012.
- [7] Gopalan M.A., Vidhyalakshmi S, Mallika S, Observations on hyperboloid of one sheetJMath; 2(3):221-226,2012. $x^2 \Box 2y^2 \Box z^2 \Box 2$, Bessel
- [8] Gopalan M.A., Vidhyalakshmi S, Usha Rani T.R., Mallika S, Integral points on the homogeneous cone $6z^2 \square 3y^2 \square 2x^2 \square 0$, Impact J Sci Tech; 6(1):7-13, 2012.
- [9] Gopalan M.A., Vidhyalakshmi S, Sumathi G, Lattice points on the elliptic paraboloidApplied Mathematics;7(4): 379-385, 2012. z $\Box 9x^2 \Box 4y^2$, Advances in
- [10] Gopalan M.A., Vidhyalakshmi S, Usha Rani T.R.,Integral points on the non-homogeneous cone $2z^2 \square 4xy \square 8x \square 4z \square 0$, Global Journal of Mathematics and Mathematics sciences 2012;2(1):61-67.
- [11] Gopalan M.A., Vidhyalakshmi S, Lakshmi K, Lattice points on the elliptic paraboloid 16 y 2 \Box 9z 2 \Box 4x, Bessel JMath;
- [12] Python Object-Oriented Programming by Steven F.Lott and Dusty Phillips ,4th edition.
- [13] Effective Python by Brett Slatkin , 1st edition









45.98



IMPACT FACTOR: 7.129



IMPACT FACTOR: 7.429



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Call: 08813907089 🕓 (24*7 Support on Whatsapp)