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International Journal For Research in  
Applied Science and Engineering Technology



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# INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

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**Volume:** 2017 **Issue:** conference **Month of publication:** December 2017

**DOI:**

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# Lower level subsets of an anti-fuzzy HX ideal of a HX ring

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**Abstract:** In this paper, we introduce the concept of lower level subsets of an anti-fuzzy HX ideal of a HX ring. We also discuss the relation between a given anti-fuzzy HX ideals of a HX ring and its lower level HX ideals and investigate the conditions under which a given HX ring has a properly inclusive chain of HX ideals. We introduce the concept of homomorphism and anti homomorphism of lower level subsets of an anti-fuzzy HX ideal and discuss some of its properties.

**Keywords:** HX ring, anti-fuzzy HX ideal, homomorphism, lower level subset.

**AMS Subject Classification (2000):** 20N25, 03E72, 03F055, 06F35, 03G25.

## I. INTRODUCTION

In 1965, Lotfi.A.Zadeh [9] introduced the concept of fuzzy set. Fuzzy sets attracted many mathematicians and grew enormously by finding applications in many areas. We introduce a notion of anti fuzzy HX ideal of a HX ring and some of its properties are discussed. We prove that a fuzzy subset of a HX ring is an anti fuzzy HX ideal if and only if the lower level subsets are HX ideals of a HX ring. In 1982 Wang-jin Liu [6] introduced the concept of fuzzy subring and fuzzy ideal. In 1988, Professor Li Hong Xing [5] proposed the concept of HX ring and derived some of its properties, then Professor Zhong [10] gave the structures of HX ring on a class of ring.

## II. PRELIMINARIES

In this section, we site the fundamental definitions that will be used in the sequel. Throughout this paper,  $R = (R, +, \cdot)$  is a Ring,  $e$  is the additive identity element of  $R$  and  $xy$ , we mean  $x \cdot y$ .

## III. LOWER LEVEL SUBSETS OF AN ANTI-FUZZY HX IDEAL

### A. Definition

Let  $\lambda_\mu$  be an anti-fuzzy HX ideal of a HX ring  $\mathfrak{R}$ . For any  $t \in [0,1]$ , we define the set  $L(\lambda_\mu; t) = \{ A \in \mathfrak{R} / \lambda_\mu(A) \leq t \}$  is called a lower level subset of  $\lambda_\mu$ .

### B. Theorem

Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}$  and  $L(\lambda_\mu; t)$  is non-empty, then for  $t \in [0,1]$ ,  $L(\lambda_\mu; t)$  is a HX right ideal of  $\mathfrak{R}$ .

1) *Proof:* Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}$ .

For any  $A, B \in L(\lambda_\mu; t)$ , we have,  $\lambda_\mu(A) \leq t$  and  $\lambda_\mu(B) \leq t$ .

$$\begin{aligned} \text{Now, } \lambda_\mu(A - B) &\leq \max \{ \lambda_\mu(A), \lambda_\mu(B) \} \\ &\leq \max \{ t, t \} = t, \text{ for some } t \in [0,1]. \\ \lambda_\mu(A - B) &\leq t. \end{aligned}$$

For any  $A \in L(\lambda_\mu; t)$  and  $B \in \mathfrak{R}$ , we have,  $\lambda_\mu(A) \leq t$ .

$$\begin{aligned} \text{Now, } \lambda_\mu(AB) &\leq \lambda_\mu(A) \leq t. \\ \lambda_\mu(AB) &\leq t. \end{aligned}$$

Hence,  $A - B, AB \in L(\lambda_\mu; t)$ .

Hence,  $L(\lambda_\mu; t)$  is a HX right ideal of a HX ring  $\mathfrak{R}$ .

### C. Theorem

Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}$  and  $L(\lambda_\mu; t)$  is non-empty, then for any  $t \in [0,1]$ ,  $L(\lambda_\mu; t)$  is a HX left ideal of  $\mathfrak{R}$ .

1) *Proof:* Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}$ .

For any  $A, B \in L(\lambda_\mu; t)$ , we have,  $\lambda_\mu(A) \leq t$  and  $\lambda_\mu(B) \leq t$ .

Now,  $\lambda_\mu(A - B) \leq \max \{ \lambda_\mu(A), \lambda_\mu(B) \}$   
 $\leq \max \{ t, t \} = t$ , for some  $t \in [0,1]$ .

$$\lambda_\mu(A - B) \leq t.$$

For any  $A \in L(\lambda_\mu; t)$  and  $B \in \mathfrak{R}$ , we have,  $\lambda_\mu(A) \leq t$ .

Now,  $\lambda_\mu(BA) \leq \lambda_\mu(A) \leq t$ .

$$\lambda_\mu(BA) \leq t$$

Hence,  $A - B, BA \in L(\lambda_\mu; t)$ .

Hence,  $L(\lambda_\mu; t)$  is a HX left ideal of a HX ring  $\mathfrak{R}$ .

#### D. Theorem

Let  $\lambda_\mu$  be an anti-fuzzy HX ideal of a HX ring  $\mathfrak{R}$  and  $L(\lambda_\mu; t)$  is non-empty, then for  $t \in [0,1]$ ,  $L(\lambda_\mu; t)$  is a HX ideal of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

#### E. Theorem

Let  $\mathfrak{R}$  be a HX ring and  $\lambda_\mu$  be a fuzzy subset of  $\mathfrak{R}$  such that  $L(\lambda_\mu; t)$  is a HX right ideal of  $\mathfrak{R}$  for all  $t \in [0,1]$  then  $\lambda_\mu$  is an anti-fuzzy HX right ideal of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

#### F. Theorem

Let  $\mathfrak{R}$  be a HX ring and  $\lambda_\mu$  be a fuzzy subset of  $\mathfrak{R}$  such that  $L(\lambda_\mu; t)$  is a HX left ideal of  $\mathfrak{R}$  for all  $t \in [0,1]$  then  $\lambda_\mu$  is an anti-fuzzy HX left ideal of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

#### G. Theorem

Let  $\mathfrak{R}$  be a HX ring and  $\lambda_\mu$  be a fuzzy subset of  $\mathfrak{R}$  such that  $L(\lambda_\mu; t)$  is a HX ideal of  $\mathfrak{R}$  for all  $t \in [0,1]$  then  $\lambda_\mu$  is an anti-fuzzy HX ideal of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

#### H. Theorem

A fuzzy subset  $\lambda_\mu$  of  $\mathfrak{R}$  is a fuzzy HX ideal of a HX ring  $\mathfrak{R}$  if and only if the level HX subsets  $L(\lambda_\mu; t)$ ,  $t \in \text{Image } \lambda_\mu$ , are HX ideals of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

#### I. Theorem

Let  $\lambda_\mu$  be an anti-fuzzy HX ideal of a HX ring  $\mathfrak{R}$ . If two lower level HX ideals,  $L(\lambda_\mu; t_1), L(\lambda_\mu; t_2)$  with  $t_1 < t_2$  of  $\lambda_\mu$  are equal if and only if there is no  $A$  in  $\mathfrak{R}$  such that

$$t_1 \leq \lambda_\mu(A) < t_2.$$

1) *Proof:* It is clear.

#### J. Theorem

Any HX ideal  $H$  of a HX ring  $\mathfrak{R}$  can be realized as a lower level HX ideal of some anti-fuzzy HX ideal of  $\mathfrak{R}$ .

1) *Proof:* It is clear.

### K. Remark

As a consequence of the Theorem 3.9 and 3.10, the lower level HX ideals of an anti-fuzzy HX ideal  $\lambda^\mu$  of a HX ring  $\mathfrak{R}$  form a chain. Since  $\lambda^\mu(Q) \leq \lambda^\mu(A)$  for all  $A$  in  $\mathfrak{R}$  and therefore  $L(\lambda^\mu; t_0)$ , where  $\lambda^\mu(Q) = t_0$  is the smallest and we have the chain :  $\{Q\} = L(\lambda^\mu; t_0) \subset L(\lambda^\mu; t_1) \subset L(\lambda^\mu; t_2) \subset \dots \subset L(\lambda^\mu; t_n) = \mathfrak{R}$ , where  $t_0 < t_1 < t_2 < \dots < t_n$ .

## III. HOMOMORPHISM AND ANTI HOMOMORPHISM OF A LOWER LEVEL SUBSETS OF AN ANTI-FUZZY HX IDEAL OF A HX RING

In this section, we introduce the concept of homomorphism and anti homomorphism of lower level subsets of an anti-fuzzy HX ideal and discuss some of its properties. Throughout this section,  $t \in [0,1]$ .

### A. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism and onto, then the anti-image of a lower level HX right ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX right ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be a homomorphism.

Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ . Clearly,  $f(\lambda_\mu)$  is an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_2$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Choose  $t \in [0,1]$  in such a way that  $X, Y \in L(\lambda_\mu; t)$  and hence  $X-Y \in L(\lambda_\mu; t)$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(Y) \leq t$  and  $\lambda_\mu(X-Y) \leq t$ .

For this  $t \in [0,1]$ , let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(XY) \leq t$ .

We have to prove that  $L(f(\lambda_\mu); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

Let  $X, Y \in L(\lambda_\mu; t)$  and hence  $X-Y \in L(\lambda_\mu; t)$ .

For  $f(X), f(Y) \in L(f(\lambda_\mu); t)$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X) - f(Y)) &= (f(\lambda_\mu))(f(X-Y)), \\ &= \lambda_\mu(X-Y) \\ &\leq t \\ (f(\lambda_\mu))(f(X) - f(Y)) &\leq t. \\ (f(X) - f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

For,  $f(X) \in L(f(\lambda_\mu); t)$  and  $f(Y) \in \mathfrak{R}_2$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X) f(Y)) &\leq (f(\lambda_\mu))f(X) \\ &\leq t \\ (f(\lambda_\mu))(f(X)f(Y)) &\leq t. \\ (f(X) f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

Hence,  $L(f(\lambda_\mu); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

### B. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism and onto, then the anti-image of a lower level HX left ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX left ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX left ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be a homomorphism.

Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ . Clearly,  $f(\lambda_\mu)$  is an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_2$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Choose  $t \in [0,1]$  in such a way that  $X, Y \in L(\lambda_\mu; t)$  and hence  $X-Y \in L(\lambda_\mu; t)$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(Y) \leq t$  and  $\lambda_\mu(X-Y) \leq t$ .

For this  $t \in [0,1]$ , let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(XY) \leq t$ .

We have to prove that  $L(f(\lambda_\mu); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

Let  $X, Y \in L(\lambda_\mu; t)$  and hence  $X-Y \in L(\lambda_\mu; t)$ .

For  $f(X), f(Y) \in L(f(\lambda_\mu); t)$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X) - f(Y)) &= (f(\lambda_\mu))(f(X-Y)), \\ &= \lambda_\mu(X-Y) \\ &\leq t \\ (f(\lambda_\mu))(f(X) - f(Y)) &\leq t. \\ (f(X) - f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $YX \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

For,  $f(X) \in L(f(\lambda_\mu); t)$  and  $f(Y) \in \mathfrak{R}_2$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(Y) f(X)) &\leq (f(\lambda_\mu))(f(X)) \\ &\leq t \\ (f(\lambda_\mu))(f(Y) f(X)) &\leq t. \\ (f(Y) f(X)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

Hence,  $L(f(\lambda_\mu); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

### C. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism and onto, then the anti-image of a lower level HX ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

1) *Proof:* It is clear.

### D. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX right ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be a homomorphism.

Let  $\eta_\alpha$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_2$ . Clearly,  $f^{-1}(\eta_\alpha)$  is an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ . Let  $X, Y \in \mathfrak{R}_1$  then  $f(X), f(Y) \in \mathfrak{R}_2$ .

Choose  $t \in [0, 1]$  in such a way that  $f(X), f(Y) \in L(\eta_\alpha; t)$  and hence  $f(X) - f(Y) \in L(\eta_\alpha; t)$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(Y)) \leq t$  and  $\eta_\alpha(f(X) - f(Y)) \leq t$ .

For this  $t \in [0, 1]$ ,  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(X)f(Y)) \leq t$ .

We have to prove that  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ . Now, Let  $X, Y \in L(f^{-1}(\eta_\alpha); t)$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(X - Y) &= \eta_\alpha(f(X - Y)) \\ &= \eta_\alpha(f(X) - f(Y)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(X - Y) &\leq t \\ X - Y &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Let  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(XY) &\leq (f^{-1}(\eta_\alpha))(X) \\ &= \eta_\alpha(f(X)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(XY) &\leq t \\ XY &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Hence,  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ .

#### E. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX left ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be a homomorphism.

Let  $\eta_\alpha$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_2$ . Clearly,  $f^{-1}(\eta_\alpha)$  is an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ . Let  $X, Y \in \mathfrak{R}_1$  then  $f(X), f(Y) \in \mathfrak{R}_2$ .

Choose  $t \in [0, 1]$  in such a way that  $f(X), f(Y) \in L(\eta_\alpha; t)$  and hence  $f(X) - f(Y) \in L(\eta_\alpha; t)$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(Y)) \leq t$  and  $\eta_\alpha(f(X) - f(Y)) \leq t$ .

For this  $t \in [0, 1]$ ,  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(X)f(Y)) \leq t$ .

We have to prove that  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ . Now, Let  $X, Y \in L(f^{-1}(\eta_\alpha); t)$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(X - Y) &= \eta_\alpha(f(X - Y)) \\ &= \eta_\alpha(f(X) - f(Y)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(X - Y) &\leq t \\ X - Y &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Let  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(XY) &\leq (f^{-1}(\eta_\alpha))(Y) \\ &= \eta_\alpha(f(Y)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(XY) &\leq t \\ XY &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Hence,  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ .

#### F. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX ideal of an anti-fuzzy HX ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX ideal of an anti-fuzzy HX ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* It is clear.

#### G. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is an anti homomorphism and onto, then the anti-image of a lower level HX right ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX left ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX left ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

*I) Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be an anti homomorphism.

Let  $\lambda_\mu$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ . Clearly,  $f(\lambda_\mu)$  is an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_2$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Choose  $t \in [0,1]$  in such a way that  $X, Y \in L(\lambda_\mu; t)$  and hence  $Y-X \in L(\lambda_\mu; t)$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(Y) \leq t$  and  $\lambda_\mu(Y-X) \leq t$ .

For this  $t \in [0,1]$ , let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(XY) \leq t$ .

We have to prove that  $L(f(\lambda_\mu); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

Let  $X, Y \in L(\lambda_\mu; t)$  and hence  $Y-X \in L(\lambda_\mu; t)$ .

For  $f(X), f(Y) \in L(f(\lambda_\mu); t)$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X)-f(Y)) &= (f(\lambda_\mu))(f(Y-X)), \\ &= \lambda_\mu(Y-X) \\ &\leq t \\ (f(\lambda_\mu))(f(X)-f(Y)) &\leq t. \\ (f(X)-f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

For,  $f(X) \in L(f(\lambda_\mu); t)$  and  $f(Y) \in \mathfrak{R}_2$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(Y)f(X)) &\leq (f(\lambda_\mu))(f(X)) \\ &\leq t \\ (f(\lambda_\mu))(f(Y)f(X)) &\leq t. \\ (f(Y)f(X)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

Hence,  $L(f(\lambda_\mu); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

#### H. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is an anti homomorphism and onto, then the anti-image of a lower level HX left ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX right ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

*I) Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be an anti homomorphism.

Let  $\lambda_\mu$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ . Clearly,  $f(\lambda_\mu)$  is an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_2$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Choose  $t \in [0,1]$  in such a way that  $X, Y \in L(\lambda_\mu; t)$  and hence  $Y-X \in L(\lambda_\mu; t)$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(Y) \leq t$  and  $\lambda_\mu(Y-X) \leq t$ .

For this  $t \in [0,1]$ , let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $XY \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

Then,  $\lambda_\mu(X) \leq t$  and  $\lambda_\mu(XY) \leq t$ .

We have to prove that  $L(f(\lambda_\mu); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

Let  $X, Y \in L(\lambda_\mu; t)$  and hence  $Y-X \in L(\lambda_\mu; t)$ .

For  $f(X), f(Y) \in L(f(\lambda_\mu); t)$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X)-f(Y)) &= (f(\lambda_\mu))(f(Y-X)), \\ &= \lambda_\mu(Y-X) \\ &\leq t \\ (f(\lambda_\mu))(f(X)-f(Y)) &\leq t. \\ (f(X)-f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

let  $X \in L(\lambda_\mu; t)$  and  $Y \in \mathfrak{R}_1$  then  $YX \in L(\lambda_\mu; t)$ , as  $L(\lambda_\mu; t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$ .

For,  $f(X) \in L(f(\lambda_\mu); t)$  and  $f(Y) \in \mathfrak{R}_2$ ,

$$\begin{aligned} (f(\lambda_\mu))(f(X) f(Y)) &\leq (f(\lambda_\mu))f(X) \\ &\leq t \\ (f(\lambda_\mu))(f(X)f(Y)) &\leq t. \\ (f(X) f(Y)) &\in L(f(\lambda_\mu); t). \end{aligned}$$

Hence,  $L(f(\lambda_\mu); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

#### I. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\lambda_\mu$  be an anti-fuzzy HX ideal on  $\mathfrak{R}_1$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is an anti homomorphism and onto, then the anti-image of a lower level HX ideal  $L(\lambda_\mu; t)$  of an anti-fuzzy HX ideal  $\lambda_\mu$  of a HX ring  $\mathfrak{R}_1$  is a lower level HX ideal  $L(f(\lambda_\mu); t)$  of an anti-fuzzy HX ideal  $f(\lambda_\mu)$  of a HX ring  $\mathfrak{R}_2$ .

1) *Proof:* It is clear.

#### J. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX right ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is an anti homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be an anti homomorphism.

Let  $\eta_\alpha$  be an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_2$ . Clearly,  $f^{-1}(\eta_\alpha)$  is an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ . Let  $X, Y \in \mathfrak{R}_1$  then  $f(X), f(Y) \in \mathfrak{R}_2$ .

Choose  $t \in [0, 1]$  in such a way that  $f(X), f(Y) \in L(\eta_\alpha; t)$  and hence,  $f(Y) - f(X) \in L(\eta_\alpha; t)$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(Y)) \leq t$  and  $\eta_\alpha(f(Y) - f(X)) \leq t$ .

For this  $t \in [0, 1]$ ,  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(X)f(Y)) \leq t$ .

We have to prove that  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ . Now, Let  $X, Y \in L(f^{-1}(\eta_\alpha); t)$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(X - Y) &= \eta_\alpha(f(X - Y)) \\ &= \eta_\alpha(f(Y) - f(X)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(X - Y) &\leq t \\ X - Y &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Let  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX right ideal of an anti-fuzzy HX right ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(YX) &\leq f^{-1}(\eta_\alpha)(X) \\ &= \eta_\alpha(f(X)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(YX) &\leq t \\ YX &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Hence,  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX left ideal of an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_1$ .

#### K. Theorem



Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX left ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is a homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* Let  $R_1$  and  $R_2$  be any two rings and  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  be an anti homomorphism.

Let  $\eta_\alpha$  be an anti-fuzzy HX left ideal of a HX ring  $\mathfrak{R}_2$ . Clearly,  $f^{-1}(\eta_\alpha)$  is an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ . Let  $X$  and  $Y$  in  $\mathfrak{R}_1$ , implies  $f(X)$  and  $f(Y)$  in  $\mathfrak{R}_2$ .

Let  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ . Let  $X, Y \in \mathfrak{R}_1$  then  $f(X), f(Y) \in \mathfrak{R}_2$ .

Choose  $t \in [0, 1]$  in such a way that  $f(X), f(Y) \in L(\eta_\alpha; t)$  and hence  $f(Y) - f(X) \in L(\eta_\alpha; t)$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(Y)) \leq t$  and  $\eta_\alpha(f(Y) - f(X)) \leq t$ .

For this  $t \in [0, 1]$ ,  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

Then,  $\eta_\alpha(f(X)) \leq t$ ,  $\eta_\alpha(f(X)f(Y)) \leq t$ .

We have to prove that  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ . Now, Let  $X, Y \in L(f^{-1}(\eta_\alpha); t)$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(X - Y) &= \eta_\alpha(f(X - Y)) \\ &= \eta_\alpha(f(Y) - f(X)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(X - Y) &\leq t \\ X - Y &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Let  $f(X) \in L(\eta_\alpha; t)$  and  $f(Y) \in \mathfrak{R}_2$  then  $f(X)f(Y) \in L(\eta_\alpha; t)$ , as  $L(\eta_\alpha; t)$  be a lower level HX left ideal of an anti-fuzzy HX left ideal  $\eta_\alpha$  of the HX ring  $\mathfrak{R}_2$ .

$$\begin{aligned} (f^{-1}(\eta_\alpha))(XY) &\leq (f^{-1}(\eta_\alpha))(X) \\ &= \eta_\alpha(f(X)) \\ &\leq t \\ (f^{-1}(\eta_\alpha))(XY) &\leq t \\ X Y &\in L(f^{-1}(\eta_\alpha); t). \end{aligned}$$

Hence,  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX right ideal of an anti-fuzzy HX right ideal of a HX ring  $\mathfrak{R}_1$ .

### L. Theorem

Let  $R_1$  and  $R_2$  be any two rings,  $\mathfrak{R}_1$  and  $\mathfrak{R}_2$  be HX rings on  $R_1$  and  $R_2$  respectively. Let  $\eta_\alpha$  be an anti-fuzzy HX ideal on  $\mathfrak{R}_2$ . If  $f: \mathfrak{R}_1 \rightarrow \mathfrak{R}_2$  is an anti homomorphism on HX rings. Let  $L(\eta_\alpha; t)$  be a lower level HX ideal of an anti-fuzzy HX ideal  $\eta_\alpha$  of a HX ring  $\mathfrak{R}_2$  then  $L(f^{-1}(\eta_\alpha); t)$  is a lower level HX ideal of an anti-fuzzy HX ideal  $f^{-1}(\eta_\alpha)$  of a HX ring  $\mathfrak{R}_1$ .

1) *Proof:* It is clear.

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