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# Algorithms for Image Denoising using Hard Thresholding in Curvelet Domain

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**Abstract:** Generally due to random variation of pixel values, Speckle Noise will occur in images. So it is essential to apply various filtering Algorithms to denoise such an images. There are Wiener filtering and Wavelet based thresholding methods to denoise noisy images. In this paper initially I used Wiener filter for the purpose of reducing the noise but this does not exhibit satisfactory performance. Curvelet transform represents natural image better than any other transformations. Therefore, Curvelet coefficient can be used to segment true image and noise. In this, threshold based denoising algorithm has been developed using hard thresholding techniques in Curvelet domain, the experimental results shows its efficacy over Wiener filtering method. So Speckle noise can be effectively reduced by using Thresholding in Curvelet domain.

**Index Terms:** Speckle Noise, Wiener filtering, Curvelet transform, Image thresholding techniques.

## I. INTRODUCTION

For better quality, analysis with good vision, Image denoising is required. There are different types of noises which can degrade the quality of images. In this paper I concentrate on the Speckle noise occurs due to random variation of the pixel values. Mathematically this noise is modelled as:

$$\text{Speckle noise} = I * (1 + N)$$

Where 'I' is the original image matrix and 'N' is the noise with zero mean value having normal distribution. Wiener filtering comes under the non-coherent type of denoising method, which is mainly used as a restoration technique for all type of noisy images. However this filter does not giving better quality of images. Curvelet transform was introduced to overcome this disadvantage. Curvelet transform is developed from Wavelet as multi-scale representation. In Curvelet domain the large coefficients value are shown as original image signal and the small coefficients value shown as noise signal. In this paper, I proposed first discrete Curvelet transform with Hard thresholding method. The proposed method consist of three parts, Curvelet transform(FDCT), Curvelet coefficients processing and inverse transform(IFDCT). In the first step Curvelet transform of noisy image is calculated which are threshold by different thresholding function. Finally, inverse Curvelet transform is found to reconstruct denoising image. The reconstructed denoised image was compared with original image. Here Hard thresholding without logarithm and with logarithm is performed.

## II. WIENER FILTERING ALGORITHM

An optimum linear filter which is involved only for linear estimation of a desired signal sequence is Wiener filter. The Wiener filter algorithm considers a signal  $S_x(f)$  corrupted with noise  $S_n(f)$ . The noise has zero mean and variance of  $\sigma_n^2$ . The resulting signal obtained after Wiener filtering will be  $H(f)$ . The transfer function corresponding to Wiener filter was given by:

$$H(f) = \frac{S_{xy}(f)}{S_y(f)} = \frac{S_x(f)}{S_x(f) + S_n(f)} \dots\dots\dots (1)$$

This filter-optimization problem is to minimize the mean-square error of the signal that is defined by the actual filter output. This resulting solution is commonly known as the Wiener filter. The block diagram of a Wiener filter is shown in figure 1.

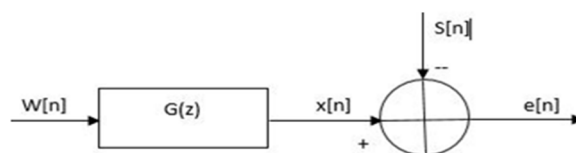


Figure 1: Block Diagram of Wiener Filter for Denoising Speckle Noisy image.

Here,

$$G(Z) = \sum_{i=0}^N a_i Z^{-i} \dots\dots\dots (2)$$

$w[n]$  and  $s[n]$  are random process signal. The filter output is  $x[n]$  and  $e[n]$  are the estimation error. An input signal  $w[n]$  is convolved with the Wiener filter  $G[z]$  and the result is compared to a reference signal  $s[n]$  to obtain the filtering error  $e[n]$ . The image denoising using the Wiener filter is shown in the flowchart in figure 2.

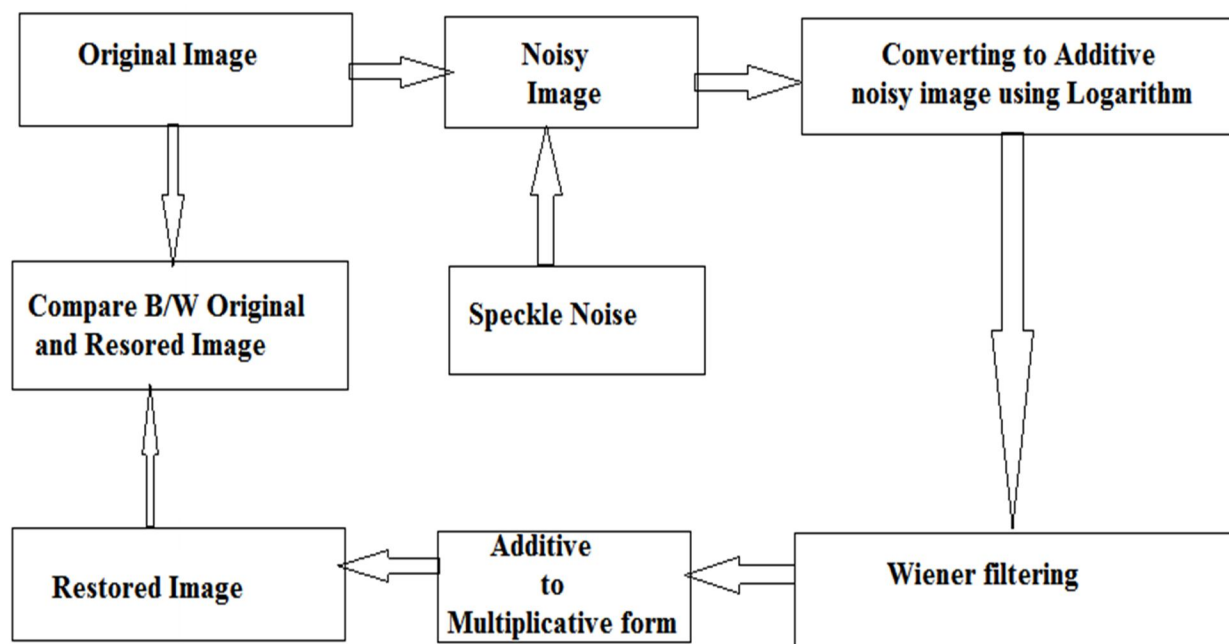


Figure 2: Flowchart of Denoising using Wiener Filter Algorithm

Step by step Algorithm for denoising using Wiener Filter:

- 1) Step 1: Take an original image.
- 2) Step 2: Add different variance of multiplicative (speckle) noise with original image.
- 3) Step 3: Convert the multiplicative noisy image into additive noisy image using logarithmic Transformation.
- 4) Step 4: Applying the Wiener filtering to additive noisy image. Here, I am using different size of Wiener filter mask. The mask size depending upon noise variance.
- 5) Step 5: Showing the restored image after Wiener filtering.
- 6) Step 6: Convert the restored image from additive to multiplicative form using anti- logarithmic transformation.
- 7) Step 7: Compare the restored image that obtained in step 6 with original image.

### III. ALGORITHM OF IMAGE DENOISING IN CURVELET DOMAIN

The idea of the Curvelet transform is first to decompose the image into Subband. The discrete Curvelet transform is mathematically expressed as:

$$c^D(j, l, k) = \sum_{0 \leq t_1, t_2 < n} f[t_1, t_2] \overline{\varphi_{j,l,k}^D[t_1, t_2]} \dots\dots\dots (3)$$

Where,  $f[t_1, t_2]$  is 2D signal of Cartesian arrays with  $t_1 \geq 0$  and  $t_2 < n$ .  $C^D(j, l, k)$  are Curvelet coefficients at scale  $j$ , location  $l$  and coordinates  $k = (k_1, k_2) \in \mathbb{Z}^2$ , and  $\varphi_{j,l,k}^D$  is a digital Curvelet waveform, here the superscript D is stands for digital. Here, I proposed two different algorithms in Curvelet domain with two different thresholding methods, first algorithm is for image denoising in Curvelet domain using hard thresholding without logarithmic function and second one is with logarithmic function.

**A. Algorithm For Image Denoising In Curvelet Domain Using Hard Thresholding**

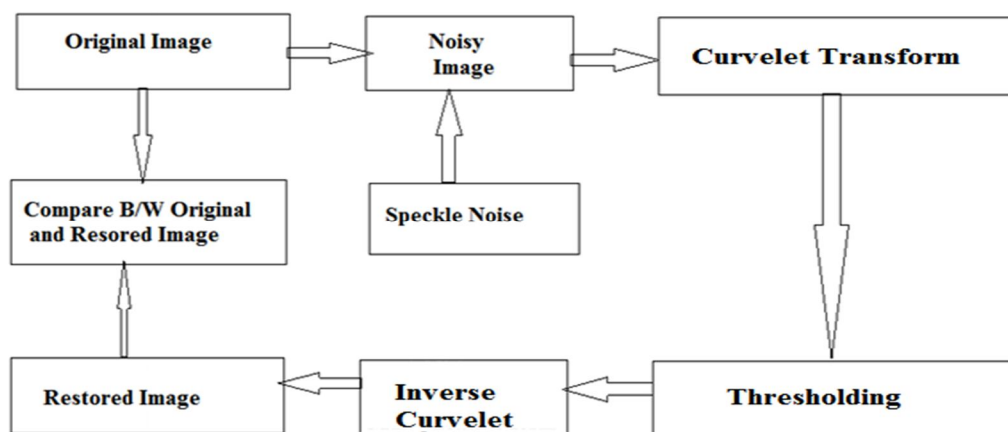


Figure 3: Flowchart of Curvelet Transform Algorithm for image Denoising using Hard Thresholding.

Step by step Algorithm for denoising using Hard Thresholding

- 1) Step 1: Take the original image.
- 2) Step 2: Add different variance of multiplicative (speckle) noise with original image.
- 3) Step 3: Apply the Curvelet transformation of noisy image.
- 4) Step 4: Apply different thresholding approach over the Curvelet coefficient.
- 5) Step 5: Applying inverse Curvelet transformation to obtain the restored image over the thresholded Curvelet coefficient.
- 6) Step 6: Compare the restored image that obtained in step 6 with original image.

**B. Algorithm For Image Denoising In Curvelet Domain Using Hard Thresholding With Logarithm**

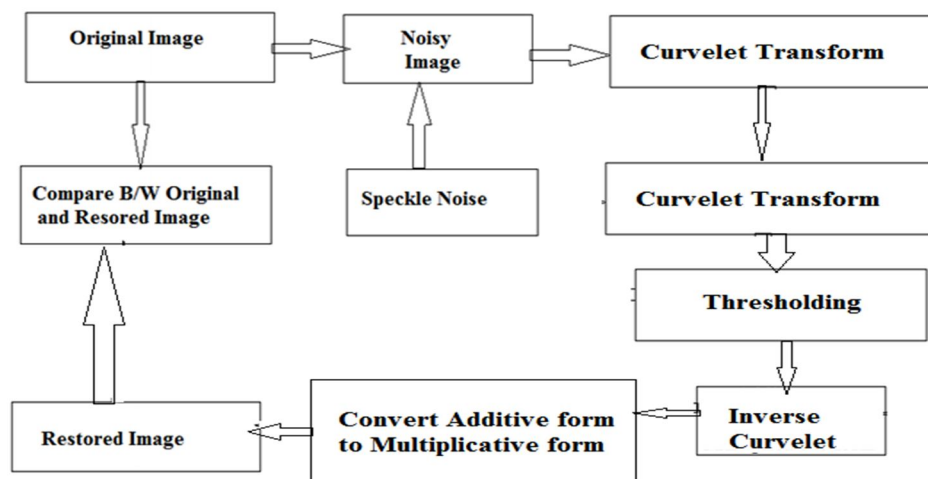


Figure 4: Flowchart of Curvelet Transform Algorithm for image Denoising using Hard Thresholding with Logarithm.

Step by step Algorithm for denoising using Hard Thresholding:

- 1) Step 1: Take the original image.
- 2) Step 2: Add different variance of multiplicative (speckle) noise with original image.
- 3) Step 3: Convert the multiplicative noisy image into additive noisy image using logarithmic transformation.
- 4) Step 4: Apply the Curvelet transformation on noisy image.
- 5) Step 5: Apply different thresholding approach over the Curvelet coefficient.
- 6) Step 6: Applying inverse Curvelet transformation to obtain the restored image over the thresholded Curvelet coefficient.
- 7) Step 7: Convert the restored image from additive to multiplicative form using anti-logarithmic transformation.
- 8) Step 8: Compare the restored image that obtained in step 6 with original image.



Hard-thresholding is a type of global thresholding, in this thresholding method thresholds the complete image with a single threshold value. So using that method for image denoising select one threshold value for whole image. Hard thresholding sets to zero those elements whose absolute value is lower than the threshold value and neglecting zero element. Hard thresholding function is as follows:

$$f(y) = \begin{cases} y, & |y| > \lambda \\ 0, & |y| \leq \lambda \end{cases} \dots\dots\dots (4)$$

Where,  $y$  and  $f(y)$  are the Curvelet coefficients before and after hard threshold processing,  $\lambda$  is a threshold value.

#### IV. RESULT & DISCUSSIONS

In this paper results of two different image restoration techniques are presented. First one is analysis of Wiener filter based method and the second one is proposed method in sparse/ transform domain using hard thresholding with and without logarithm function. The statistical parameters are computed for original and restored as well as original and noisy images. A comparative result is presented

##### A. Original Image with Different Noise Variance for Standard Image (Lena)



Figure 5: (a) Original image, 512 by 512, 8bits/pixel, with MSE = 0, PSNR = 1, (b) Speckle noisy image with var.0.04, (c) Speckle noisy image with var. 0.06, (d) Speckle noisy image with var. 0.08

##### B. Denoised Standard Image (Lena) in Frequency Domain using Wiener Filtering with Different Noise Variance



Figure 6: (a) Original image, 512 by 512, 8bits/pixel, with MSE = 0, PSNR = 1, (b) Restored image of noise var.0.04, (c) Restored image of noise var. 0.06, (d) Restored image of noise var.0.08

##### C. Denoised Standard Image (Lena) in Sparse/Transform Domain with Different Noise Variance using Hard-thresholding



Figure 7: (a) Original image, 256 by 256, 8bits/pixel, with MSE = 0, PSNR = 1, (b) Restored image of noise var.0.04, (c) Restored image of noise var. 0.06, (d) Restored image of noise var.0.08

**D. Denoised Standard Image (Lena) in Sparse/Transform Domain with Different Noise Variance using Hard-thresholding with Logarithm.**



Figure 8: (a) Original image, 256 by 256, 8bits/pixel, with MSE = 0, PSNR =1, (b) Restored image of noise var.0.04,(c)Restored image of noise var. 0.06, (d) Restored image of noise var.0.08

## V. CONCLUSION

The results of all restoration techniques such as the nonlinear Wiener filtering method in Frequency domain, Hard-thresholding in sparse domain without logarithm and Hard-thresholding in sparse domain with logarithm have been described. The obtained restored image is compared with original image. So I conclude that the restoration method Hard-thresholding in sparse domain using logarithm is better than other nonlinear Wiener filtering in Frequency domain and Hard-thresholding in sparse domain without logarithm methods.

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