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Multi Attributes Decision-making: A Survey

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Abstract: In Decision-making domain, selection of best alternative is a complex problem based on some conflicting criteria. Multi Criteria Decision-Making(MCDM) helps to find the best alternatives among the set of alternatives and find the optimal solution. MCDM can be applied on a wide range of application domains. The objective of the survey is mainly focused on different types of MCDM approach, which are robust and also optimal, to solve different real life problems. Analytical Hierarchical Process(AHP), Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS), Simple Additive Weighting(SAW), Weighted Product Method(WPM), Elimination EtChoix Traduisant la REalite'(ELECTRE), Preference Ranking Organization method for Enrichment Evaluation (PROMETHEE) are different types of MCDM methods that we have discussed compactly in this paper. This survey article contains various types of MCDM method and their applications on various domains and discussion about the advantage and disadvantage of each method.

Keywords: Multi criteria decision-making(MCDM), fuzzy set theory, TOPSIS, FTOPSIS, AHP, FAHP, best choice, decision-making.

I. INTRODUCTION

In today's complex world decision making has become more and more tougher and can barely be solved by considering a single attribute or which can also be termed as criterion for a certain problem. So there comes the utility and the hallmark of MCDM methodologies in multi-objective problems where comparisons as well as ranking and selection can be done between the multiple attributes and multiple alternatives with the initial help of the decision makers. Decision-making can be treated as the cognitive process where choosing the best option among the alternatives is logical. It consists of a set of criteria and alternatives. Each criteria has a weighted value that can be obtained from decision-maker or expert group. After evaluating the weighted value of different criteria, the decision-making can be made. Depending on the type of problem, MCDM model contains various elements and the following picture depicts the most widely found elements-



Figure 1.1 MCDM Model's elements

There are several other classes of MCDM which can be termed as multi-attribute decision making (MADM) and multi-objective decision making (MODM). Here we will mainly be discussing about MADM. In multi-criteria problem, It is complex to determine the best optimal choice among the alternatives when several criteria are involved. A problem can be solved in different ways. One of the way is to select the best alternative from a group of alternatives (where "best" can be treated as "the most preferred alternative" of a decision maker) and another way is to select from a small set of good alternatives (Aruldoss, et al., 2013). Choosing the best



solution is definitely a complex task where the problem consists different criteria. The objective of this survey article is to facilitate the decision-makers when several choices are available to solve a problem. MCDM problem can be expressed as

 $C_1 \quad C_2 \quad \dots \quad C_n$

$$\mathbf{D} = \begin{bmatrix} A_1 \\ A_2 \\ \vdots \\ A_m \end{bmatrix} \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ x_{m1} & x_{m2} & \cdots & x_{mn} \end{bmatrix}$$
$$\mathbf{W} = \begin{bmatrix} W_1 & W_2 & \cdots & W_n \end{bmatrix}$$

D is a comparison matrix. Where A_1 , A_2 , ... Am are the set of possible alternatives from which decision maker have to select the best alternative. C_1 , C_2 , ..., C_n is the set of criteria. Based on these criteria performance of alternatives are measured. x_{ij} is represent the rating of alternatives which is obtained from the comparison between alternative A_i and each criteria C_j . Weight of each criteria C_j is expressed by W_j . Sometime such information, which is provided to decision-maker might be incomplete or imprecise. Human thought can create impression of vagueness. So in this situation problem solving is quite difficult. To overcome this problem Fuzzy set theory is introduced along with the MCDM, which is able to solve the uncertain situations. That is called Fuzzy Multi criteria Decision Making(FMCDM). In 1965, Zadeh (Zadeh 1965) proposed the fuzzy set theory to support uncertainty associated with vagueness or impression, and thus relevant to human cerebration. A fuzzy MCDM model consists of several criteria, alternatives and weight of each criteria, which can be represented in the term of linguistic values and expressed by fuzzy numbers with help of a committee of decision-makers. Most of FMCDM problems, final rating of alternatives are still in fuzzy numbers. De-fuzzification is required to convert from fuzzy value to crisp value for decision-making.

There are several type of MCDM and FMCDM methods available that are used to solve the decision-making problems and this survey article is mainly based on understanding the MCDM and how to solve this problem by providing the various MCDM methods. As the application area of MCDM method is very large, there are lots of work that have been proposed in MCDM domain and different type of MCDM methods are applied for selection of the optimal choice in different field. We have tried to sum up some of them. Each MCDM method has its own characteristics and uniqueness. Two or more methods can also be combined to produce a hybridization approach which can be used for solving complex decision-making problems. Some of the application areas of MCDM methods are location planning (Awasthi, et al., 2010), Supply chain management (Davari, et al., 2008; Zaeri et al., 2011), E commerce (Mishra, 2013), Software Industry (Hicdurmaz, 2012), Financial (Wua et al., 2011), Airlines (Lee et al., 2005) etc. There are some example of hybrid approach in MCDM, such as AHP and Fuzzy TOPSIS (Awasthi and Chauhan, 2011), Fuzzy AHP and DEA (Do and cheni, 2014) etc.

This article is organized as follows. We have discussed different types of MCDM methods and their applications on various research fields in section 2. Section 3 contains the findings and the conclusion is given in section 4.





Attributes can be classified in two different types, qualitative and quantitative. These above mentioned MCDM methods can be applied on both data types. The main goal of these methods is to find the best solution and selecting the best alternative. The hierarchical structure of various MCDM methods is showed in figure 2.1. These methods have been discussed in following section as follows-

A. Analytic Hierarchy Process (AHP)

AHP was originally developed by Prof. Thomas L.Saaty(1980). It is mainly developed for dealing with the complex decision making problem which have several types of conflicting criteria and alternatives. This method reduces the workload of decision-makers. The goal of AHP is to evaluate the final ranking, that are obtained from the pair-wise comparison of both alternatives and criteria. AHP is a simple method, because it doesn't require to construct a complex expert system with the knowledge of decision-maker enclosed in it. Computations made by the AHP are always supported by the decision-maker.

In AHP, every individual evaluation is very simple that can be easily deduced by a user, but when the number of criteria and alternatives increase, then it requires a large number of evaluations. In fact the number of pair-wise comparisons grows immensely with the number of criteria and options. For an example, suppose a problem consist of 10 criteria and 4 alternatives. So number of comparisons required to build a weight vector becomes $(4 \times 3)/2 = 6$ and number of pair-wise comparisons required to build

the score matrix becomes $4 \times (10 \times 9)/2 = 180$.

Steps of AHP

The major steps of AHP can be implemented as follows.

1) Step 1. Make pair-wise comparisons between the objects and construct the comparison matrix.

All the pair-wise comparisons are expressed by a Comparison matrix. Each object has a score, which is provided by the decisionmaker that can be calculated based on the comparison scale. Upper triangular matrix is filled up by actual values of judgements and lower triangular matrix is filled up by reciprocal values. Suppose A is a $m \times m$ comparison matrix, where m' is the number of criteria. Each entry a_{ij} of the matrix A represents the importance of the *i*th criterion corresponds to the *j*th criterion. Each pair of a_{ij} and a_{ji} are satisfying the following constraint,

$$a_{ii} \cdot a_{ii} = \mathbf{1} \tag{1}$$

2) Step 2. Construct the Normalized matrix and Weighted Normalized matrix.

After building the comparison matrix, it is required to be normalized by making the sum of each column equal to 1. Suppose A_1 is normalized matrix and each entry of that matrix, \bar{a}_{ij} is calculated as

$$\overline{a}_{ij} = \frac{a_{ij}}{\sum_{k=1}^{m} a_{kj}}$$
(2)

Finally, the Criteria Weight Vector w^{\dagger} is calculated by averaging the entries on each row of A_1 i.e.

$$w_i = \frac{\sum_{k=1}^{m} \bar{\sigma}_{ik}}{m} \tag{3}$$

3) Step 3. Computation of the Option Score matrix:

The Option Score matrix, **B** is a $m \times n$ real matrix, where m' is a set of criteria and n' is a set of alternatives. Each entry b_{ij} of **B** represents the score of *ith* option with respect to *j*th criteria. For each criteria a pair-wise comparison matrix B^i is built (i = 1, ..., m). B^i is a $n \times n$ real matrix, where *n* is the number of alternatives. The same procedure which is described above is applied to each B^i . After evaluating each B^i , finally score matrix *S* is obtained.

4) Step 4. Ranking the Options

After computing the weight vector W and score matrix S, global score of vector v is obtains by multiplying S and W.

$$\boldsymbol{v} = \boldsymbol{S}.\boldsymbol{w} \tag{4}$$

Each entry v_i of v is represented by the global score which is obtained after applying AHP. Finally the largest entry of v is considered the best option and the option ranking is completed by ordering the global scores in diminishing order.



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5) Step 5. Checking the consistency

During computing the pair-wise comparison, inconsistency may occur. So it is always important to check the consistency during the pair-wise comparison. The step of checking consistency as follows

- a) Calculate the Principle Eigen value(λ_{max}), which is obtained from the summation of product between each element of Eigen vector and the sum of column of the decision matrix.
- b) Calculate the Consistency Index(CI) as follows,

$$CI = \frac{\lambda_{max} - n}{n - 1} \tag{5}$$

where *n* is a number of objects.

c) Calculate the consistency ratio(CR), which is obtained from the following equation,

$$CR = \frac{CI}{RI}$$
(6)

where RI stands for Random Consistency Index.

If the value of Consistency Ratio is smaller or equal to 10%, the value of present inconsistency is acceptable. If the Consistency Ratio is greater than 10%, we need to revise the subjective judgments in the decision matrix in order to get a renewed value of inconsistency which will be put to test again.

B. Simple Additive Weighting(SAW)

Multi-attribute decision-making (MADM) is a one type of MCDM problem. MADM models are selector models and used for evaluating, ranking and selecting the most appropriate alternative among the set of alternatives (Memariani et al., 2009). It is a simple approach to find final score of alternatives. SAW(Fishburn,1967) consists of mainly two steps, first evaluation of the the final score of each alternative is done and then finally they are ranked. The method is describe is as follows

$$P_i = \sum_{j=1}^k w_j \cdot r_{ij} \; ; \; i = 1, 2, \dots, m$$
^[7]

where r_{ij} is the normalized value of decision matrix, that can be calculated as follows,

for profit attribute

$$r_{ij} = \frac{d_{ij}}{d_j^{Max}}; \quad d_j^{Max} = \max_{1 \le i \le m} d_{ij} \quad ; j = 1, 2, \dots, k$$
[8]

for cost attribute

$$r_{ij} = \frac{d_j^{Min}}{d_{ij}}; \quad d_j^{Min} = \min_{1 \le i \le m} d_{ij} \quad ; \ j = 1, 2, \dots, k$$
[9]

C. Weighted Product Method(WPM)

WPM is similar to the SAW method. The only difference between SAW and WPM is, instead of performing summation operation to calculate the rank in case of SAW, here in case of WPM multiplication(Miller and Starr, 1969) operation is performed to calculate the rank. In WPM, the procedure to calculate the normalized value of an alternative is also same as that of SAW method.

D. Technique for Order Preference by Similarity to Ideal Situation (TOPSIS)

It is an another brilliant methodology for solving MCDM problems, developed by Hwang and Yoon in 1981 with further developments by Yoon in 1987 and Hwang, Lai and Liu in 1993 respectively. The principle of the TOPSIS is select the alternative that is closest the positive ideal solution and farthest from the negative ideal solution. The positive ideal solution, A^+ is formed as a composite of the best performance values exhibited. The negative ideal, A^- , is the composite of the worst performance values. The process of the TOPSIS method is carried out as follows

1) Step1: Calculate the normalized decision matrix $\mathbf{R} = [r_{ij}]_{mxn}$ using the alternatives m and criteria n. The normalized value r_{ij} is calculated by the following equation



$$r_{ij} = \frac{x_{ij}}{\sqrt{\sum_{l=1}^{m} x_{ij}^2}}, i = 1, 2, \dots, m \text{ and } j = 1, 2, \dots, n.$$
^[10]

2) Step2: Calculate the weighted normalized decision matrix $V = [v_{ij}]$. The weighted normalized value v_{ij} is calculated as follows:

$$v_{ij} = (r_{ij})(w_j), i = 1, 2, \dots, m \text{ and } j = 1, 2, \dots, m$$
 [11]

where w_j is the weight of the *j*th attribute and $\sum_{j=1}^{n} w_j = 1$

3) Step 3: Determine the positive ideal solution (PIS) A^+ and negative ideal solution (NIS) A^-

$$A^{+} = \left\{ \binom{\max}{i} v_{ij} \middle| j \in J \right\}, \binom{\min}{i} v_{ij} \middle| j \in J' \right\}, i = 1, 2, ..., m = \{v_{1}^{+}, v_{2}^{+}, ..., v_{n}^{+}\}$$
[12]

$$A^{-} = \left\{ \binom{\min}{i} v_{ij} \middle| j \in J \right\}, \binom{\max}{i} v_{ij} \middle| j \in J' \right\}, i = 1, 2, ..., m = \{v_1, v_2, ..., v_3\}$$
[13]

Where J is a set of benefit attributes and J' is a set of cost attributes.

4) Step 4: Calculate the separation measures using the m-dimensional Euclidean distance. The separation measures of each alternative from the positive ideal solution are as follows

$$S_i^+ = \sqrt{\sum_{j=1}^n (v_{ij} - v_j^+)^2}, \quad i = 1, 2, ..., m$$
[14]

The separation measure of each alternative from the positive ideal solution are as follows

$$S_{i}^{-} = \sqrt{\sum_{j=1}^{n} (v_{ij} - v_{j}^{-})^{2}}, \quad i = 1, 2, \dots, m$$
[15]

5) Step 5: Calculate the relative closeness to the ideal solution. The relative closeness of the alternative A_i with respect to A^+ is defined as follows:

$$C_{i} = \frac{S_{i}^{-}}{S_{i}^{+} + S_{i}^{-}} \qquad i = 1, 2, ..., m; \mathbf{0} \le C_{i} \le \mathbf{1}$$
[16]

Step 6: Rank the alternatives in descending order with respect to

E. Elimination EtChoix Traduisant la REalite(ELECTRE)

ELECTRE was initiated by the Benayoun, Roy and Sussmann in 1966. Several versions of ELECTRE method was proposed like ELECTRE I, ELECTRE IS, ELECTRE II, ELECTRE III, ELECTRE IV and ELECTRE TRI. This method is efficient and effective for the MCDM. The basic principle of the ELECTRE method is based on the concept of outranking by using pair wise comparisons among alternatives under each criteria. There are two steps of ELECTRE method

1) Building the outranking relation

2) Exploitation of the outranking relation

ELECTRE method is used to discard some alternatives from the problem which are not acceptable. After discarding unacceptable alternatives another MCDA is used to select the best one. The main advantages of the ELECTRE method is that using this method before applying another MCDA with a restricted set of alternatives it saves much time. ELECTRE method varies from one to another version according to the type of the decision-making problem, degree of complexity, information quality. In ELECTRE method there are two sets of parameters- i) the importance co-efficient, ii) veto thresholds.

The simple ELECTRE provides the basic understanding concept and followed by the extensions of ELECTRE I, ELECTRE IS, ELECTRE II, ELECTRE IV, and ELECTRE TRI for the purpose of introducing veto thresholds concept and pseudo criteria which are the fundamental applications of ELECTRE method for MCDM.

F. Preference Ranking Organization Method for Enrichment Evaluation (PROMETHEE)

PROMETHEE was first introduced by professor Jean Pierre Brans in 1982. It is based on the principle of the out ranking method by using the mutual comparison of each alternative pair for each criteria. There are two steps included-Step 1. Assigning a preference function

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In this step, starting point is an evaluation matrix that represent the performance of each alternative under each criteria. By using the data of the evaluation matrix compare the alternatives pair-wise under each criteria. The results are represented by a function called the preference function. The preference function ranges from 0 to 1, where 0 means no difference and 1 means big difference between the pair.

Step 2. Estimating the outranking degree of the options

Calculate the global preference matrix by multiplying the preferences with the weights of the criteria and adding the single value. In global preference matrix the sum of the row represents the strength of an alternative (dominance) and the sum of the column represent how much an alternative is dominated by the other ones (sub dominance). Calculate the rank of the alternatives by subtracting the sub dominance value from the dominance value.

PROMETHEE method does not provide the weights of the criteria. The decision-makers provide the weights of the criteria and the preference function. Various PROMETHEE method is introduced like PROMETHEE I, PROMETHEE II, PROMETHEE GAIA.

S1.	MCDM Methods	Description	Advantages	Disadvantages
No				
1	Analytic	It provides pair wise	1.Stright forward, flexible and favourable.	1.To find the goal it needs large
	hierarchy	comparison of several	2. Always checks	number of pair wise comparisons.
	process (AHP)	alternatives for several	inconsistency.	2.Ranking evaluation is in
		criterion.	3.Problem is built into a	irregular manner.
			hierarchical structure that helps in finding the	3.Inconsistancy obligatory by 1 to 9
			goal.	scale.
			4.It gives a clear idea about the importance of	4.Subjective evaluation.
			each criteria.	5.Not efficient for large set of
			5.Perform pair-wise	criteria.
			comparison between the	
			attributes.	
2.	Technique for	Choose the alternative which	1. Decision making is simple using both cost	1.only independent criteria are
	Order of	is near to positive ideal	and profit criteria.	allowed.
	Preference by	solution and farthest from	2.Evaluate the rank of each alternatives.	2.Normalization is required for
	Similarity to Ideal	negative ideal solution	3.Easily programmable and simple	criteria evaluation.
	Solution(TOPSIS)		computation process	3.Criteria are
			4.Good computational	monotonically decreasing or
			efficiency.	Increasing
				in nature.
3.	Simple Additive	Provides pair wise	1.It is simple technique and most often used in	It is only efficient when
	Weighting(SAW)	comparison of several	MCMD.	criteria evaluation is
		alternatives for several	2.Consistency is measured.	maximized.
		criterion. and calculate		
		score for each		
		alternative. It based on the		
		weighted average.		
4.	Weighted Product	Perform comparison	1.Can remove any unit of measure.	No support for calculating weights.
	model(WPM)	between alternatives by the	2. It is used relative values.	
		weights and ratio of each		
		criterion.		
5.	Data Envelopment	DEA is used to find	1. Multiple inputs and outputs can be handled.	1.Measurement error can cause
	Analysis (DAE)	The efficiency of	2.Relation between inputs	significant problems
	(Afshari, 2010)	combination of multi inputs	and outputs are not	2. Absolute efficiency
		and multi outputs of the	necessary.	cannot be measured.
		problem	3. Comparisons are directly	3.Statistical tests are not applicable.
			against peers	4.Large problems can be demanding.
			4.Inputs and outputs can have very different	
			units	

Table 1. MCDM methods with its advantages and disadvantages



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6.	ELECTRE	It build the outranking relation	1.Outranking is used	1.Time consuming
		then explore the relation. This		2. It is a complex decision making
		method discard some		method and requires lot of primary
		alternative which is not		data.
		acceptable.		
.7.	PROMETHEE	Choose the best	1. Group level decision making is supported	1.Does not provides any
		alternative by using the		guideline of weighting
		mutual comparison of each		information of criteria but
		alternative pair for each		assume that the decision
		criteria. In this method		makers are able to provide
		preference		the weights of the criteria
		function is used which		properly.
		is provided by the		2. The way in which the
		decision maker for		preference ranking
		represent the		information is processed is
		Performance of each		complicated and hard to
		criteria of each		explain for the non
		alternative.		specialist.

G. Fuzzy Set theory in Multi Criteria Decision Making(MCDM) problem

In MCDM problem, constructing pair-wise comparison between the objects is dealing with the judgement of decision-maker. Sometimes information provided to the decision-maker is incomplete or imprecise and some problem dealing with the uncertainties and vagueness. Human thought or perception cannot be judged by the form of exact numerical value. To support this problem, fuzzy set theory was introduced into decision making domain where the decision maker can give their opinion in the form of linguistic term rather than exact numerical value.

2.7.1 Fuzzy set theory

The fuzzy sets are represented by linguistic terms that builds one or more linguistic variables, i.e. the linguistic variables have their possible states defined in a universe of discourse, represented by these linguistic terms (Sevkli et al., 2010).

A fuzzy set 'C 'can be represented as,

$C = \{(x,\mu_c(x)) \mid x \in X\}$

where $\mu_{c}(x)$ is called the Membership Function(MF) for the fuzzy set *C*. *X* is reoffered to as Universe of Discourse's is represented as linguistic values. Each element of *X* has membership grade between 0 and 1.

Fuzzy set and it's MF can be represented as different way, such as Triangular, Trapezoidal,

Sigmoidal, Gaussian etc.

Fuzzy set theory can be applied on different types MCDM methods for supporting the uncertainties and vagueness. It is compact with the various type of MCDM methods and it helps to increase the performance of this methods. Methods of FMCDM is Fuzzy Analytical Hierarchical Process(FAHP), Fuzzy Technique for Order of Preference by Similarity to Ideal Solution(FTOPSIS), Fuzzy Simple Additive Weighting(FSAW), Fuzzy Weighted Product Method(FWPM) etc.

H. Application of FMCDM method

In day-to-day life FMCDM methods are used in various field. It reduces the complexity of decision-making problem and helps to provide flexible decision-making. Some of FMCDM methods such as FAHP, FSAW, FWAP has capability of consistency checking. It removes the inconsistency while making the judgement by decision-maker. Some of FMCDM methods and its application are discussed in this article.

Some application area of FAHP are describe in Table2 i.e. A suitable bridge construction(Pan, 2008), Evaluation Of The Best Technical Institutions (Chatterjee and Bani Mukherjee, 2010), Contractor Selection (Haslinda et al., 2011), Evaluating Tourism Islands(Maizura et al., 2012).



Table 2. A	Application of	of Fuzzy AHP
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Author & year	Title of Article	Variable, Parameter		Methodology	Finding
		Criteria	Alternatives		(Best Alternatives)
Pan,	Fuzzy AHP approach for	1.Quality	3 alternatives	Fuzzy AHP	Advancing Shoring Method
2008	selecting the	2.Cost	method		is the most
	suitable bridge	3 .Safety	1.Full-span Precast		appropriate alternative
	Construction method	4.Duration	&		
	(Pan, 2008)	5.Shape	Launching		
		_	Method		
			2.Advance Shoring		
			Method		
			3.Incremental		
			Launching Method		
Chatterjee &.	Study of Fuzzy-AHP	1. Campus Infrastructure.	3 alternatives	Fuzzy AHP	Find the Best
Mukherjee,	Model To Search The	2,Faculty.	of college.		Technical Institutions.
2010	Criterion In The	3. Student			
	Evaluation Of The	4. Academic	1.BCREC		BCREC is the
	Best Technical	Ambience	2.BCET		select as best
	Institutions: A Case Study	6.Teaching Learning	3.DIATM		Technical Institution
	(Chatterjee and Mukherjee,	Process			
	2010)	7.Supplementary Process			
Alias, Maizura,	Contractor Selection using	1.financial:C1	4 alternatives	Fuzzy AHP	Select the best contractor
Noor, Selamat,	Fuzzy	2.performance:C2	of contractor	(FAHP)	A1>A3>A2>A4
Saman &	Comparison Judgement	3.Staff:C3 4.Equipment:C4			
Abdullah,	(Alias et al., 2011)		1.A1		Contractor A1 is the best
2011			2.A2		preferred
			3.A3		choices by decision maker
			4.A4		
Maizura Noor,	Fuzzy Analytic	1.Attraction:D1	3 Domain	Fuzzy AHP	Find the best
Amalina, Sabri,	Hierarchy Process	2.Environment:D2	experts	(FAHP)	criteria of social
Hitam, Ali	(FAHP) Approach	3. Accomodation:D3			attributes
& smail,	For Evaluating	4.Transportation:D4			performance for
2012	Tourism Islands in	5.Restaurant:D5			tourism island.
	Terengganu, Malaysia	6.Other Facilities:D6			Attraction is the
	(Noor et al., 2012)	7.Activity:D7			most important
		8.Entertainment:D8			criteria for
		9.Residents Attitudes:D9			selection island
		10.Souvenir:D10			Evaluation.

Sub criteria (Pan, 2008) Durability, Suitability Damage cost, Construction cost, Traffic conflict, Site condition, Constructability, Weather condition, Landscape, Geometry, Environmental preservation.

Sub criteria (Chatterjee and Mukherjee, 2010): Hostel, Transport/canteen/Internet, Power backup, Security, Teacher/Student ratio, Qualification/Experience of Faculty, Faculty retention, Admission, Academic Result, Placement, Classroom, Laboratory, Library, Syllabus coverage, Tutorial/ remedial Use of Advance Teaching Aid, Alumni, Co-curricular activity, Cultural activity, seminar/ Workshop. Sub criteria (Alias et al., 2011): Asset: C1-2, Liability: C1-2, Current: C2-1, Previous: C2-2, Experience:C31, Qualification: C3-2. Sub criteria (Noor et al., 2012): Unspoiled Nature, Unspoiled Forest, Colourful Fish, Beautiful Scenery, Traditional Fishermen Village, Marvellous Coral Reef, Nice Beaches, Waterfall. The first three important criteria are attraction, environment and accommodation. The first three important sub-dimensions are unspoiled nature , beautiful scenery and marvellous coral reef.

Some implementation areas of FTOPSIS method are describe in Table3. These fields consist Manufacturing System (Karsak, 2000), Threat Synthetic Evaluation in Multi-Target Tracing System (Wang, 2007), Supplier Selection (Sevkli, 2010; Yayla et al., 2012), Location planning (Awasthi et al., 2010; Boran, 2011; Ashrafzadeh, 2012), Stock Marketing (Madi and Tap, 2011) etc.



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Table 3. Application of Fuzzy TOPSIS

Author & year	Title of Article	Variable, Parameter		Methodology	Finding	
		Criteria	Alternatives	-	(Best Alternatives)	
Karsak.	Fuzzy MCDM	1.Capital and	8FSM alternatives	Fuzzy TOPSIS	FMS ₂ >FMS ₂ >FMS ₂	
2000	procedure for	operating Cost	1 FMS	(FTOPSIS)	$FMS_4 > FMS_7 > FMS_5 > FMS_1 >$	
2000	evaluating Flexible	2 Required floor	2 FMS ₂	(1101515)	FMS_	
	Manufacturing System(FMS)	space	3 FMS		111156	
	alternatives	3 Product flexibility	4 FMS		FMS ₂ is the best FSM	
	(Karsak 2000)	A volume	5 FMS-		alternatives	
	(Kursuk, 2000)	flexibility	6 FMS		anerhauves	
		5 Quality Improvement	7 FMS-			
		6 Work-In-Progress(WIP)	8 FMS			
Wang Huan Oin	Research on ETOPSIS	1 Change ratio of	5 alternatives of target	Fuzzy TOPSIS	To find which target	
Van & Bai	Model of Threat	target velocity: D.	1 Target1	(FTOPSIS)	Underwater Unmanned vehicle	
2007	Synthetic Evaluation	2 Change ration of	2 Target2	(1101515)	(IIIIV) should attack first	
2007	in Multi-target	target radial	3 Target3		(00 v) should attack hist.	
	Tracing System	velocity: D-	A TargetA		Target1 \ Target3 \	
	(Wang et al. 2007)	3 Change ration of target	5 Target5		Target5> Target4>	
	(Wang et al., 2007)	navigational angel: D ₂	5.1 argets		Target?	
		A Target orientation			Target2	
		mobile velocity:D.			UVV should attack Target1	
		5 Absolute value			first	
		of target velocity			liist	
		between estimation and				
		anticipation:D				
		6 Absolute value				
		of pavigational				
		on havigational				
		target and UUV: D.				
		7 Absolute value				
		of depth between target and				
		ULIV:D				
		8 Absolute value of distance				
		between target and LILIV:Do				
		0 Probability to be payal				
		vessels: Do				
Sevkli Zaim	An Application of	1 Delivery	3 Supplier	Fuzzy TOPSIS	Select the best provide forging	
Turkvilmaz &	Fuzzy TOPSIS	performance	alternatives	1 uzzy 101 515	parts for Propeller shaft	
Satur	Method for Supplier	2 Quality	andrhauves		for the light and	
2010	Selection	2. Quanty	1 Δ		heavy commercial	
2010	(Savkli at al. 2010)	3 Price/Cost	1.A 2 B		vahicles C A B	
	(Sevkii et al., 2010)	4 Finncial strength	2.D 3.C		C is selected as best supplier	
		5 Management and organizational	5.0		e is selected as best supplier	
		strength				
Awasthi	A multi-criteria	1 Accessibility(C1)	3 Location	Fuzzy TOPSIS	Selection of notential locations	
Chauhan	Decision-making	2 Security (C2)	alternatives	(FTOPSIS)	for urban	
& Goval	approach for location	3 Connectivity to multimodal	1 A1 is situated	(1101515)	distribution centres	
2010	planning for	transport (C3)	outside the city		distribution centres	
2010	urban distribution	4 Costs(C4)	close to a		A1>A3>A2	
	centres under	5 Environmental impact (C5)	highway while		111/110/112	
	uncertainty (Awasthi et al	6 Proximity to customers (C6)	locations		A1 is select as the	
	2010)	7.Proximity to suppliers (C7)	2.A2 is situated		best location for	
		8.Resource availability (C8)	inside the city		urban distribution	
		9.Conformance to	on the outskirts		centres	
		sustainable	inside the city			
		freight regulations (C9)	close to			
		10.Possibility of expansion (C10)	highways and to			
		11.Quality of service (C11)	the customer			
			locations			
			3. A3 is situated			



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			in the city centre far		
			from		
			highways		
			8		
Madi &	Eugan TODSIS	1 Markat	2 alternatives of	Eugan TODSIS	Salast the most proferable
Maul &	Fuzzy TOFSIS		3 alternatives of	Fuzzy TOFSIS	Select the most preferable
1 ap,2011	Method in the	Valuation(RM	Investment Boards on	(FTOPSIS)	investment boards
	Selection of	billion):C1	Bursa Malaysia		by incorporating
	Investment Boards by	2) Stock Trading	1.The Main		operational risks .
	Incorporating Operational	Volume (million	Board: A1		Main Board is the best suitable
	Ricks (Madi and Tan 2011)	units) :C2	2 The Second		choice
	Risks (Madi and Tup, 2011)	2) Steple Trading	Decide A2		MESDAQ is the second shellow
		3) Stock Trading	Board:A2		MESDAQ is the second choice
		Value(RM million)	3.The MESDAQ		and Second Board is the last
		:C3	Market:A3		choice.
Boran,	An integrated	1.Expansion possibility: C1	4 Alternatives of	Fuzzy preference	select The best
2011	Intuitionist fuzzy	2 Availability of	candidate	relation Fuzzy	location for building a new
2011	multi aritaria dagision	2. Trumability of	culture.	TODSIS/ETODSIS)	plant
				101313(1101313)	plant
	making method for	Material:C2 3.Community	1.A ₁		
	facility location	considerations:C3, 4.Distance to	$2.A_2$		A ₂ has been selected as best
	selection (Boran,	market:C4	3.A ₃		location .
	2011)	5. labour cost:C5	$4.A_{4}$		
Ashrafzadeh.	Application of fuzzy TOPSIS	1.Labor costs	5 Alternatives	Fuzzy TOPSIS	Selecting the best
2012	method for	2 Transportation costs	Locations		location for new
2012	the selection of	2. Handling ages	Locations		watch ou co
		5.Handling costs			warehouse
	Warehouse Location: A Case	4.Land cost	1. Isfahan: A_1		
	Study	5.Skilled labour	2. Arak:A ₂		
	(Ashraf zadeh, 2012)	6Availability of labour force.	3. Rasht:A ₃		$A_1 > A_2 A_{5>} A_4 > A_3$
		7.Land availability	4. Urmia:A ₄		
		8.Climate	5. Tabriz:A₅		$Isfahan(A_1)$ select as best
		9 Existence of			location for new warehouse
		madas of			location for new warehouse
		inodes of			
		transportation			
		10.Telecommunication systems			
		Quality and			
		reliability of modes			
		of transportation			
		12 Quality and			
		reliability of			
		utilities			
		13. Proximity to			
		customers			
		14. Proximity to			
		suppliers or			
		producers			
		15 Load times and			
		responsiveness			
Yayla	Fuzzy TOPSIS	1.Quality	3 Alternatives of	Fuzzy TOPSIS	Select the best supplier
, Yildiz & Özbek,	Method in Supplier	2.Delivery Time	supplier	(FTOPSIS)	
2012	Selection and	3.Cost			A1> A3 > A2
	Application in the Garment	4.Flexibility	1.Supplier1:A1		Supplier 1(A1) as best supplier
	Industry	5 Geographic Location	1 Supplier2: A2		II , ,
	(Varla 2012)	creeographic Docation	1 Supplier2: A 2		
	(1 ayia, 2012)		1.Supplier5:A5		

Various types of application field of Fuzzy SAW method are describe in table4. Some applications of this method are Personnel Selection problem (Afshari et al., 2010), Optimal Robots and Manipulators Selection (Bai and Wang, 2010), Project Manager Selection (Afshari et al., 2012) etc.



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Table4.	Applica	tion of	Fuzzv	SAW
i aore i.	rppnea	citon or	IGLEJ	01111

Author & year	Title of Article	Variable, Parameter		Methodology	Finding
		Criteria	Alternatives		(Best Alternatives)
Afshari,	Simple Additive	1. Ability to work	5 Personal	Simple Additive	Select the best
Mojahed &	Weighting approach to	in different	alternatives	Weighting (SAW)	personnel who
Yusuff, 2010	Personnel Selection problem	business units:C1			have passed
	(Afshari et al., 2010)	2. Past experience:	1.P1		examination in a
		C2	2. P2		Telecom company
		3. Team player:C3	3.P3		
		4. Fluency in a	4.P4		P3>P2>P5>P1>P4
		foreignlanguage:C4	5.P5		
		5. Strategic			P3 is select as best
		Thinking:C5			personnel
		6. Oral			
		communication skills:C6			
		7. Computer Skills			
		:C7			
Bai &	Applying Fuzzy	1. Axes:C1	20 .Alternatives of	Fuzzy simple	Select the optimal robot
Wang,2010	Multi-Criteria Decision	2. Payload (kg):C2	Robot	additive weighting	system from a large
	Making	3.Repeatability (mm):C3	A,B,C,D,E,F,G,H,I,J,	(FSAW)	group of
	for Optimal Robots	4.Accuracy (mm):C4	K,L,M,N,O,P,QR,S,T		robot candidates.
	and Manipulators	5:System cost			The top 10 optimal
	Selection (Bai and Wang,	(US\$):C5			robot is:
	2010)	6:Weight (kg):C6			D > C > P > J > B > E >
		7: Max Motion			O > N > I > Q.
		Speed (rad/s):C7			
		8.Mounting method			
		(average, good,			
		super):C8			
		9.Power dissipation			
		(kW):C9			
		10.H-Reach (mm):C10			
		11 V-Reach(mm):			
		(m3):C12 space			
Afshari,	Project Manager	1.Basic Requirements	3 Project	Fuzzy Simple	Selecting project manager
Yusuff &	Selection by Using	2.Project Management	manager	Additive	in
Derayatifar,	Fuzzy Simple	Skills	alternatives.(candidate	Weighting(FSAW	MAPNA Company
2012	Additive Weighting	3.Management Skills))	
	Method (Afshari,2012)	4.Interpersonal Skills			P2>P3>P1
			1.P1		
			2.P2		Candidate P2
			3.P3		Select as best
					project manager

Sub criteria (Afshari et al., 2012): Past experience, Education, .Communication skills, Computer skills, Time Management, Cost Management, .Resource Management, Quality Management, Planning, .Organizing, Controlling, Problem solving, Decision making, Team development.

I. Multi Criteria Group Decision making (MCGDM) and Multi Attribute Decision-Making(MADM)

In multi-criteria environment, sometime it is quiet difficult for single decision-maker to give his/her appraisal for different domain such as banking, stock market etc. One decision maker can't give sufficient information due to insufficient knowledge or experience.



This problem can be solved by the group decision-making (GDM), where a certain group of decision-makers are present and they can give their judgements on some problem. Sometime problem contains uncertainties and vagueness, therefore the judgements of decision makers go in the form of linguistic term rather than exact numerical values (Jiang and Liu, 2013). In multi-criteria environment the GDM is called Multi Criteria Group Decision-making (MCGDM).

MADM is a one type of MCDM problem. It is dealing with the selection problem, where the numbers of alternatives are chosen supported on a set of attributes. It is a discrete method and dealing with the finite number of alternatives. Table5 describe the some application area of MCGDM and MADM.

Author & year	Title of Article	Variable Parameter		Methodology	Finding
		Criteria	Alternatives		(Best Alternatives)
Saghafian	Multi-criteria Group	1 Publications and	Name of three eligible	Multi Criteria	Finding the best candidate
& Hejazi	Decision Making	researches (C1)	candidates	Group Decision	for
2005	Using A Modified	2 Teaching skills (C2)	culture	Making(MCGDM)	teaching in an University
2005	Euzzy TOPSIS	3 Practical experiences	1 4 1	Fuzzy TOPSIS	teaching in an emversity
	Procedure (Saghafian and Heiazi	in industries and	2 4 2	(FTOPSIS)	A2-A3-A1
		corporations (C3)	2.82	(1101515)	AZZAJZAI
	2003)	4 Past experiences in	5.45		A2 is the best candidate
		teaching $(C4)$			A2 is the best calibrate
		(5) Teaching			
		discipline (C5)			
Wong Chan &	Group Euzzy Multi gritoria	1 profitability of	5 mitable	Group Euggy Multi	Salaat a guitable material
Chap 2007	Decision	supplier (C1)	J Suitable Motorial Supplier	oritoria Desision	supplier for
Chen ,2007				Criteria Decision	supplier for
	Freehestign (Weng et al. 2007)	2. Relationship	1.A1	Making, Fuzzy	purchasing martial of new
	Evaluation (wang et al., 2007)	2 Taskaslasiasl	2.A2	I UPSIS	product.
		5. Technological	5.A5	(FTOPSIS)	AD: AD: A1: A4: A5
		capability (C3)	4.A4		A2>A3>A1>A4>A5
		4. Conformance	5.A5		A2 is the best alternatives
		quanty (C4)			
		5. Conflict			
W		1 Debter tetal	2	European and the state of a	
Wang &	A fuzzy multi-criteria group	1.Debt to total	3 companies	Fuzzy multi-criteria	$A_2 > A_1 > A_3$
SKao, 2009			1.A ₁	group decision	
	making model for the	2. Working capital to total	2.A ₂	making	A_2 has best
	financial performance evaluation		3.A ₃	(FMCGDM),	beneficial performance.
		3.Quick ratio		nizzy TOPSIS	
	airlines (wang and Skao, 2009)	4.Cash now ratio		(FTOPSIS)	
		5. working capital			
		to current assets			
		fatio.6.Accounts payable			
		7. accounts			
		receivable			
		l urnover			
		8. Fixed assets			
		turnover			
		9. Net income(loss) turnover			
		10.Gross profit			
		ratio.			
		11.Operation profit ratio			
		12.Net income			
I' 0 I' 2012		ratio		MARGALIC	
Jiang & Liu,2013	A Multi-Criteria	1.Financial measurements: y_1	Four commercial banks	Multi-Criteria Group	Select the best commercial
	Group Decision-	2.Customers: y_2	1	Decision	bank
	Making Model for Performance	3.1internal business	1.X ₁	Making (MCGDM),	
	Evaluation of	process:y ₃	1.x ₂	Balanced	$x_4 > x_{1>} x >_2 x_3$
	Commercial Banks	4. Learning and	1.X ₃	scorecard	
	(Jiang and Liu, 2013)	growth:y ₄	1.X ₄	(BSC),linguistic 2-	x_4 is selected as best
1		1	1	tuples	commercial bank.

Table5. Application of Multi Criteria Group Decision-making (MCGDM)



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Wimatsari,	Multi-Attribute Decision Making	1. GPA (Grade	8 Students	Fuzzy Multi	Student selection
Putra,	Scholarship Selection	Point Average):C1	where Achievement	Attribute Decision	for achievement
Buana,2013	Using A Modified	2. Quotient of	Scholarship is 5	Making (FMADM),	scholarship and
	Fuzzy TOPSIS	income parents by	students and	Fuzzy	Underprivileged scholarship.
	(Wmatsari, 2013)	the number of	Underprivileged	TOPSIS	
		dependents:C2	scholarship is 3 students	(FTOPSIS)	The five
		3. The Usage of	1.001		candidates who
		Electrical Power:C4	2.002		have five highest
		4. Student	3.003		score was selected as the
		Activities:C5	4.004		recipient of a scholarship
			5.005		achievement and
			6.006		rank is 006>005>
			7.007		001>008>
			8.008		003
					3 Candidates who achieve
					Underprivileged
					scholarship and
					rank is
					004>002>007

Two or more method can be combined in MCDM domain for evaluating the best result. So hybridization of methods is possible for solving a decision-making problem. Some application area of hybridization method is discussed in table6. Sustainable city logistics planning (Awasthi ang Chauhan, 2011) problem is solved by the combined method of AHP and fuzzy TOPSIS, is a beautiful example of hybridization between MCDM methods.

Author & year	Title of Article	Variable, Parameter		Methodology	Finding
		Criteria	Alternatives		(Best Alternatives)
Chang	Fuzzy TOPSIS	1.Cost:x1	16 configuration	Fuzzy	Select a the best configuration
&	Decision Method for	2.Speed:X2	alternatives	TOPSIS	alternative of CNC lathe
.Tseng,	Configuration Management	3.Strength:x3	A1 to A16	(FTOPSIS),	machine.
2008	(Chang and Tseng,	4.Lubrication system:x4		Fuzzy quality	A4 is chosen as best
	2008)	5.Coolant pump		function	alternative
		system:x5		deployment	
				(QFD)	
Zhuofu, Wei-	Improved multi-	1.Project	Comprehensive	Entropy	Choose the proper project
min & Jun-zu;	attribute fuzzy	Characteristics	evaluation value of	method,	delivery
Bin,2008	comprehensive	2.Owners' Needs	the	Fuzzy compr-	system for a large-
	evaluation in project	& Preferences	alternatives	ehension	scale water
	delivery decision-	3. Project Circumstances.	1.Traditional	evaluation	supply project
	making		method (DBB)		
	(Zhuofu et al., 2008)		2. Design-build		CM at-Risk>DB>
			method (DB)		DBB
			3. construction		CM at-Risk is
			management at		chosen as best project
			risk method		delivery
			(CM at-Risk)		method.
Apak &	Evaluating an	1. M1 decision	3 Intelligent	Fuzzy AHP,	Evaluating a
Vayvay,	intelligent business	Management System	Business System	Fuzzy	proper IBS of IT
2009	system with a fuzzy	2. M2 Intelligent	(IBS) alternatives	TOPSIS	department
	multi-criteria approach (Apak	text mining	1.A1		
	and Vayvay, 2009)	3.M3 risk	2. A2		A3>A1>A2
		management	3.A3		A2 select as best IBS.



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Santos,	Fuzzy Systems for Multi	1.Attributes Revenue:C1	10 customers	Fuzzy Rule-	CRM (Customer
2010	criteria Decision Making	2. Percentage of bills	Alternatives An	Based	Relationship Management)
	(Santos,	late more than 30	n=1 To 10.	Systems	systems in a
	2010)	days:C2		Fuzzy	transport company.
		3.Regularity of payment		TOPSIS	
		bills:C3		(FTOPSIS),F	A2 is select as best customer.
		4.Total weight carried:C4		uzzy	
		5.Amount of invoice by		Flexible	
		customer:C5		TOPSIS	
		6.Amount of Transport		(FFTOPSIS)	
		invoice:C6			
Awasthi	A hybrid approach	1.Technical	4 sustainable	AHP & Fuzzy	Select the best
& Chauhan,	integrating Affinity	2.Social	city logistics	TOPSIS	sustainable city logistics
2011	Diagram, AHP and	3.Economic	initiative		initiative
	fuzzy TOPSIS for sustainable	4.Enviornment	1.Vehicle sizing		
	city		restrictions:A1		A4 > A2 > A1 > A3.
	logistics planning		2.Congestion		
	(Awasthi and		charging schemes:A2		A4 (Timing
	Chauhan, 2011)		3.Urban distribution		Restrictions) is select as the
			centre:A3		best sustainable city logistics
			4.Access Timing		initiative.
			Restrictions:A4		
Nagar,	Development of	1. Purchasing	5 Maintenance	Multiple-	selecting the most
2011	Fuzzy Multi Criteria Decision	cost:C1	alternatives	Criteria	appropriate maintenance
	Making	2. Establishment		Decision	approach
	Method for	cost (machine -floor	1. Predictive	Making(MCD	for Air caster.
	Selection of Optimum	requirements, etc.):C2	maintenance:.A1	M),Fuzzy sets	
	Maintenance Alternative	3.Operating cost:C3	2. Breakdown		A1 >A2>A4 >A3 >A5.
	(Nagar, 2011)	4.Reliability:C4	maintenance:A2		
		5.Operational	3. Routine		A1, is select as the best
		flexibility:C5	maintenance:A3		maintenance alternative for
		6.Productivity:C6	4.Preventive		Air caster.
		7. Risks	Maintenance:A4		
		(safety):C7	5.Corrective		
		8. Supplier's	maintenance:A5		
		environmental			
		behaviors:C8			
Hicdurmaz,	A Fuzzy Multi		4 type of	Fuzzy AHP,	selection of
2012	Criteria Decision	1.People	Software Life	Fuzzy	appropriate
	Making Approach to	2.Process	Cycle Model (SLCM)	TOPSIS	software life cycle model
	Software Life Cycle Model	3.Tecnical			(SLCM) of software
	Selection		1. Waterfall		development process
	(Hicdurmaz, 2012)		Model		
			2. V Model		Evolutionary
			3. Spiral Model		Prototyping > V
			4. Evolutionary		Model > Spiral > Waterfall
			Prototyping		
					Evolutionary
					Proto-Typing
					model select as
					best software life
					cycle model of
					software
					development
					process



Evaluation attributes (Zhuofu et al., 2008): Project scale(A1), Project complexity(A2), Depth of the design document(A3), Degree of involvement after contract award(A4), Cost control(A5), Schedule control(A6), Risk allocation(A7), Circumstance of local construction market(A8), Law and local regulation(A9).

Sub criteria (Apak and Vayvay, 2009): Optimization model(C1), Time series analysis(C2), Structured text analysis(C3), Numeric data analysis(C4,), Forecasting model(C5), Clustering(C6), Classification(C7), Profiling(C8), Hyper linking(C9), System(C10), Prediction(C11).

Sub criteria (Awasthi and Chauhan, 2011): Logistical efficiency (C1), Mobility(C2), Accessibility(C3), Service quality(C4), Loading factor(C5), Customer coverage(C6), Freeing of public space(C7), Energy conservation(C8), Trip effectiveness(C9), Revenues(C10), Volume of freight handled(C11), Accidents(C12), Costs:(C13), Congestion (C14), Air pollution(C15), Noise(C16) Sub criteria (Hicdurmaz, 2012): Ease of management, User involvement and Feedback, Cost, Complexity, Critically, Flexibility, Reusability, Doc. and software quality, Testing and integration, .Focus on design and architecture, Formal reviews, Requirement stability.

III. FINDINGS

MCDM has certainly become one of the most supreme techniques in decision-making field. Methods of MCDM are designed perfectly to choose the best option for a complex decision-making problem based on criteria evaluation and ranking the criteria. Though it is very much difficult to sum up all the different techniques in MCDM world but our main motto behind this paper is to give an initial outline to a novice researcher in this area and to show the various application domains of MCDM methods such as FAHP, FTOPSIS, FSAW which we have discussed in this survey article.

Following section of this paper contains the results of this survey.

From our survey we have found wide variations of application domain on which Fuzzy MCDM techniques were applied such as Manufacturing System, Supply chain management, Location planning, Stock Marketing, Construction, Evaluation Of The Best Technical Institutions, Contractor Selection, Evaluating Tourism Islands, Robotics, E commerce, Software Industries, Project Manager Selection, Quality Management etc. We are putting a table too for better understanding,

Sl no	Commercial	Industrial	Environmental estimation	Performance rating
1	To find the most preferable	To select the optimal method for	Find the best criteria of social	To search criteria in the evolution
	investment boards by	bridge construction.	attributes	of the best
	incorporating operational risks .		performance for tourism island.	technical institution.
2	To find the optimal robot system	Contractor selection, in selecting the	To find the best potential	To find which target Underwater
	from a large group of robot	best contractor who are able to	locations for urban distribution	Unmanned vehicle (UUV) should
	candidates.	provide best service.	centres.	attack first.
3	To evaluate financial	To find the best Flexible	To find the best location for	To find the best personnel who
	performance of different airlines	Manufacturing System	building a new plant	is suitable
	companies.	(FMS) in industries.		in a Telecom company.
4	To evaluate banking performance	To find the best supplier to provide	To find the best suitable location	To Find the best candidate for
	of	forging parts for Propeller shaft for	for building a new warehouse.	teaching in an
	commercial banks.	the light and heavy		University.
		commercial vehicles		
5	To select the best configuration	Find the best supplier in garment	To find the best	Student selection for achievement
	alternative of a lathe machine.	industry.	sustainable city logistics	scholarship and underprivileged
			initiative.	scholarship.
6	To evaluating an Intelligent	To select the best project manager in		To select the best customer in a
	Business System of IT	a certain company.		transport company.
	department.			

Table No. 7 Domain-wise Applications of MCDM methods



7		To Select the suitable material		
		supplier for purchasing martial of		
		new product.		
8		To find proper project delivery		
		system for a large-scale water		
		supply project.		
9		To find the most		
		appropriate maintenance approach		
		for air caster.		
10		To select the appropriate Software		
		Life Cycle Model (SLCM) of		
		software development process.		
contr	6	10	5	6

This table describes the application fields of the FMCDM techniques and also gives us the clear essence about generalized the domains in which these techniques can be applied. We have divided the generalized domains into 4 parts. Under these domains we have also listed respective domain works. From the survey we have listed 6, 10 5 and 6 applications under commercial, industrial, environmental estimation and performance rating respectively. Though it will be wrong to say that FMCDM methods are mostly used in industrial sectors but from our short survey we have found more number of applications in industrial area than any other areas. From this above table we can easily conclude that the application areas of these methods are numerous. In most of these decision making problems, a fuzzy approach to MCDM is applied according to the complexity and the difficulty of the problem and due to its capability of handling uncertain situations and as it proves to be the best determination for the decision makers. Table No. 8 FMCDM methods and their respective number of occurrence

Sl. no	MCDM methods	allowance
1	FAHP	4
2	FTOPSIS	8
3	FSAW	3
4	Combinational	7
5	FMCGDM	5

Table 8 gives the most widely used fuzzy MCDM techniques in MCDM problems and they are also ranked according to their usage and applicability in various domains. The allowance number shows their number of occurrences in different problems in this survey. For better understanding we have also plotted a graph indicating respective usages of different Fuzzy MCDM techniques as follows



Figure 3.1 FMCDM methods and its allowance for different applications

Most widely used Fuzzy MCDM techniques only are taken into consideration. This is basically the graphical representation of the table no 8. The Fuzzy MCDM techniques include Fuzzy AHP(FAHP), Fuzzy TOPSIS(FTOPSIS), Fuzzy SAW(FSAW), Fuzzy Combinational techniques and Fuzzy MCGDM(FMCGDM) techniques.



From the above figure we can say that FTOPSIS and Fuzzy combinational techniques come among the most widely used FMCDM techniques in order to be used in some domain though it will be unfair to judge the usefulness of these techniques only in a small scale as we have done that based on our survey. In between these techniques there also many techniques which include some alterations in classical techniques and those alterations are new variations of those techniques which are actually altered for gaining better result and according to the problem analysis. We are enlisting also some of the papers where these modified approaches have been shown.

S. Saghafian and S.R Hejazi (Saghafian and Hejazi,2005) proposed a modified Fuzzy TOPSIS procedure in which they have implemented a new approach for measuring distance using the fuzzy comparison function instead of simple vertex method. W. Zhuo, etal. (Zhuo-fu etal., 2008) have used a new weight evaluation technique "entropy weight method" which modifies the experts subjective weight and give the comprehensive weight, instead of using the attribute weight setting method. Some of the papers listed in this article also show the combinational methods for better result. A. Awasthi and S.S. Chauhan (Awasthi and Chauhan, (2011)) are previously used the simple Fuzzy TOPSIS method for location planning but for better evaluation later they have proposed a combinational approach towards city logistic planning.

Many other MCDM methods are also there such as Fuzzy BCC, FSROWA, Fuzzy SBM, COPRAS-G, VIKOR, Fuzzy DEMATEL, Grey theory, Data envelopment analysis (DAE), Aggregated Indices Randomization method (AIRM), Goal Programming etc. But as the world of MCDM is too vast to be restricted to a survey, we have only taken the methods under MADM which are vastly used methods.

IV. CONCLUSIONS

This paper is actually meant for outlining the research opportunities in MCDM and also their respective features that can be taken for solving domain problem when multiple choices are available for decision making. Paper mainly aims at finding the importance of MCDM methods in various field. We also conclude that FMCDM is the best to be applied in various domains for selecting the best alternatives among set of alternatives based on multiple criteria where vagueness and uncertainty involved and as they can be applied can be applied on both quantitative and qualitative data items. Various applications include domain such as Location planning, IT industry, Banking, Marketing, Supply chain management and other multi criteria domain etc. This survey is not biased towards any certain problem domain and mainly lists various fields of action so that a novice in this field can have the basic application ideas. Methods of FMCDM has been selected based on the problem type and its domain

In recent years, combining different methods i.e. building hybrid methods has become very common due to advancing technologies and increasing complexity. The combination of multiple methods handles and fulfils the deficiencies that can be seen in certain methods. These hybrid methods can be extremely successful in their applications, but only if their strengths and weaknesses are properly assessed. That is why we have also shown respective advantages and disadvantages of certain MCDM methods in our paper.

Lastly we conclude that MCDM techniques mixed with fuzzy are able to handle some the most complex decision making problems and the research area as well as application area of MCDM techniques is huge. So the future scope in this field is immense.

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