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# **More Results on k-Super Mean Labeling**

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Abstract: Let G be a (p, q) graph and  $f: V(G) \rightarrow \{k, k + 1, k + 2, ..., p + q + k - 1\}$  be an injection. For each edge e = uv, let  $f^*(e) = \frac{f(u) + f(v)}{2}$  if f(u) + f(v) is even and  $f^*(e) = \frac{f(u) + f(v) + 1}{2}$  if f(u) + f(v) is odd, then f is called k - super mean labeling if  $f(V) \cup \{f^*(e): e \in E(G)\} = \{k, k + 1, k + 2, ..., p + q + k - 1\}$ . A graph that admits a k - Super mean labeling is called k-Super mean graph. In this paper we investigate k - super mean labeling of  $n(S(S_3)), (P_n; S_2), [P_n; Q_3], T_n \cup T(L_m), D(F_n)$ . Keywords: k-Super mean labeling, k-Super mean graph,  $n(S(S_3)), (P_n; S_2), [P_n; Q_3], T_n \cup T(L_m), D(F_n)$ . AMS Subject Classification--- 05C78

#### I. INTRODUCTION

All graphs in this thesis are finite, simple and undirected. Terms not defined here are used in the sense of Harary [7]. The symbols V(G) and E(G) will denote the vertex set and edge set of a graph G. Graph labeling was first introduced in the late 1960's. Many studies in graph labeling refer to **Rosa's** research in 1967. Labeled graphs serve as useful models for a broad range of applications such as X-ray, crystallography, radar, coding theory, astronomy, circuit design and communication network addressing. Particularly interesting applications of graph theory can be found in [1-4]. The concept of mean labeling was introduced and studied by S. Somasundaram and R. Ponraj [12]. The concept of super mean labeling was introduced and

studied by D. Ramya et al [11]. Further some results on super mean graphs are discussed in [8,9,10,13,15]. B. Gayathri and M. Tamilselvi [5-6, 14] extended super mean labeling to k-super mean labeling. In this paper we investigate k-supermean labeling of  $n(S(S_3)), (P_n; S_2), [P_n; Q_3], T_n \cup T(L_m), D(F_n)$ . Here k denoted as any positive integer greater than or equal to 1.

#### **II. MAIN RESULTS**

#### A. Definition 2.1

Let G be a (p, q) graph and f: V(G)  $\rightarrow$  {1,2,3,..., p + q} be an injection. For each edge e = uv, let  $f^*(e) = \frac{f(u)+f(v)}{2}$  if f(u) + f(v) is even and  $f^*(e) = \frac{f(u)+f(v)+1}{2}$  if f(u) + f(v) is odd, then f is called super mean labeling if f(V)  $\cup$  {f\*(e): e  $\in$  E(G)} = {1,2,3,..., p + q}. A graph that admits a super mean labeling is called super mean graph.

#### B. Definition 2.2

Let G be a (p, q) graph and f: V(G)  $\rightarrow$  {k, k + 1, k + 2, ..., p + q + k - 1} be an injection. For each edge e = uv, let  $f^*(e) = \frac{f(u)+f(v)}{2}$  if f(u) + f(v) is even and  $f^*(e) = \frac{f(u)+f(v)+1}{2}$  if f(u) + f(v)) is odd, then f is called **k** - **super mean labeling** if f(V)  $\cup$  {f\*(e): e  $\in E(G)$ } = {k, k + 1, k + 2, ..., p + q + k - 1}. A graph that admits a k - Super mean labeling is called **k-Super mean graph.** 

#### C. Definition 2.3

A subdivision of a graph G is a graph resulting from the subdivision of each edge by a new vertex.

#### D. Definition 2.4

A triangular snake  $(T_n)$  is obtained from a path by identifying each edge of the path with an edge of the cycle  $C_3$ .

#### E. Definition 2.5

A double triangular snake  $D(T_n)$  consists of two triangular snake that have a common path. That is, a double triangular snake is obtained from a path  $v_1$ ,  $v_2$ , ...,  $v_n$  by joining  $v_i$  and  $v_{i+1}$  to a new vertices  $w_i$  for i = 1, 2, ..., n-1 and to a new vertices  $u_i$  for i = 1, 2, ..., n-1.



# F. Definition 2.6

A star graph  $S_n$  is the complete bipartite graph  $K_{1,n}$ .

# G. Definition 2.7

The ladder graph  $L_n$  is obtained from the Cartesian product of two path graphs.

# H. Definition 2.8

For any graph G, the graph mG denotes the disjoint union of m copies of G.

# I. Theorem 2.9

The graph  $n(S(S_3))$  is a k-Super mean graph for all  $n \ge 1$ .

Let  $V(n(S(S_3))) = \{u_i, v_i, w_i, s_i, v'_i, w'_i, s'_i; 1 \le i \le n\}$  and  $E(n(S(S_3))) = \{e_i = (u_i, v'_i), e'_i = (v_i, v'_i), e''_i = (w_i, w'_i); 1 \le i \le n\} \cup \{e''_i = (u_i, s'_i), e^{iv}_i = (s_i, s'_i), e^{v}_i = (u_i, w'_i); 1 \le i \le n\}$  be the vertices and edges of  $n(S(S_3))$  respectively.

Define  $f: V(n(S(S_3))) \to \{k, k + 1, k + 2, ..., k + 13n - 1\}$  by  $f(u_i) = k + 13i - 9; \ 1 \le i \le n$   $f(s_i) = k + 13i - 13; \ 1 \le i \le n$   $f(s'_i) = k + 13i - 1; \ 1 \le i \le n$   $f(v'_i) = k + 13i - 7; \ 1 \le i \le n$   $f(v_i) = k + 13i - 4; \ 1 \le i \le n$   $f(w_i) = k + 13i - 3; \ 1 \le i \le n$ Now the induced edge labels are  $f^*(e_i) = k + 13i - 5; \ 1 \le i \le n$  $f^*(e'_i) = k + 13i - 5; \ 1 \le i \le n$ 

 $f^*(e_i^{''}) = k + 13i - 10; \ 1 \le i \le n$   $f^*(e_i^{iv}) = k + 13i - 12; \ 1 \le i \le n$   $f^*(e_i^{v}) = k + 13i - 6; \ 1 \le i \le n$ Here p = 7n, q = 6n. Clearly,  $f(V) \cup \{f^*(e): e \in E(n(S(S_3)))\} = \{k, k + 1, ..., k + 13n - 1\}.$  So f is a k – Super mean labeling. Hence  $n(S(S_3))$  is a k – Super mean graph.

# J. Example 2.10

10 – Super mean labeling of  $6(S(S_3))$  is given in figure 1:

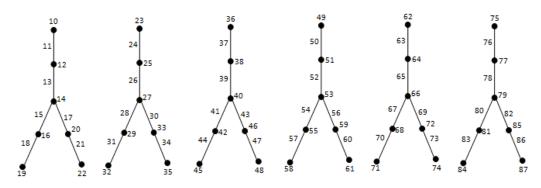


Figure 1: 10 – Super mean labeling of  $6(S(S_3))$ 



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# K. Definition 2.11

Let G be a graph with fixed vertex v and let (P<sub>m</sub>;G) be the graph obtained from m copies of G and the path  $P_m: u_1, u_2, ..., u_m$  by joining  $u_i$  with the vertex v of the i<sup>th</sup> copy of G by means of an edge, for  $1 \le i \le m$ .

# L. Theorem 2.1

The graph  $(P_n; S_2)$  is a k-Super mean graph for all  $n \ge 1$ .

#### Proof:

Let  $V((P_n; S_2)) = \{u_i, v_i, w_i, w_i'; 1 \le i \le n\}$  and  $E((P_n; S_2)) = \{e_i = (u_i, u_{i+1}), 1 \le i \le n-1\} \cup \{e_i' = (u_i, v_i), e_i'' = (w_i, v_i), e_i'' = (v_i, w_i'); 1 \le i \le n\}$  be the vertices and edges of  $(P_n; S_2)$  respectively. Define  $f: V((P_n; S_2)) \to \{k, k+1, k+2, ..., k+8n-1\}$  by  $f(u_i) = \begin{cases} k+8i-8; & 1 \le i \le n; if n is odd \\ k+8i-2; & 1 \le i \le n; if n is even \end{cases}$   $f(v_i) = \begin{cases} k+8i-4; & 1 \le i \le n; if n is odd \\ k+8i-4; & 1 \le i \le n; if n is odd \\ k+8i-4; & 1 \le i \le n; if n is even \end{cases}$   $f(w_i) = \begin{cases} k+8i-4; & 1 \le i \le n; if n is odd \\ k+8i-10; & 1 \le i \le n; if n is even \end{cases}$ Now the induced edge labels are  $f^*(e_i) = k+8i-7; & 1 \le i \le n; if n is odd \\ k+8i-3; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i') = \begin{cases} k+8i-7; & 1 \le i \le n; if n is odd \\ k+8i-3; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i') = \begin{cases} k+8i-7; & 1 \le i \le n; if n is odd \\ k+8i-3; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i') = \begin{cases} k+8i-7; & 1 \le i \le n; if n is odd \\ k+8i-3; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i'') = \begin{cases} k+8i-5; & 1 \le i \le n; if n is odd \\ k+8i-5; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i'') = \begin{cases} k+8i-5; & 1 \le i \le n; if n is odd \\ k+8i-5; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i'') = \{k+8i-5; & 1 \le i \le n; if n is odd \\ k+8i-5; & 1 \le i \le n; if n is odd \end{cases}$   $f^*(e_i'') = \{k+8i-3; & 1 \le i \le n; if n is odd \\ k+8i-5; & 1 \le i \le n; if n is odd \end{cases}$ Here p = 4n, q = 4n - 1. Clearly,  $f(V) \cup \{f^*(e): e \in E((P_n; S_2))\} = \{k, k+1, ..., k+8n-1\}$ . So f is a k – Super mean labeling.

#### M. Example 2.13

40 – Super mean labeling of  $(P_4; S_2)$  is given in figure 2:

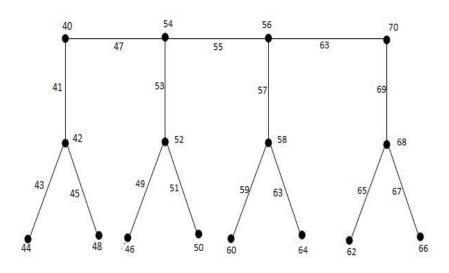


Figure 2: 40 – Super mean labeling of  $(P_4; S_2)$ 



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# N. Definition 2.14

Let G be a graph with fixed vertex v, and let  $[P_m;G]$  be the graph obtained from m copies of G by joining v<sub>i</sub> and v<sub>i+1</sub> by means of an edge for some j and  $1 \le i \le m - 1$ .

O. Theorem 2.15 The graph  $[P_n; Q_3]$  is a k-Super mean graph for all  $n \ge 1$ . Proof: Let  $V([P_n; Q_3]) = \{u_i, v_i, w_i, x_i, u'_i, v'_i, w'_i, x'_i; 1 \le i \le n\}$  and  $E([P_n; Q_3]) = \{e_i = (u_i, u_{i+1}), 1 \le i \le n-1\} \cup \{e'_i = (u_i, v_i), e''_i =$  $(w_{i}, v_{i}), e_{i}^{\prime\prime\prime} = (w_{i}, x_{i}), : 1 \le i \le n \} \cup \{e_{i}^{iv} = (u_{i}, x_{i}), e_{i}^{v} = (u_{i}, u_{i}^{\prime}), e_{i}^{vi} = (v_{i}, v_{i}^{\prime}): 1 \le i \le n \} \cup \{e_{i}^{vii} = (w_{i}, w_{i}^{\prime}), e_{i}^{viii} = (w_{i}, w_{i}^{\prime}), e_{i}^{vii} = (w_{i}, w_{i}^{\prime}), e$  $(x_i, x'_i), e_i^{ix} = (u'_i, x'_i); 1 \le i \le n \} \cup \{e_i^x = (u'_i, v'_i), e_i^{xi} = (v'_i, w'_i), e_i^{xii} = (w'_i, x'_i); 1 \le i \le n \}$ be the vertices and edges of  $[P_n; Q_3]$  respectively. Define  $f: V([P_n; Q_3]) \to \{k, k+1, k+2, ..., k+21n\}$   $f(u_i) = \begin{cases} k+21i-21; & 1 \le i \le n; if n is odd \\ k+21i-2; & 1 \le i \le n; if n is oven \end{cases}$   $f(u'_i) = \begin{cases} k+21i-11; & 1 \le i \le n; if n is oven \\ k+21i-13; & 1 \le i \le n; if n is oven \end{cases}$   $f(v'_i) = \begin{cases} k+21i-17; & 1 \le i \le n; if n is oven \\ k+21i-6; & 1 \le i \le n; if n is oven \end{cases}$   $f(w'_i) = \begin{cases} k+21i-13; & 1 \le i \le n; if n is oven \\ k+21i-13; & 1 \le i \le n; if n is oven \end{cases}$   $f(w'_i) = \begin{cases} k+21i-13; & 1 \le i \le n; if n is oven \\ k+21i-11; & 1 \le i \le n; if n is oven \end{cases}$   $f(x'_i) = \begin{cases} k+21i-6; & 1 \le i \le n; if n is oven \\ k+21i-17; & 1 \le i \le n; if n is oven \end{cases}$   $f(v_i) = \begin{cases} k+21i-19; & 1 \le i \le n; if n is oven \\ k+21i-4; & 1 \le i \le n; if n is oven \end{cases}$   $f(w_i) = \begin{cases} k+21i-2; & 1 \le i \le n; if n is oven \\ k+21i-21; & 1 \le i \le n; if n is oven \end{cases}$   $f(w_i) = \begin{cases} k+21i-2; & 1 \le i \le n; if n is oven \\ k+21i-21; & 1 \le i \le n; if n is oven \end{cases}$   $f(x_i) = \begin{cases} k+21i-4; & 1 \le i \le n; if n is oven \\ k+21i-21; & 1 \le i \le n; if n is oven \end{cases}$   $f(x_i) = \begin{cases} k+21i-4; & 1 \le i \le n; if n is oven \\ k+21i-21; & 1 \le i \le n; if n is oven \end{cases}$ Now the induced edge labels are Define  $f: V([P_n; Q_3]) \to \{k, k + 1, k + 2, ..., k + 21n - 2\}$  by Now the induced edge labels are  $f^{*}(e_{i}) = k + 21i - 1; \ 1 \le i \le n - 1$   $f^{*}(e_{i}') = \begin{cases} k + 21i - 20; \ 1 \le i \le n; if n is odd \\ k + 21i - 3; \ 1 \le i \le n; if n is odd \\ k + 21i - 12; \ 1 \le i \le n; if n is odd \\ k + 21i - 12; \ 1 \le i \le n; if n is odd \\ k + 21i - 20; \ 1 \le i \le n; if n is odd \\ k + 21i - 20; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 10; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 5; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 16; \ 1 \le i \le n; if n is odd \\ k + 21i - 15; \ 1 \le i \le n; if n is odd \\ k + 21i - 15; \ 1 \le i \le n; if n is odd \\ k + 21i - 15; \ 1 \le i \le n; if n is odd \\ k + 21i - 9; \ 1 \le i \le n; if n is odd \\ k + 21i - 9; \ 1 \le i \le n; if n is odd \\ k + 21i - 9; \ 1 \le i \le n; if n is odd \\ k + 21i - 9; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le i \le n; if n is odd \\ k + 21i - 8; \ 1 \le n; if n is odd \\ k + 21i - 8; \ 1 \le n; if n is odd \\ k + 21i - 8; \ 1 \le n; if n is odd \\ k + 21i - 8; \ 1 \le n; if n is odd \\ k + 21i - 8; \ 1 \le n; if n is odd \\ k + 21i - 8; \$  $f^*(e_i) = k + 21i - 1; \ 1 \le i \le n - 1$ 



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 $f^*(e_i^{xii}) = \begin{cases} k+21i-9; & 1 \le i \le n; if \ n \ is \ odd \\ k+21i-14; & 1 \le i \le n; if \ n \ is \ even \end{cases}$ 

Here p = 8n, q = 13n-1. Clearly,  $f(V) \cup \{f^*(e) : e \in E([P_n; Q_3])\} = \{k, k + 1, ..., k + 21n - 2\}$ . So f is a k – Super mean labeling. Hence  $[P_n; Q_3]$  is a k – Super mean graph.

# P. Example 2.16

50 – Super mean labeling of  $[P_2; Q_3]$  is given in figure 2.3:

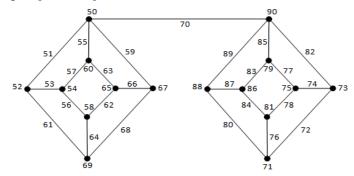


Figure 3: 50 – Super mean labeling of  $[P_2; Q_3]$ 

### Q. Theorem 2.17

The graph  $T_n \cup T(L_m)$  is a k-Super mean graph for all  $n, m \ge 2$ . Proof: Let  $V(T_n \cup T(L_m)) = \{u_i, v_i; 1 \le i \le n\} \cup \{w_i, w'_i, 1 \le i \le m\}$  and  $E(T_n \cup T(L_m)) = \{e_i = (u_i, u_{i+1}), e'_i = (v_i, u_i); 1 \le i \le n-1\}$  $1\} \cup \{e_i'' = (v_{i}, u_{i+1}), e_i''' = (w_{i}, w_{i+1}); 1 \le i \le n-1\} \cup \{e_i^v = (w_{i+1}, w_i'), e_i^{vi} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_{i+1}'), 1 \le i \le n-1\} \cup \{e_i^{iv} = (w_i', w_i'), 1 \le n-1\} \cup \{e_i^{iv} = (w_i', w_i'),$  $(w_i, w'_i)$ ;  $1 \le i \le n$ } be the vertices and edges of  $T_n \cup T(L_m)$  respectively. Define  $f: V(T_n \cup T(L_m)) \to \{k, k+1, k+2, ..., k+5n+6m-8\}$  by  $f(u_i) = k + 5i - 5; \ 1 \le i \le n$  $f(v_i) = k + 5i - 3; \ 1 \le i \le n - 1$  $f(w_i) = f(u_n) + 6i - 5; \ 1 \le i \le m$  $f(w'_i) = f(u_n) + 6i - 3; \ 1 \le i \le m$ Now the induced edge labels are  $f^*(e_i) = k + 5i - 2; \ 1 \le i \le n - 1$  $f^*(e'_i) = k + 5i - 4; \ 1 \le i \le n - 1$  $f^*(e_i'') = k + 5i - 1; \ 1 \le i \le n - 1$  $f^*(e_i'') = f(u_n) + 6i - 2; \ 1 \le i \le m$  $f^*(e_i^{iv}) = f(u_n) + 6i - 4; \ 1 \le i \le m - 1$  $f^*(e_i^v) = f(u_n) + 6i - 1; \ 1 \le i \le m - 1$  $f^*(e_i^{vi}) = f(u_n) + 6i; \ 1 \le i \le m - 1$ Here p = 2(m+n)-1, q = 3n+4m-6. Clearly,  $f(V) \cup \{f^*(e) : e \in E(T_n \cup T(L_m))\} = \{k, k+1, \dots, k+5n+6m-8\}.$ So f is a k – Super mean labeling. Hence  $(T_n \cup T(L_m))$  is a k – Super mean graph.

#### R. Example 2.18

200 – Super mean labeling of  $(T_4 \cup T(L_4))$  is given in figure 4:



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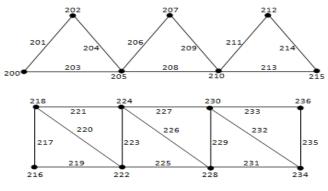


Figure 4: 200 – Super mean labeling of  $(T_4 \cup T(L_4))$ 

S. Definition 2.19: Double  $D(F_n)$  is obtained by  $P_n+2K_1$ .

T. Theorem 2.20 The graph  $D(F_n)$  is a k-Super mean graph for all  $n \ge 1$ . Proof: Let  $V(D(F_n)) = \{u, v\} \cup \{u_i; 1 \le i \le n\}$  and  $E(D(F_n)) = \{e_i = (u_i, u_{i+1}); 1 \le i \le n-1\} \cup \{e'_i = (u_i, u); 1 \le i \le n\} \cup \{u_i, u\}$  $\{e_i^i = (u_i, v); n + 1 \le i \le 2n, 1 \le j \le n\}$  be the vertices and edges of  $D(F_n)$  respectively. Define  $f: V(D(F_n)) \to \{k, k + 1, k + 2, ..., k + 4n - 2\}$  by f(u) = kf(v) = k + 4n $f(u_i) = k + 4i - 2; \ 1 \le i \le n$ Now the induced edge labels are  $f^*(e_i) = k + 4i; \ 1 \le i \le n - 1$  $f^*(e'_i) = k + 2i - 1; \ 1 \le i \le 2n$ Here p = n+2, q = 3n-1. Clearly,  $f(V) \cup \{f^*(e) : e \in E(D(F_n))\} = \{k, k + 1, ..., k + 4n - 2\}.$ So f is a k – Super mean labeling. Hence  $D(F_n)$  is a k – Super mean graph.

*U. Example 2.21:* 

100 – Super mean labeling of  $D(F_7)$  is given in figure 5:

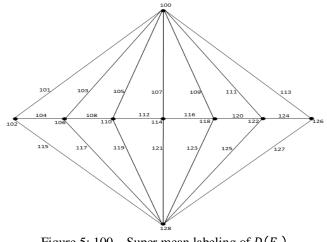


Figure 5: 100 -Super mean labeling of  $D(F_7)$ 



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#### **III.CONCLUSIONS**

Graph labeling has its own applications in communication networks and astronomy. so, enormous types of labeling have grown. Towards this, k-super mean labeling is also a kind of labeling which is an extension of super mean labeling. we discussed k-super mean labeling of the graphs  $n(S(S_3))$ ,  $(P_n; S_2)$ ,  $[P_n; Q_3]$ ,  $T_n \cup T(L_m)$ ,  $D(F_n)$ .

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