# Cryptographic Algorithm Based on Prime Assignment 

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#### Abstract

Cryptography is a concept of protecting information and conversations which are transmitted through a public source, so that the send and receiver only read and process it. There are several encryption and decryption algorithm which involves mathematical concepts to provide more security to the text which has to be shared through a medium. In this paper, an algorithm is provided for both coding and decoding using cyclic symmetric matrices. Also Euler totient function, prime numbers are employed here. Furthermore, algorithm using prime number in integers is extended to prime numbers in Gaussian integers. This concept increases the security of the text.


Keywords: Cryptography; encryption- decryption algorithms; Gaussian primes; cyclic symmetric matrix. 2010 MSC Subject Classifications - 11T71, 11C20, 11A25, 11R04.

## I. INTRODUCTION

For centuries, people have sent secret messages by various means. But some messages were not maintained secretly as there was no proper security. In order to maintain secrecy, cryptography was developed. It is the process of converting ordinary plain text (message to be sent) into some unintelligible text and vice versa. It helps to transmit data in a particular form so that the intended persons can read and process it. It is also useful for user authentication.
In olden days, an algorithm in cryptography was based on concepts which are well- known by all. But now- a- days, it is mainly based on mathematical theory and computer applications. Especially, number theory is playing a vital role in it, which employs the concepts such as congruence, Euler's theorem.
In modern days, one can make use of any mathematical concepts to make their algorithm. As much as mathematics imposed, as much as security increases. Motivated by [3], this work aims to propose an algorithm to improve the security based on things such as prime numbers, Euler phi function, cyclic symmetric matrices. By modifying the assignments of alphabets in [3], this work is developed.
This paper involves two algorithms. First one uses integer prime assignment whereas second one uses Gaussian prime assignment. For the second case, Euler phi function on Gaussian integers $\varphi_{\mathbb{Z}[i]}$ is employed.

Common notations and definitions:

1) $W_{i}=i^{t h}$ word in the message to be sent
2) $\eta\left(W_{i}\right)=$ no. of letters in $W_{i}$
3) $E\left(\eta\left(W_{i}\right)\right)=\left\{\begin{array}{l}k_{i}=\frac{\eta\left(W_{i}\right)+1}{2}, \text { if } \eta\left(W_{i}\right) \text { is odd } \\ k_{i}=\frac{\eta\left(W_{i}\right)}{2}, \text { if } \eta\left(W_{i}\right) \text { is even }\end{array}\right.$
4) $I_{i}=$ Identity matrix of order $i$
5) $A_{i}=k_{i}^{\text {th }}$ row of cyclic matrix $M_{i}$
6) $D\left(A_{i}\right)=$ diagonal matrix with values in $A_{i}$

## II. ALGORITHM BASED ON INTEGER PRIMES

## A. Euler phi Function on $\mathbb{N}$

1. Euler phi function $\varphi(n)$ is defined on natural numbers which counts the numbers which are less than $n$ and prime to it. ie., $\varphi(n)=\mid\{k \in \mathbb{N}: k<n$ and $(k, n)=1\} \mid$
2. For a prime $p, \varphi(p)=p-1$

## B. Algorithm for Encryption

Assign the first 26 prime numbers to the alphabets. i.e.,

| 2 | 3 | 5 | 7 | 11 | 13 | 17 | 19 | 23 | 29 | 31 | 37 | 41 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | B | C | D | E | F | G | H | I | J | K | L | M |
| N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| 43 | 47 | 53 | 59 | 61 | 67 | 71 | 73 | 79 | 83 | 89 | 97 | 101 |

The algorithm is defined as follows:

1) Let the message to be encrypted be $W_{1}, W_{2}, \ldots, W_{n}$ (separated as words and omitting spaces).
2) For all $1 \leq i \leq n$, assign each letters in $W_{i}$ with the above defined table.
3) Apply $\varphi$ for each assigned values in $W_{i}$.
4) Construct a cyclic symmetric matrix for each $W_{i}$ separately.
5) Calculate $E\left(\eta\left(W_{i}\right)\right)$, for all $1 \leq i \leq n$
6) Find the $k_{i}^{\text {th }}$ row from the matrix and construct $A_{i}, 1 \leq i \leq n$
7) Evaluate $D\left(A_{i}\right)-\eta\left(W_{i}\right) I_{\eta\left(W_{i}\right)}, 1 \leq i \leq n$, which is the encrypted key. (For each word it is separated by commas)
C. Algorithm for Decryption
8) Let $B_{i}=D\left(A_{i}\right)-\eta\left(W_{i}\right) I_{\eta\left(W_{i}\right)}, 1 \leq i \leq n$
9) Calculate $C_{i}=D\left(B_{i}\right)+\eta\left(B_{i}\right) I_{\eta\left(B_{i}\right)}, 1 \leq i \leq n$
10) Find $E\left(\eta\left(B_{i}\right)\right)=k_{i}, 1 \leq i \leq n$

This gives that first digit of $C_{i}$ is the $k_{i}^{\text {th }}$ letter of the $i^{\text {th }}$ word.
Now, the second digit of $C_{i}$ is the $\left(k_{i}+1\right)^{\text {th }}$ letter of $i^{\text {th }}$ word and so on (This works on cyclic order).
4) Rewrite $C_{i}$ as in the above order.
5) For every digit in $C_{i}$, add 1 .
6) Convert the digits into alphabets.
a) Example 1: Let us work on the word "HELLO"

- Encryption
> Let $W_{1}$ be the word HELLO
$>$ Assign the positions of the letters.

| H | E | L | L | O |
| :---: | :---: | :---: | :---: | :---: |
| 19 | 11 | 37 | 37 | 47 |

$>$ Apply $\varphi$

| H | E | L | L | O |
| :---: | :---: | :---: | :---: | :---: |
| 18 | 10 | 36 | 36 | 46 |

> The cyclic symmetric matrix is

$$
M=\left(\begin{array}{lllll}
18 & 10 & 36 & 36 & 46 \\
10 & 36 & 36 & 46 & 18 \\
36 & 36 & 46 & 18 & 10 \\
36 & 46 & 18 & 10 & 36 \\
46 & 18 & 10 & 36 & 36
\end{array}\right)
$$

$>$ Here $\eta\left(W_{1}\right)=5$, which is odd.
Thus, $E\left(\eta\left(W_{1}\right)\right)=k_{1}=\frac{5+1}{2}=3$
$>$ The $3^{\text {rd }}$ row of $M$ forms $A_{1}$.
i.e., $A_{1}=\left(\begin{array}{ll}36 & 36461810)\end{array}\right.$
$>D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}=\left(\begin{array}{ccccc}36 & 0 & 0 & 0 & 0 \\ 0 & 36 & 0 & 0 & 0 \\ 0 & 0 & 46 & 0 & 0 \\ 0 & 0 & 0 & 18 & 0 \\ 0 & 0 & 0 & 0 & 10\end{array}\right)-\left(\begin{array}{lllll}5 & 0 & 0 & 0 & 0 \\ 0 & 5 & 0 & 0 & 0 \\ 0 & 0 & 5 & 0 & 0 \\ 0 & 0 & 0 & 5 & 0 \\ 0 & 0 & 0 & 0 & 5\end{array}\right)$

$$
=\left(\begin{array}{ccccc}
31 & 0 & 0 & 0 & 0 \\
0 & 31 & 0 & 0 & 0 \\
0 & 0 & 41 & 0 & 0 \\
0 & 0 & 0 & 13 & 0 \\
0 & 0 & 0 & 0 & 5
\end{array}\right)
$$

The encrypted key is 313141135 .

- Decryption
$>B_{1}=D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}$

$$
=(313141135)
$$

$>C_{1}=D\left(B_{1}\right)+\eta\left(B_{1}\right) I_{\eta\left(B_{1}\right)}$

$$
=\left(\begin{array}{ll}
36 & 364618
\end{array}\right)
$$

$>E\left(\eta\left(B_{1}\right)\right)=\frac{5+1}{2}=3$
So first digit of $C_{1}$ is the $3^{r d}$ letter in $W_{1}$.
The order is

| 36 | 36 | 46 | 18 | 10 |
| :--- | :--- | :--- | :--- | :--- |
| $3^{\text {rd }}$ | $4^{\text {th }}$ | $5^{\text {th }}$ | $1^{\text {st }}$ | $2^{\text {nd }}$ |

$\rightarrow$ Thus the rewritten form is ( 1810363646 )
$>$ Adding 1, one can get (1911373747), which corresponds to the word "HELLO".
b) Example 2: Let us consider "WORK HARD"

- Encryption
$>\quad$ Let $W_{1}$ be the word $W O R K$ and $W_{2}$ be HARD
$>$ Assign the positions of the letters.

| W | O | R | K |
| ---: | :---: | :---: | :---: |
| 83 | 47 | 61 | 31 |


| H | A | R | D |
| :---: | :---: | :---: | :---: |
| 19 | 2 | 61 | 7 |

$>\operatorname{Apply} \varphi$

| W | O | R | K |
| :---: | :---: | :---: | :---: |
| 82 | 46 | 60 | 30 |


| H | A | R | D |
| :---: | :---: | :---: | :---: |
| 18 | 1 | 60 | 6 |

> The cyclic symmetric matrix is

$$
M_{1}=\left(\begin{array}{llll}
82 & 46 & 60 & 30 \\
46 & 60 & 30 & 82 \\
60 & 30 & 82 & 46 \\
30 & 82 & 46 & 60
\end{array}\right) \text { and } M_{2}=\left(\begin{array}{cccc}
18 & 1 & 60 & 6 \\
1 & 60 & 6 & 18 \\
60 & 6 & 18 & 1 \\
6 & 18 & 1 & 60
\end{array}\right)
$$

$>$ Here $\eta\left(W_{1}\right)=\eta\left(W_{2}\right)=4$, which is even.
Thus, $E\left(\eta\left(W_{1}\right)\right)=E\left(\eta\left(W_{2}\right)\right)=k_{1}=k_{2}=\frac{4}{2}=2$
$>$ The $2^{\text {nd }}$ row of $M_{1}$ forms $A_{1}$ and $2^{\text {nd }}$ row of $M_{2}$ forms $A_{2}$.
i.e., $A_{1}=(46603082)$ and $A_{2}=(160618)$
$\Rightarrow D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}=\left(\begin{array}{cccc}46 & 0 & 0 & 0 \\ 0 & 60 & 0 & 0 \\ 0 & 0 & 30 & 0 \\ 0 & 0 & 0 & 82\end{array}\right)-\left(\begin{array}{llll}4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 4\end{array}\right)$

$$
=\left(\begin{array}{cccc}
42 & 0 & 0 & 0 \\
0 & 56 & 0 & 0 \\
0 & 0 & 26 & 0 \\
0 & 0 & 0 & 78
\end{array}\right)
$$

$$
D\left(A_{2}\right)-\eta\left(W_{2}\right) I_{\eta\left(W_{2}\right)}=\left(\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 60 & 0 & 0 \\
0 & 0 & 6 & 0 \\
0 & 0 & 0 & 18
\end{array}\right)-\left(\begin{array}{llll}
4 & 0 & 0 & 0 \\
0 & 4 & 0 & 0 \\
0 & 0 & 4 & 0 \\
0 & 0 & 0 & 4
\end{array}\right)
$$

$$
=\left(\begin{array}{cccc}
-3 & 0 & 0 & 0 \\
0 & 56 & 0 & 0 \\
0 & 0 & 2 & 0 \\
0 & 0 & 0 & 14
\end{array}\right)
$$

The encrypted key is $42562678,-356214$.

- Decryption
$>B_{1}=D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}$

$$
\begin{gathered}
=(42562678) \\
B_{2}=D\left(A_{2}\right)-\eta\left(W_{2}\right) I_{\eta\left(W_{2}\right)}=(-356214)
\end{gathered}
$$

$>C_{1}=D\left(B_{1}\right)+\eta\left(B_{1}\right) I_{\eta\left(B_{1}\right)}$

$$
\begin{aligned}
= & (46603082) \\
C_{2}= & D\left(B_{2}\right)+\eta\left(B_{2}\right) I_{\eta\left(B_{2}\right)} \\
& =(160618)
\end{aligned}
$$

> $E\left(\eta\left(B_{1}\right)\right)=E\left(\eta\left(B_{2}\right)\right)=\frac{4}{2}=2$
So first digit of $C_{1}$ is the $2^{\text {nd }}$ letter in $W_{1}$ and first digit of $C_{2}$ is $2^{\text {nd }}$ letter in $W_{2}$.
The order is

| 46 | 60 | 30 | 82 |
| :--- | :--- | :--- | :--- |
| $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ | $1^{\text {st }}$ |


| 1 | 60 | 6 | 18 |
| :---: | :--- | :--- | :--- |
| $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ | $1^{\text {st }}$ |

> Thus the rewritten form is (82 466030 ) and (18 1606 )
$>$ Adding 1 , one can get ( 83476131 ) and (192617), which corresponds to the words "WORK" and "HARD"

## III. ALGORITHM BASED ON GAUSSIAN PRIMES

## A. Gaussian Integers

Gaussian integers are complex numbers $z=a+i b$ where $a, b$ are integers and it is denoted by $\mathbb{Z}[i]$. The norm of $z=a+i b$ is given by $N(a+i b)=a^{2}+b^{2}$.

## B. Gaussian Primes

$z=a+i b i$ a Gaussian prime if one of the following holds:

- If $a \neq 0, b \neq 0$, then $a+i b$ is a Gaussian prime if and only if $N(a+i b)=a^{2}+b^{2}$ is an integer prime.
- If $a \neq 0$, then $b i$ is a Gaussian prime if $|b|$ is an integer prime and $|b| \equiv 3(\bmod 4)$.
- If $b \neq 0$, then $a$ is a Gaussian prime if $|a|$ is an integer prime and $|a| \equiv 3(\bmod 4)$.

Note
If $p$ is an integer prime such that $p \equiv 1(\bmod 4)$, then $p=x^{2}+y^{2}$. Thus $x+i y, x<y$ is a Gaussian prime corresponding to $p$.
Euler phi function on $\mathbb{Z}[i]$

- In [1], $\varphi_{\mathbb{Z}[i]}(a+i b)$ is defined as the number of Gaussian integers which are invertible modulo $a+i b$.
- If $p+q i$ is a Gaussian prime, then $\varphi_{\mathbb{Z}[i]}(p+q i)=N(p+q i)-1=p^{2}+q^{2}-1$

Algorithm for encryption.
Assign the Gaussian prime numbers to the alphabets. i.e.,

| $1+i$ | $3+0 i$ | $1+2 i$ | $7+0 i$ | $11+0 i$ | $2+3 i$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | B | C | D | E | F |
| $1+4 i$ | $19+0 i$ | $23+0 i$ | $2+5 i$ | $31+0 i$ | $1+6 i$ |
| G | H | I | J | K | L |
| $4+5 i$ | $43+0 i$ | $47+0 i$ | $2+7 i$ | $59+0 i$ | $5+6 i$ |
| M | N | O | P | Q | R |
| $67+0 i$ | $71+0 i$ | $3+8 i$ | $79+0 i$ | $83+0 i$ | $5+8 i$ |
| S | T | U | V | W | X |
| $4+9 i$ | $1+10 i$ |  |  |  |  |
| Y | Z |  |  |  |  |

The algorithm is defined as follows:

1) Let the message to be encrypted be $W_{1}, W_{2}, \ldots, W_{n}$ (separated as words and omitting spaces).
2) For all $1 \leq i \leq n$, assign each letters in $W_{i}$ with the above defined table.
3) Apply $\varphi_{\mathbb{Z}[i]}$ for each assigned values in $W_{i}$.
4) Construct a cyclic symmetric matrix for each $W_{i}$ separately.
5) Calculate $E\left(\eta\left(W_{i}\right)\right)$, for all $1 \leq i \leq n$
6) Find the $k_{i}^{t h}$ row from the matrix and construct $A_{i}, 1 \leq i \leq n$
7) Evaluate $D\left(A_{i}\right)-\eta\left(W_{i}\right) I_{\eta\left(W_{i}\right)}, 1 \leq i \leq n$, which is the encrypted key. (For each word it is separated by commas)

Algorithm for decryption
a) Let $B_{i}=D\left(A_{i}\right)-\eta\left(W_{i}\right) I_{\eta\left(W_{i}\right)}, 1 \leq i \leq n$
b) Calculate $C_{i}=D\left(B_{i}\right)+\eta\left(B_{i}\right) I_{\eta\left(B_{i}\right)}, 1 \leq i \leq n$
c) Find $E\left(\eta\left(B_{i}\right)\right)=k_{i}, 1 \leq i \leq n$

This gives that first digit of $C_{i}$ is the $k_{i}^{t h}$ letter of the $i^{t h}$ word.
Now, the second digit of $C_{i}$ is the $\left(k_{i}+1\right)^{\text {th }}$ letter of $i^{\text {th }}$ word and so on (This works on cyclic order).
d) Rewrite $C_{i}$ as in the above order.
e) For every digit in $C_{i}$, add1 and then observethat the remaining is in the form $x^{2}+y^{2}$ so write it as $x+$ iy where $0<x<y$ and if $y=0$, write it as $x+0 i$.
f) Convert the digits into alphabets.

## Example 3

Let us consider "WORK HARD"

- Encryption
> Let $W_{1}$ be the word $W O R K$ and $W_{2}$ be HARD
$>$ Assign the positions of the letters.

| W | O | R | K |
| :---: | :---: | :---: | :---: |
| $83+0 i$ | 47 | $5+6 i$ | $31+0 i$ |
|  | $+0 i$ |  |  |


| H | A | R | D |
| :---: | :---: | :---: | :---: |
| $19+0 i$ | $1+i$ | $5+6 i$ | $7+0 i$ |

$>\operatorname{Apply} \varphi_{\text {Z }[i]}$

| W | O | R | K |
| :---: | :---: | :---: | :---: |
| 6888 | 2208 | 60 | 960 |


| H | A | R | D |
| :--- | :--- | :--- | :--- |
| 360 | 1 | 60 | 48 |

> The cyclic symmetric matrix is

$$
M_{1}=\left(\begin{array}{cccc}
6888 & 2208 & 60 & 960 \\
2208 & 60 & 960 & 6888 \\
60 & 960 & 6888 & 2208 \\
960 & 6888 & 2208 & 60
\end{array}\right) \text { and } M_{2}=\left(\begin{array}{cccc}
360 & 1 & 60 & 48 \\
1 & 60 & 48 & 360 \\
60 & 48 & 360 & 1 \\
48 & 360 & 1 & 60
\end{array}\right)
$$

$>$ Here $\eta\left(W_{1}\right)=\eta\left(W_{2}\right)=4$, which is even.

$$
\text { Thus, } E\left(\eta\left(W_{1}\right)\right)=E\left(\eta\left(W_{2}\right)\right)=k_{1}=k_{2}=\frac{4}{2}=2
$$

> The $2^{\text {nd }}$ row of $M_{1}$ forms $A_{1}$ and $2^{\text {nd }}$ row of $M_{2}$ forms $A_{2}$.

$$
\text { i.e., } A_{1}=\left(\begin{array}{llll}
2208 & 60 & 960 & 6888
\end{array}\right) \text { and } A_{2}=\left(\begin{array}{llll}
1 & 60 & 48 & 360
\end{array}\right)
$$

$>D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}=\left(\begin{array}{cccc}2208 & 0 & 0 & 0 \\ 0 & 60 & 0 & 0 \\ 0 & 0 & 960 & 0 \\ 0 & 0 & 0 & 6888\end{array}\right)-\left(\begin{array}{llll}4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 4\end{array}\right)$
$=\left(\begin{array}{cccc}2204 & 0 & 0 & 0 \\ 0 & 56 & 0 & 0 \\ 0 & 0 & 956 & 0 \\ 0 & 0 & 0 & 6884\end{array}\right)$

$$
\begin{aligned}
D\left(A_{2}\right)-\eta\left(W_{2}\right) I_{\eta\left(W_{2}\right)}= & \left(\begin{array}{cccc}
1 & 0 & 0 & 0 \\
0 & 60 & 0 & 0 \\
0 & 0 & 48 & 0 \\
0 & 0 & 0 & 360
\end{array}\right)-\left(\begin{array}{cccc}
4 & 0 & 0 & 0 \\
0 & 4 & 0 & 0 \\
0 & 0 & 4 & 0 \\
0 & 0 & 0 & 4
\end{array}\right) \\
& =\left(\begin{array}{cccc}
-3 & 0 & 0 & 0 \\
0 & 56 & 0 & 0 \\
0 & 0 & 44 & 0 \\
0 & 0 & 0 & 356
\end{array}\right)
\end{aligned}
$$

The encrypted key is 220456956 6884, -3 5644356

- Decryption
$>B_{1}=D\left(A_{1}\right)-\eta\left(W_{1}\right) I_{\eta\left(W_{1}\right)}$

$$
\begin{aligned}
= & \left(\begin{array}{llll}
2204 & 56 & 956 & 6884
\end{array}\right) \\
B_{2} & =D\left(A_{2}\right)-\eta\left(W_{2}\right) I_{\eta\left(W_{2}\right)} \\
& =\left(\begin{array}{llll}
-3 & 56 & 44 & 356
\end{array}\right) \\
= & \left(\begin{array}{llll}
2208 & 60 & 960 & 6888
\end{array}\right) \\
C_{2} & =D\left(B_{2}\right)+\eta\left(B_{2}\right) I_{\eta\left(B_{2}\right)} \\
& =\left(\begin{array}{llll}
1 & 60 & 48 & 360
\end{array}\right)
\end{aligned}
$$

$>C_{1}=D\left(B_{1}\right)+\eta\left(B_{1}\right) I_{\eta\left(B_{1}\right)}$
$\Rightarrow E\left(\eta\left(B_{1}\right)\right)=E\left(\eta\left(B_{2}\right)\right)=\frac{4}{2}=2$
So first digit of $C_{1}$ is the $2^{\text {nd }}$ letter in $W_{1}$ and first digit of $C_{2}$ is $2^{\text {nd }}$ letter in $W_{2}$.

The order is

| 2208 | 60 | 960 | 6888 |
| :---: | :---: | :---: | :---: |
| $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ | $1^{\text {st }}$ |


| 1 | 60 | 48 | 360 |
| :---: | :---: | :---: | :---: |
| $2^{\text {nd }}$ | $3^{r d}$ | $4^{\text {th }}$ | $1^{\text {st }}$ |

$\rightarrow$ Thus the rewritten form is ( $\left.\begin{array}{lllll}6888 & 2208 & 60 & 960\end{array}\right)$ and ( $\left.\begin{array}{llll}360 & 1 & 60 & 48\end{array}\right)$.
$>$ Adding 1 , one can get ( 6889220961961 ) and (361 26149 ), which can be written as $\left(83^{2} 47^{2} 5^{2}+6^{2} 31^{2}\right.$ ) and $\left(1^{2}+1^{2} 5^{2}+6^{2} 7^{2} 19^{2}\right)$. Hence one can get $(83+0 i 47+0 i 5+6 i 31+0 i)$ and $(19+0 i 1+i 5+6 i 7+0 i)$ which corresponds to the words "WORK" and "HARD".

## IV. CONCLUSION

In this paper, there are two algorithms. One involving integer primes and the other uses Gaussian primes. One can maintain comparatively more secrecy in second one than that of first one. To improve much more security, one can modify the assignment by taking large primes as well as Gaussian primes.

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