



iJRASET

International Journal For Research in
Applied Science and Engineering Technology



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Volume: 11 Issue: VII Month of publication: July 2023

DOI: <https://doi.org/10.22214/ijraset.2023.54782>

www.ijraset.com

Call:  08813907089

E-mail ID: ijraset@gmail.com

Designing FIR Filter using Distributed Arithmetic

Bindu K S¹, Chidananda Murthy M V², M N Eshwarappa³, Gaurav Dutta Saxena⁴

^{1, 2, 3}Dept of ECE, Sri Siddhartha Institute of Technology, Tumkur, India

⁴LEOS-ISRO, Bangalore, India

Abstract: Distributed arithmetic technique is employed in this paper to develop the FIR filter. To eliminate undesired signal and noise, FIR filters are frequently employed as digital filters in digital signal processing. This method also calls for shift registers and an accumulator and stores the FIR filter coefficients in a look-up table (LUT). By using this method, shift and accumulate can take the place of the multipliers in the FIR filter. The size of the LUT can be reduced for larger filter coefficients by dividing it into any number of LUTs, which are made up of taps that are FIR filter coefficients. FIR filter is created in MATLAB using the DA technique, and manual computation yields the same result.

Keywords: MATLAB, FIR filter, Distributed arithmetic, filter coefficients, LUT

I. INTRODUCTION

Digital signal processing use FIR filters for a variety of purposes, including frequency selection, smoothing, and noise reduction. The complexity and power consumption of the FIR filter are increased by the necessity of a large number of multipliers to implement the necessary filter coefficients. By lowering the quantity of multipliers necessary for filter design, this problem can be resolved. The computation complexity of the multiplication operations employed in the filter design is reduced by the use of distributed arithmetic in the construction of FIR filters. This method substitutes another operation for multiplication. Page Layout

II. FILTER DESIGN

A. FIR filter with Multiplier

A finite number of input samples are used by the FIR filter to generate a finite number of output responses. It is chosen because it produces a linear phase response as a result of the symmetry of the filter coefficients. In a linear phase response, each component is delayed by the same amount of time and is also helpful in maintaining the phase of the signal, which is helpful in applications for image processing and audio. Each input sample is multiplied by a corresponding filter coefficient in order for the filter to work on the input signal. The results are then added together to create the filtered output sample.

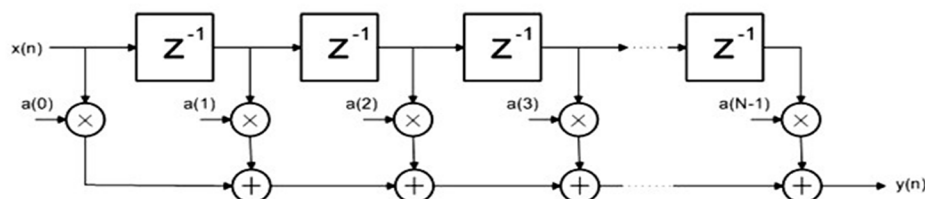


Fig: Conventional tapped delay line FIR filter

The FIR operation is described by the equation

$$y(n) = a_0x(n) + a_1x(n-1) + a_2x(n-2) + a_3x(n-3) + \dots + a_Nx(n-N) \\ = \sum_{i=0}^N a_i x(n-i)$$

where,

$x(0)$ is input signal

$y(n)$ is output signal

a_0 is taps or filter coefficients

Figure shows FIR filter with has N adder, N+1 filter coefficients (or taps) and N+1 multipliers If order of FIR filter is 4 then equation is

$$Y(n) = \sum_{i=0}^3 a(i) x(n-i) \\ y(n) = a(0)x(n) + a(1)x(n-1) + a(2)x(n-2) + a(3)x(n-3) + a(4)x(n-4)$$

The filter coefficients can be used to calculate the frequency response of a filter, allowing for the design of a variety of filters, including high-pass, low-pass, band-pass, and band-stop filters. Windowing approach can be used to create the necessary filter taps or coefficients by multiplying the desired frequency response by the window function. Least Square and Parks McClellan are two additional implementation strategies that can be employed for filter design. Based on filter performance metrics including ripple, transition bandwidth, and attenuation, the FIR filter is chosen. FIR filters are preferred over IIR filters due to its advantages such as linear phase response, stability, and the possibility to construct same frequency responses.

B. FIR filter design using Distributed arithmetic

Digital signal processing uses the Distributed arithmetic technique to carry out computations quickly and effectively. This method replaces the standard addition and multiplication operations with algorithms that are implemented on hardware to save FPGA resources. This method lessens the number of arithmetic operations, which in turn lessens the complexity of the hardware. It is used to substitute a Look Up Table and a shifter-accumulator for all multiplications and additions. Multiplying $c[n]x[n]$ results in a multiplication by a constant because DA depends on knowing the filter coefficients.

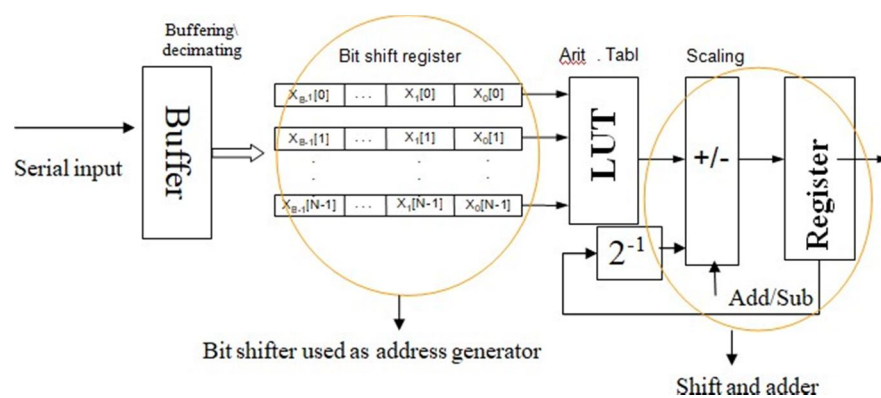


Fig: Block diagram of implementation of FIR filter using DA

The above image depicts the block design for the DA for FIR filter. When implementing DA, the number of inputs that must be stored must match the length of the coefficients in each buffer stage. Then, the LSB bits of each coefficient are used as the LUT's address. To accept an N-bit address, where N is the number of coefficients, a $2n$ word LUT is preprogrammed to do so. Each mapping is given the proper weight by the combined effect of two elements. A shift-adder is effectively used to implement the accumulation. For hardware implementation, shift the accumulator content itself in each direction by one bit to the right rather than shifting each intermediate value by power factor, which necessitates an expensive barrel shifter.

Below gives the explanation of distributed arithmetic technique:

- 1) Generation of coefficients for sampling frequency = 4KHz, $F_{pass} = 60\text{Hz}$, $F_{stop} = 400\text{Hz}$, $A_{pass} = 0.1\text{dB}$, $A_{stop} = 60\text{dB}$ from MATLAB FDA tool and stored in a text file

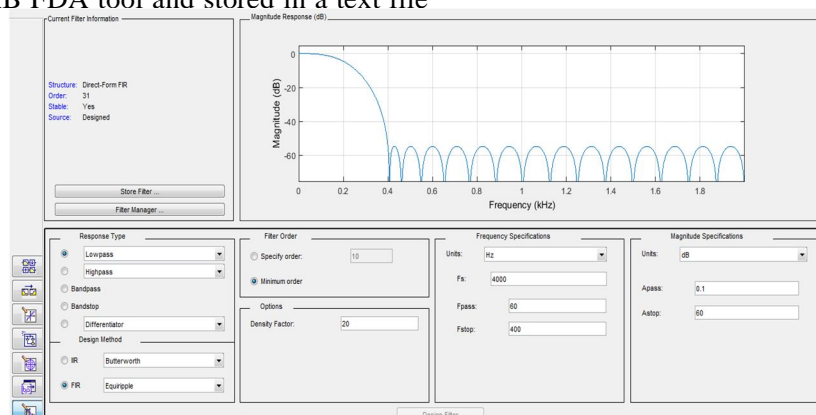
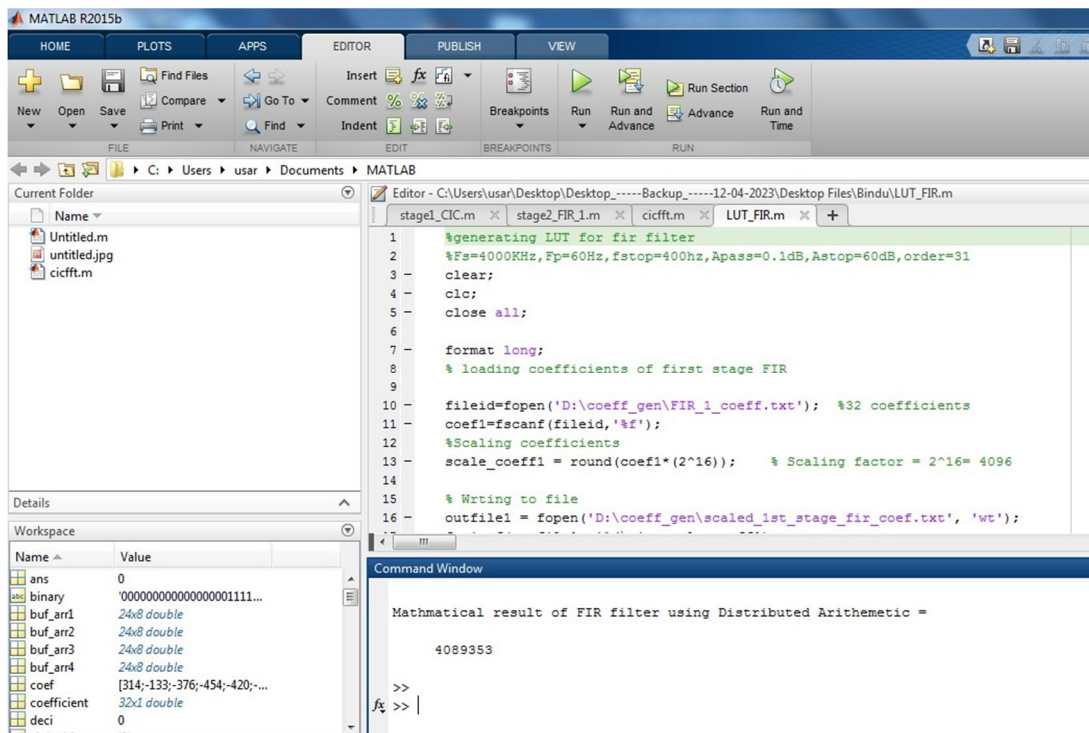


Fig: Coefficient generation in MATLAB FDA tool

- 2) MATLAB code is made to scale by power of 16 for the coefficients generated and to take two's complement value of all generated coefficients



```

1 %generating LUT for fir filter
2 %Fs=4000KHz, Fp=60Hz, fstop=400hz, Apass=0.1dB, Astop=60dB, order=31
3 clear;
4 clc;
5 close all;
6
7 format long;
8 % loading coefficients of first stage FIR
9
10 fileid=fopen('D:\coeff_gen\FIR_1_coeff.txt'); %32 coefficients
11 coef1=fscanf(fileid,'%f');
12 %Scaling coefficients
13 scale_coef1 = round(coef1*(2^16)); % Scaling factor = 2^16= 4096
14
15 % Writing to file
16 outfile = fopen('D:\coeff_gen\scaled_1st_stage_fir_coef.txt', 'wt');

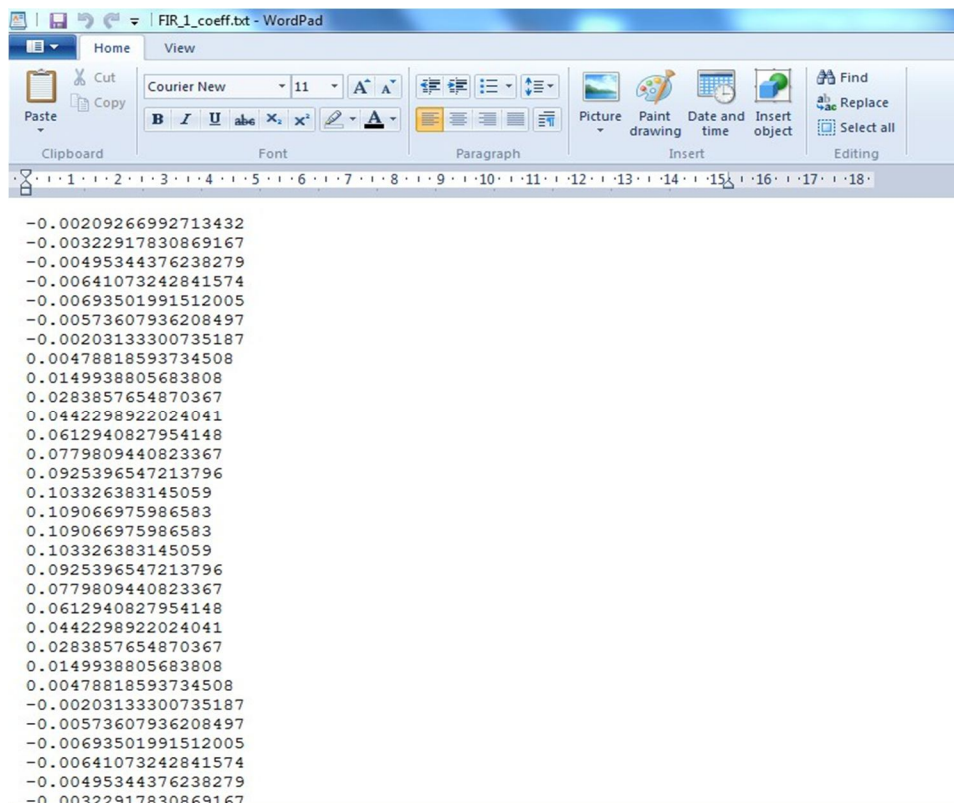
```

Command Window

Mathematical result of FIR filter using Distributed Arithmetic =

4089353

Fig: MATLAB code to generate FIR filter using DA



```

-0.00209266992713432
-0.00322917830869167
-0.00495344376238279
-0.00641073242841574
-0.00693501991512005
-0.00573607936208497
-0.00203133300735187
0.00478818593734508
0.0149938805683808
0.0283857654870367
0.0442298922024041
0.0612940827954148
0.0779809440823367
0.0925396547213796
0.103326383145059
0.109066975986583
0.109066975986583
0.103326383145059
0.0925396547213796
0.0779809440823367
0.0612940827954148
0.0442298922024041
0.0283857654870367
0.0149938805683808
0.00478818593734508
-0.00203133300735187
-0.00573607936208497
-0.00693501991512005
-0.00641073242841574
-0.00495344376238279
-0.00322917830869167

```

Fig: Coefficient generated from MATLAB FDA tool and loaded to text file

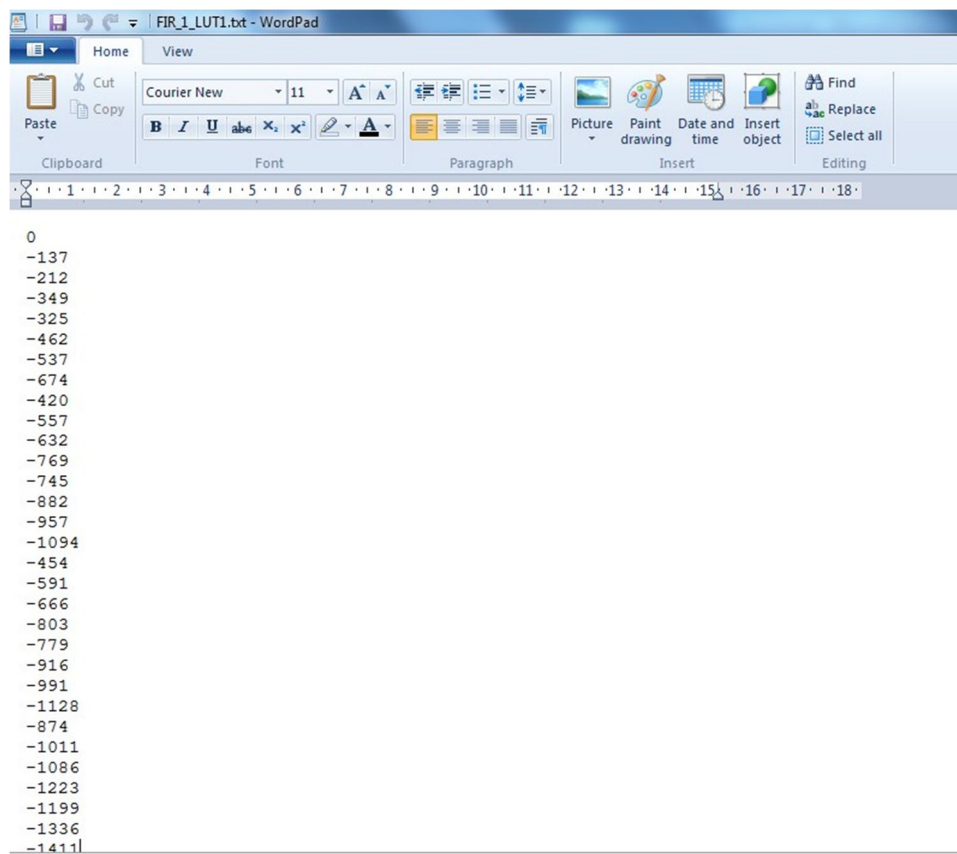
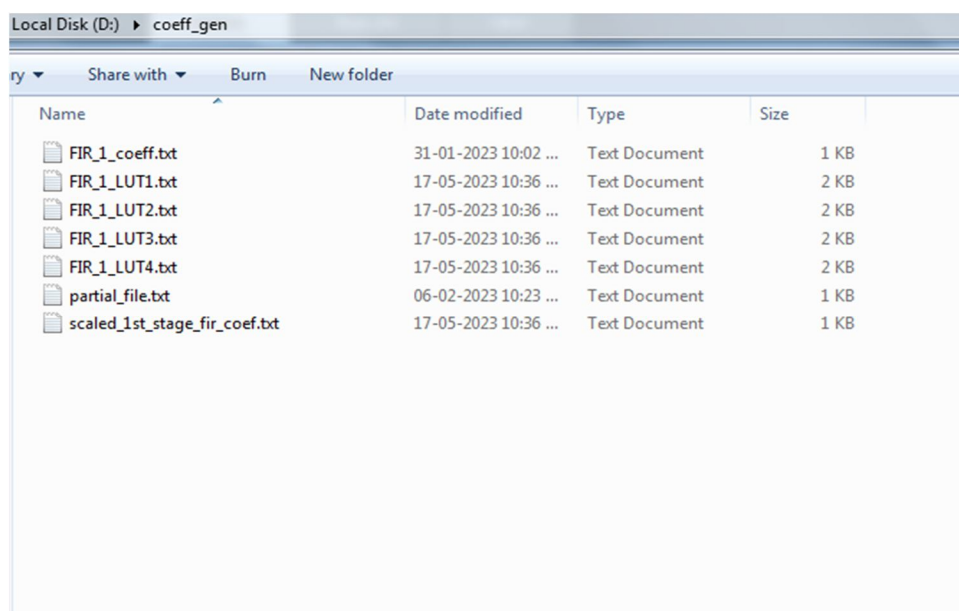


Fig: Coefficient scaled by factor 16

- 3) When more coefficients are considered the look up table is divided ,here four lookup table is considered hence the scaled two's complement coefficients can be seen in four different text files this files are considered as the look up table for DA



The screenshot shows a Windows File Explorer window titled 'Local Disk (D:) > coeff_gen'. The table below lists the files in this directory.

Name	Date modified	Type	Size
FIR_1_coeff.txt	31-01-2023 10:02 ...	Text Document	1 KB
FIR_1_LUT1.txt	17-05-2023 10:36 ...	Text Document	2 KB
FIR_1_LUT2.txt	17-05-2023 10:36 ...	Text Document	2 KB
FIR_1_LUT3.txt	17-05-2023 10:36 ...	Text Document	2 KB
FIR_1_LUT4.txt	17-05-2023 10:36 ...	Text Document	2 KB
partial_file.txt	06-02-2023 10:23 ...	Text Document	1 KB
scaled_1st_stage_fir_coef.txt	17-05-2023 10:36 ...	Text Document	1 KB

Fig: Files generated in different stages

										256_partial products				
Sl.NO	32_coefficients			LUT_1	LUT_2	LUT_3	LUT_4			LUT_1	LUT_2	LUT_3	LUT_4	
1	-137									0	0	0	0	0
2	-212		h7	-137	983	7148	314			1	-137	983	7148	314
3	-325		h6	-212	1860	6772	-133			2	-212	1860	6772	-133
4	-420		h5	-325	2899	6065	-376			3	-349	2843	13920	181
5	-454		h4	-420	4017	5111	-454			4	-325	2899	6065	-376
6	-376		h3	-454	5111	4017	-420			5	-462	3882	13213	-62
7	-133		h2	-376	6065	2899	-325			6	-537	4759	12837	-509
8	314		h1	-133	6772	1860	-212			7	-674	5742	19985	-195
9	983		h0	314	7148	983	-137			8	-420	4017	5111	-454
10	1860									9	-557	5000	12259	-140
11	2899									10	-632	5877	11883	-587
12	4017									11	-769	6860	19031	-273
13	5111									12	-745	6916	11176	-830
14	6065									13	-882	7899	18324	-516
HAND_CALCULATIONS														
	bit	pp0	pp1	pp2	pp3	sum								
15	6772		0	0	19952	-1199	18753			14	-957	8776	17948	-963
16	7148	0th	0	0	19952	-1199	18753			15	-1094	9759	25096	-649
17	7148	1st	0	0	20935	-195	20740	41480		16	-454	5111	4017	-420
18	6772	2nd	-694	19090	18714	-694	36416	145664		17	-591	6094	11165	-106
19	6065	3rd	-564	20836	10111	-697	29686	237488		18	-666	6971	10789	-553
20	5111	4th	-649	25096	5742	-360	29829	477264		19	-803	7954	17937	-239
21	4017	5th	0	34855	0	-2057	32798	1049536		20	-779	8010	10082	-796
22	2899	6th	0	0	34855	-1743	33112	2119168		21	-916	8993	17230	-482
23	1860							4089353		22	-991	9870	16854	-929

Fig: Manual calculation of FIR filter in DA technique

	A	B	C	D
Sl.NO	Sine_data	coefficients	convolution	
1	1	0	-137	0
2	2	4	-212	-848
3	2	8	-325	-2600
4	2	12	-420	-5040
5	2	16	-454	-7264
6	2	20	-376	-7520
7	2	24	-133	-3132
8	2	28	314	8732
9	2	32	983	31456
10	2	36	1860	66960
11	2	40	2899	115960
12	2	44	4017	176748
13	2	48	5111	245328
14	2	52	6065	315380
15	2	56	6772	379232
16	2	60	7148	428880
17	2	64	7148	457472
18	2	68	6772	460496
19	2	71	6065	430615
20	2	75	5111	383325
21	2	79	4017	317343
22	2	83	2899	240617
23	2	87	1860	161620
24	2	90	983	88470
25	2	94	314	29516
26	2	98	-133	-13034
27	2	102	-376	-38352
28	2	105	-454	-47670
29	2	109	-420	-45780
30	2	113	-325	-36725
31	2	116	-212	-24532
32	2	120	-137	-16440
33	2			4089353

Fig: Manual calculation of FIR filter using FIR formula

The final value generated by MATLAB code using Distributed Arithmetic technique, manual calculation using DA and formula calculated value of FIR filter all results found to be same and examined.

III.CONCLUSIONS

Finite impulse response filters are frequently used in digital signal processing applications. The multiplier-less FIR filter is built using distributed arithmetic, which incorporates a look-up table and partitioning. Memory access takes longer than multiplication. LUT split reduces the need for memory. His approach reduces the amount of time, space, and power used. This architecture delivers an effective area-time power implementation with a great deal reduced latency and area-delay complexity when compared to other FIR Filter topologies.

REFERENCES

- [1] Implementation of a low-power, space-efficient FIR filter suitable for multiple tape, Very Large Scale Integration (VLSI) Systems, vol. 11, Kyung- Saeng, K., and Lee, K.
- [2] Meyer-Base University. Digital Signal Processing utilising Field Programmable Gate Arrays, 2nd ed., Chapter 2, pages 60–66.
- [3] "Digital Filter Design," Wiley-Interscience, 1987, by T. W. Parks and C. S. Burrus.
- [4] "Digital Signal Processing: A Practical Approach," C. R. Johnson and F. J. Taylor, Addison-Wesley, 1993.
- [5] PK Meher (2006), p. Hardware eicient systemization of DA-based calculation of initial digital convolution was published in IEEE Transactions on Circuit and Systems II: Express Briefs, vol. 53(8), pp. 707–711.
- [6] Meher P K, Chandrasekaran S, et al., "FPGA realisation of FIR filters by efficient and flexible systematisation using distributed arithmetic," IEEE Transactions on Signal Processing, vol. 56(7).



10.22214/IJRASET



45.98



IMPACT FACTOR:
7.129



IMPACT FACTOR:
7.429



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Call : 08813907089  (24*7 Support on Whatsapp)