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A Review on Second Degree Homogeneous Diophantine Equation with ThreeUnknowns $x^2+y^2=122z^2$

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Abstract: The homogeneous ternary second degree equation given by $x^2+y^2=122z^2$ is analysed for its non-zero distinctintegral points on that. Completely various patterns of the equation into consideration are obtained by using python. Keywords: Ternary, quadratic, Integer solutions, Homogeneous, Diophantine, python.

I. INTRODUCTION

It is acknowledge that the quadratic Diophantine equations with 3 unknowns (homogeneous or non-homogeneous) are made in selection[1,2,]. Significantly, one might refer [3-17] for homogeneous or non-homogeneous ternary second degree Diophantine equations that are analysed for getting their corresponding non-zero distinct integer solutions. During this communication, one more attention-grabbing homogeneous ternary quadratic Diophantine equation given by $x^2 \square y^2 \square 122 z^2$ is analysed for its non-zero distinct integer results through fully different strategies with simple python programs. One may gain different values for the input of their programs.

II. STYLES OF ANALYSIS

The ternary second degree equation to be answered for its integer results is $x^2 \Box y^2 \Box 122z^2$

	(1)
A. Pattern I	
Write 122 as	
122=(11+i)(11-i)	(2)
Assume	
$z \ \square \ a^2 \ \square \ b^2$	
	(3)

Thus we tend to get, $x \Box 11a^2 \Box 11b^2 \Box 2aby \Box a^2 \Box b^2 \Box 22ab$ $z \Box a^2 \Box b^2$ We are going to see this by simple python code as follows: import math a=int(input("enter the value of a")) b=int(input("enter the value of b")) x=(11*a**2)-(11*b**2)-2*a*b; y=(a**2)+(b**2)+22*a*b; z=(a**2)+(b**2);print("the value of x is",x); print("the value of y is",y); print("the value of z is",z);



ouput : enter the value of a 5 5 enter the value of b 5 5 the value of x is -50 the value of y is 550 the value of z is 50

B. Pattern 2

Equation (1) can also be written as $x^2 \Box y^2 \Box 121z^2 \Box z^2$ $\Box x^2 \Box 121z^2 \Box z^2 \Box y^2$

(4)

Applying the tactic of cross-multiplication to the on-top system of equations, note that $x \Box 11 \Box^2 \Box 11 \Box^2 \Box 2 \Box \Box$ $y \Box \Box^2 \Box \Box^2 \Box 2 \Box \Box z \Box \Box^2 \Box \Box^2$ Applying python codes and considering alpha and beta as a and b we get,

import math

a=int(input("enter the value of a")) b=int(input("enter the value of b")) x=(11*a**2)-(11*b**2)+2*a*b;y=(-a**2)+(b**2)+22*a*b;z=(a**2)+(b**2);print("the value of x is",x); print("the value of y is",y); print("the value of z is",z);

Output :

```
enter the value of a 5
5
enter the value of b 5
5
the value of x is 50
the value of y is 550
the value of z is 50
```

C. Pattern III

One can also be written as $x^2 \Box y^2 \Box 122 z^2 \Box 1$ Write 1 as $1 \Box \Box \Box \Box A i \Box \Box \Box A i \Box 25$

(5)

As our interest is on finding integer solutions replacing a by 5A & b by 5B , we get

 $x \square 29A^2 \square 29B^2 \square 94AB$ $y \square 47A^2 \square 47B^2 \square 58AB$ $z \square 5A^2 \square 5B^2$

(7)

(6)



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Considering A,B as a,b we are following results: import math a=int(input("enter the value of a"))b=int(input("enter the value of b"))x=(29*a**2)-(29*b**2)-94*a*b;y=(47*a**2)-(47*b**2)+58*a*b;z=(5*a**2)+(5*b**2);print("the value of x is",x);

print("the value of y is",y);
print("the value of z is",z);

Output:

enter the value of a 5 5 enter the value of b 5 5 the value of x is -2350 the value of y is 1450 the value of z is 250

D. Pattern IV

Introduction of the direct metamorphoses x=u+v, y=u-v, z=2win (1) leads to

 $u^{2} \Box v^{2} \Box 244w^{2}$ Assume $w \Box c^{2} \Box d^{2}$ Thereby we are getting these following results (10)

(11)

we are getting these following results : $x \Box 22c^2 \Box 22d^2 \Box 4cd$ $y \Box \Box 2c^2 \Box 2d^2 \Box 44cd$ $z \Box 2c^2 \Box 2d^2$

import math c=int(input("enter the value of c"))) d=int(input("enter the value of d"))) x=(22*c**2)-(22*d**2)-4*c*d; y=(-2*c**2)+(2*d**2)-44*c*d; z=(2*c**2)+(2*d**2);print("the value of x is",x); print("the value of y is",y); print("the value of z is",z); (8)



Output :

enter the value of c 5 5 enter the value of d 5 5 the value of x is -100 the value of y is -1100 the value of z is 100

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III. CONCLUSION

In this paper, an bid has been created to get non-zero distinct integer results to the ternary quadratic Diophantineequation $x^2 \Box y^2$ $\Box 122 z^2$ representing homogeneous cone with python canons. As there are kinds of cones, the compendiums might rummage around for indispensable kinds of cones to get integer results for the corresponding cones with python codes.

REFERENCES

- [1] L.E. Dickson, History of theory of Numbers, Vol. 2, Chelsea publishing Company, Newyork, 1952.
- [2] Mordel, Diophantine Equations, Academic press, Newyork, 1969.
- [3] Gopalan M.A., Geetha D,Lattice points on the hyperbola of two sheets $x^2 \square 6xy \square y^2 \square 6x \square 2y \square 5 \square z^2 \square 4$, Impact J Sci Tech:4:23-32,2010.
- [4] Gopalan M.A., Vidhyalakshmi S,Kavitha A, Integral points on the homogeneous coneDiophantine J Math; 1(2):127-136, 2012. $z^2 \square 2x^2 \square 7y^2$, The
- [5] Gopalan M.A., Vidhyalakshmi S, Sumathi G, Lattice points on the hyperboloid of one sheet $4z^2 \Box 2x^2 \Box 3y^2 \Box 4$, Diophantine J Math; 1(2): 109-115, 2012.
- [6] Gopalan M.A., Vidhyalakshmi S, Lakshmi K, Integral points on the hyperboloid of two sheets
- $3y^2 \square 7x^2 \square z^2 \square 21$, Diophantine J Math; 1(2):99-107, 2012.
- [7] Gopalan M.A., Vidhyalakshmi S, Mallika S, Observations on hyperboloid of one sheetJMath; 2(3):221-226,2012. $x^2 \square 2y^2 \square z^2 \square 2$, Bessel
- [8] Gopalan M.A., Vidhyalakshmi S, Usha Rani T.R., Mallika S, Integral points on the homogeneous cone 6z² 3y² 2x² 0, Impact J Sci Tech; 6(1):7-13, 2012.
- [9] Gopalan M.A., Vidhyalakshmi S, Sumathi G, Lattice points on the elliptic paraboloidApplied Mathematics;7(4): 379-385, 2012. z \Box 9x² \Box 4y², Advances in
- [10] Gopalan M.A., Vidhyalakshmi S, Usha Rani T.R., Integral points on the non-homogeneous cone $2z^2 \square 4xy \square 8x \square 4z \square 0$, Global Journal of Mathematics and Mathematics sciences 2012;2(1):61-67.
- [11] Gopalan M.A., Vidhyalakshmi S, Lakshmi K, Lattice points on the elliptic paraboloid 16 y² \square 9z² \square 4x, Bessel JMath;
- [12] Python Object-Oriented Programming by Steven F.Lott and Dusty Phillips ,4th edition.
- [13] Effective Python by Brett Slatkin , 1st edition











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