



iJRASET

International Journal For Research in
Applied Science and Engineering Technology



INTERNATIONAL JOURNAL FOR RESEARCH

IN APPLIED SCIENCE & ENGINEERING TECHNOLOGY

Volume: 6

Issue: XI

Month of publication: November 2018

DOI:

www.ijraset.com

Call:  08813907089

E-mail ID: ijraset@gmail.com

A Methodology for Selection of an Optimum Gear Ratio for Single Speed Gearbox coupled with Continuously Variable Transmission to Achieve Best Acceleration Performance

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Abstract: The work presented deals with a numerical iterative methodology that was implemented to find an optimum speed ratio for a gearbox coupled with continuously variable transmission (CVT). The optimization has been done with the primary design objective of maximizing acceleration performance of an SAE Baja Vehicle. The time taken by the vehicle to traverse a certain specified distance is a function of the gear ratio of the vehicle. An initial estimate of this gear ratio was computed based on analytical calculations considering weight shift due to acceleration for a no-tire-slip condition. However, this analytical computation ignores the additional tractive effort afforded by moment of aerodynamic drag force and loss of torque due to rotational inertia of transmission components. Hence, this computation results in under-utilization of the available tractive effort and a more aggressive gear ratio is possible without the loss of traction. This optimized ratio is not possible to be computed manually, hence an algorithm has been developed for iterative calculations. Along with aerodynamic drag, rolling resistance, tire slip and engine rev limitations along with various system efficiencies have been considered in the program. The program computes the kinetic parameters in four distinct phases of the CVT. This algorithm predicts a more aggressive ratio which can be implemented without loss of traction. Measuring the performance improvement achieved in terms of 150 ft. traversal time, an 8.54% improvement was observed compared to the analytically predicted gear ratio.

Keywords: Continuously Variable Transmission, SAE Baja, Acceleration Performance, Traversal Time, MATLAB, tire slip.

I. INTRODUCTION

The motivation behind this work was to develop an optimized transmission system for an SAE Baja Vehicle. The metric used for determining vehicle performance is the 150 ft. straight line traversal time, wherein the minimum time suggests the best transmission system. Numerical simulation has been a preferred method for determining vehicle characteristics such as fuel economy and performance. One such vehicle simulation tool for automobiles and light commercial vehicles is VEHSIM [3]. A simplified algorithm has been derived by using the analytical treatment done by Zub R. W., to determine the optimum speed ratio for a single speed transmission system coupled to a centrifugal Continuously Variable Transmission, a common layout for SAE Baja vehicles.

II. DESIGN APPROACH

To achieve the best possible acceleration performance, one needs to first estimate the normal force acting on the driving wheels. In this particular case discussed in the paper, the vehicle is rear wheel driven and is assumed to be accelerating on level ground without any hitch forces pulling back on the vehicle. This normal force is a function of the acceleration of the vehicle due to the dynamic effects of weight transfer between the axles. Hence, an additional equation relating the acceleration of the vehicle and normal force is required. For maximizing the acceleration performance, the entire traction available at the driving wheels must be utilized. Using these two conditions the normal reaction at the rear wheels is calculated. This normal reaction is used to calculate the available tractive force. Given the available torque at the engine, the available tractive force is equated to the tractive effort of the engine in terms of a gear ratio. Solution of this equation is the first estimate of the gear ratio required to achieve maximum acceleration performance.

However, this is a crude estimate as it is valid only for the initial acceleration phase and also does not consider the effects of tire slip and rotational inertia of transmission components. Also, as the primary design objective of this optimization study is to minimize the straight-line trajectory traversal time, dynamic parameters such as drag force, clutching phase of CVT, change of overall

```

graph TD
    START([START]) --> Input[/Input gear ratio and vehicle parameters/]
    Input --> ComputeTractive[Compute tractive forces based on torque equation of engine]
    ComputeTractive --> ComputeResistive[Compute resistive forces from vehicle velocity]
    ComputeResistive --> ComputeAcceleration[Compute constant instantaneous acceleration]
    ComputeAcceleration --> ComputeVelocity[Compute vehicle velocity at the end of time step and displacement during time step]
    ComputeVelocity --> UpdateEngine[Update engine speed or CVT ratio]
    UpdateEngine --> Decision{ $s \geq 150$  ft.}
    Decision -- No --> ComputeTractive
    Decision -- Yes --> Plot[/Plot graphs/]
    Plot --> END([END])
  
```

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W - weight of the vehicle

$W/g.a_x$ - d'Alembert Force

W_f and W_r - Dynamic weights carried by front and rear wheels.

F_{xf} and F_{xr} – Tractive forces on front and rear wheel

R_{xf} and R_{xr} – Rolling resistance forces on front and rear wheel respectively

D_A – Aerodynamic drag force

R_{hz} and R_{hx} – Vertical and longitudinal hitch forces

θ - Grade angle

Considering summation of torques about point B (assuming zero angular acceleration of vehicle in pitch), the following equation is obtained.

$$W_r = (Wb \cos \theta + R_{hx} h_h + R_{hz} (d_h + L) + \frac{W}{g} a_x h + D_A h_a + W h \sin \theta) / L \quad (1)$$

For a vehicle accelerating at low speed on level ground without any hitch forces the equation reduces to

$$W_r = W \left(\frac{b}{L} + \frac{a_x}{g} \frac{h}{L} \right) \quad (2)$$

For maximum possible acceleration, the entire traction at the driving wheels is used to push the vehicle. Hence the following equation is obtained.

$$a_{x(\max)} = \frac{\mu W_r}{W} g \quad (3)$$

Where, μ is the coefficient of static friction at the road-tire interface and g is the gravitational acceleration of earth (9.81 m/s^2).

Solving equations (2) and (3) simultaneously the following equation is obtained.

$$W_r = \frac{Wb}{L - \mu h} \quad (4)$$

Thus, the available tractive force at rear wheels is given by

$$F_{xr(\text{available})} = \mu \frac{Wb}{L - \mu h} \quad (5)$$

B. Analytical Calculations For Estimating Initial Gear Ratio

Now, considering the tractive effort of the engine at the driving wheels in terms of gear ratio, following equation can be derived.

$$F_{xr} = \frac{T_e N_{tf} \eta_{tf}}{r} \quad (6)$$

Where,

T_e – Torque provided by the engine

N_{tf} – Final driveline gear ratio

η_{tf} – Final driveline efficiency

r – Radius of wheel

Equation (6) ignores the effect of rotational inertia of transmission components and wheels. However, this effect has been considered in the algorithm of the code.

Equating equation (5) and (6), the final driveline gear ratio can be expressed as

$$N_{tf} = \frac{\mu r W b}{T_e \eta_{tf} (L - \mu h)} \quad (7)$$

The final driveline ratio consists of the CVT reduction times the gear ratio of the two-step compound single-speed gearbox coupled to it. The CVT used in this study is Gaged GX9 having a low speed ratio of 3.9:1 and an overdrive speed ratio of 0.9. During the shifting phase, this ratio varies continuously. Substituting the speed reduction obtained from CVT in equation (7), the following expression is obtained.

$$N_{gearbox} = \frac{\mu r W b}{N_{CVT} T_e \eta_{tf} (l - \mu h)} \quad (8)$$

Substituting the vehicle parameters in equation (8), the gearbox ratio evaluated for this specific vehicle is 7.23. This gear ratio is a close approximation of the optimum gear ratio. However, it tends to underutilize the available ground traction. This is owing to that fact that the effect of aerodynamic drag and rotational inertia of wheels and transmission components has not been considered.

IV. NUMERICAL ITERATIVE METHODOLOGY USED FOR OPTIMIZATION

To refine the initial estimation of the gear ratio, a numerical algorithm has been developed. This algorithm considers a very small time step (0.001 seconds for this study/5 to 6 million calculations per simulation) during which the traction and resistive forces acting on the vehicle and the associated acceleration can be assumed to be constant. This value was iteratively selected for achieving a reasonable computational accuracy and acceptable simulation run time. The vehicle velocity at the start of this time step and the computed acceleration for that time step can then be used to calculate the vehicle velocity at the end of the time step by applying elementary equations of kinematic motion. Also, the displacement of the vehicle during this time step can be calculated.

$$v_f = v_i + a_{ts} t \quad (9)$$

$$s_{ts} = v_i t + \frac{1}{2} a_{ts} t^2 \quad (10)$$

where,

v_f – Final vehicle velocity at the end of the time step
 v_i – Initial vehicle velocity at the start of the time step
 s_{ts} – Displacement of the vehicle during the time step

a_{ts} – Constant vehicle acceleration during the time step
 t – Duration of the time step

This computed final vehicle velocity can then be fed back into the algorithm to calculate the tractive and resistive forces experienced by the vehicle for the next time step.

For this particular case, the only resistive forces acting on the vehicle are the aerodynamic drag for (D_A) and the rolling resistance offered by tires (R_x). The expressions for all these forces have been stated below.

$$D_A = \frac{1}{2} \rho V^2 C_D A \quad (11)$$

$$R_x = R_{xf} + R_{xr} = f_r W \quad (12)$$

Where,

ρ – Density of air at normal temperature and pressure
 V – Vehicle velocity

C_D – Coefficient of aerodynamic drag
 f_r – Coefficient of rolling resistance

The coefficient of aerodynamic drag has been considered to be 0.7 in this case. For typical SAE Baja vehicles, this coefficient varies from 0.6-1 [4], [5]. Considering the range of speeds experience by such a vehicle, the rolling resistance can be safely assumed to be constant. The coefficient of rolling resistance for tractor travelling on hard muddy terrain has been used in the simulation [1] Using this data, the algorithm computes the resistive forces on the vehicle at each time step.

Apart from these, there are inertial losses due to the rotational masses on the vehicle. For all the rotating components, the torque loss is considered by the following equation given by [1].

$$F_x = \frac{T_e N_{tf} \eta_{tf}}{r} - [(I_e + I_t) N_{tf}^2 + I_d N_f^2 + I_w] \frac{a_x}{r^2} \quad (13)$$

Where,

I_e – Rotational inertial of engine

I_d – Rotational inertia of driveshaft

I_t – Rotational inertia of transmission

I_w – Rotational inertia of wheels and axle shafts

N_{tf} – Numerical ratio final drive ratio

In this equation the tires are assumed to be in pure rolling. For the vehicle under consideration, the engine output torque is the net torque provided by the engine considering inertial losses. Hence the term I_e refers only to the rotational inertia of the primary CVT pulley. The term I_t refers to the rotational inertial of the secondary CVT pulley, gears and shafts inside the gearbox. A final drive system is also absent in the vehicle as provisions for transmitting power to the half shafts is included in the gearbox itself [6]. Hence, $I_d = 0$.

Also, by applying Newton's Second Law (NSL) of motion

$$M a_x = F_x - D_A - R_x \quad (14)$$

Combining equation (13) and (14), longitudinal vehicle acceleration can be expressed as follows.

$$a_x = \frac{\frac{T_e N_{tf} \eta_{tf}}{r} - D_A - R_x}{M + \frac{\{(I_e + I_t) N_{tf}^2 + I_w\}}{r^2}} \quad (15)$$

Computation of tractive forces is comparatively more complex than that of resistive forces. Firstly, the variation of engine torque at wide-open throttle with revving speed of the engine needs to be accounted for in the algorithm. The engine used for the vehicle is Briggs and Stratton M19H. The following graph shows the torque variation of this engine.

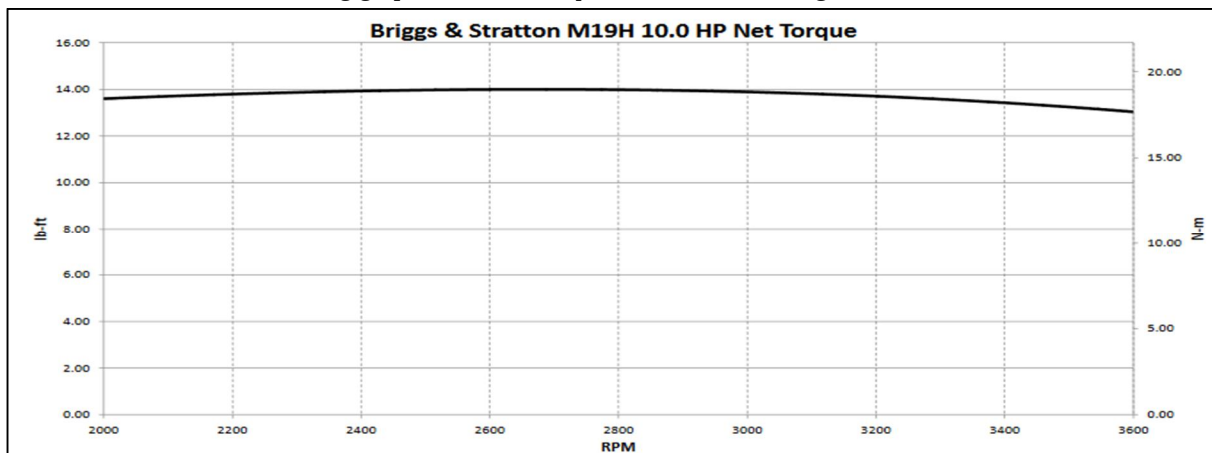


Figure 3: Briggs and Stratton M19H net torque curve
(Courtesy: Briggs & Stratton Racing, Milwaukee, WI)

For modelling this variation mathematically, a quadratic least square regression of the data has been used to relate the torque output of the engine at any given engine speed. This equation has been expressed below.

$$T = -1.4879 \times 10^{-6} N^2 + 8.3945 \times 10^{-3} N + 7.8578 \quad (16)$$

Where,

T – Torque delivered by engine at wide open throttle (N-m) N – Engine speed in revolutions per minute (RPM)

As a CVT transmission has been used in the vehicle, engine power is delivered to the wheels in 4 distinct phases. These phases have been illustrated in [2] and shown below.

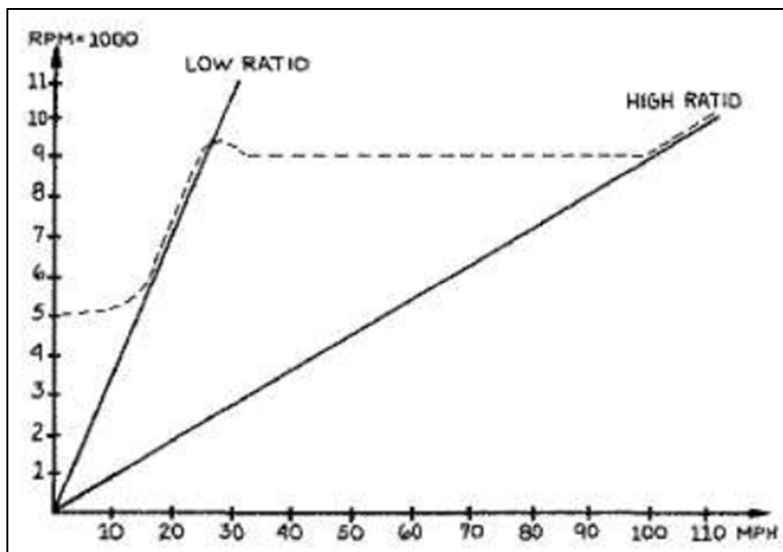


Figure 4: Speed diagram of variable speed transmission [2]

The mathematical modelling of these phases in the algorithm has been expressed below.

A. CVT Pre-engagement Phase (Clutching Phase)

During this phase, there is belt slippage occurring at the primary sheave of the CVT which provides the clutching action required to start the vehicle from standstill. Numerical analysis of this phase involves complex kinematical modelling of the components of primary clutch such as roller-cam interface and dynamics of belt-sheave interactions [10], [11], [12]. Such a mathematical treatment is out of scope for this work and hence the following assumptions have been considered for modelling of the clutching phase.

Firstly, the engine speed is assumed to be a quadratic spline variation in terms of vehicle velocity. The equation for this variation can be derived from the following boundary conditions.

$$V = 0 \Rightarrow N = N_i \quad (17)$$

$$V = V_e \Rightarrow N = N_e \quad (18)$$

$$\frac{dN}{dV}_{V=0} = 0 \quad (19)$$

Where,

V_e – Speed of the vehicle at 100% primary clutch engagement N_e – Speed of engine at 100% primary clutch engagement

N_i – Idling speed of engine

The value of V_e can be analytically determined by gearing calculations. The value of N_i and N_e are selected for required vehicle performance. The engine idling speed for the vehicle under study is set to 1600 RPM by adjusting the throttle valve opening and the required engagement speed is set to 1800 RPM by adjusting the preloaded tension of the primary spring.

Thus, the variation of engine speed with respect to vehicle velocity during this phase can be expressed as

$$N = 60.7370V^2 + 1600.0000 \quad (20)$$

Where N is in revolutions per minute and V is in meters per second. Equation (20) is calculated dynamically by the program and the coefficients are dependent upon the gear ratio given as input to the program. Hence this equation varies during each optimization iteration. The slope continuity is not maintained for the curve at engagement speed. To meet this criterion a higher order polynomial would be required.

The power delivered by the engine during the clutching phase is lost in the form of frictional heat generated due to belt slipping. Hence, only a fraction of the torque produced by the engine as given by equation (16) is transmitted to the wheels. The torque transmitted by the primary sheave is directly proportional to the centrifugal force acting on the flyweights. Hence the torque during this phase has been assumed to vary quadratically with engine speed. The equation for this variation is given by the following boundary conditions.

$$N = N_i \Rightarrow T = T_i \quad (21)$$

$$N = N_e \Rightarrow T = T_e \quad (22)$$

$$\frac{dT}{dN}_{N=N_e} = C_1 \quad (23)$$

Where,

T_i – Theoretical net initial torque generated by engine at N_i C_1 – Slope of torque curve at N_e

T_e – Net torque generated by engine at N_e

T_e and C_2 can be computed by substituting $N = N_e$ in equation (16) and its first order differential respectively. T_i can be approximated by considering the side pressure exerted by the primary sheave onto the V-belt [7] [8] [9]. Thus, the equation for torque provided by engine during this phase is given by

$$T = -1.5568 \times 10^{-4} N^2 + 0.5634 N - 491.6480 \quad (24)$$

The above assumptions also consider the efficiency of power transmission of the CVT during the clutching phase. Hence, the only the transmission efficiency of the gearbox [13] and CV joints [14] has been considered. Also, if wheel slip occurs during the clutching phase, it is assumed that the clutching effect of the CVT stops as power flows through the path of minimum resistance, which now occurs at the road-wheel interface. In this case, the torque is calculated using equation (16)

Substituting equation (24) in equation (15), the acceleration of the vehicle during this phase can be calculated. This acceleration is assumed to be constant during any time step and is used to calculate the velocities at the end of the time step using equation (9). In this phase the initial velocity of the vehicle is zero. The final velocity achieved at the end of the time step is then substituted in equation (20) to re-calculate the engine RPM for the next phase. Also, the displacement of the vehicle at each time step is calculated using equation (10). These iterations are continued till the CVT is 100% engage and no macro slippage of belt occurs.

B. Constant Speed Ratio Phases ($N \propto V$)

After completing of the clutching phase, the engine speed varies linearly with vehicle velocity. Hence, there exists a fixed constant gearing ratio between the engine and the wheels. This relationship can be expressed mathematically using the following equation.

$$N = \frac{60 N_{tf}}{2\pi r} V = C_2 V \quad (25)$$

The constant of proportionality C_2 is different for the low ratio and the high ratio of CVT due to different overall final drive ratio. An approximation of the system efficiency in these phases needs to make to accurately predict the acceleration performance. The efficiency variation has been given in [2] and shown in following graph.

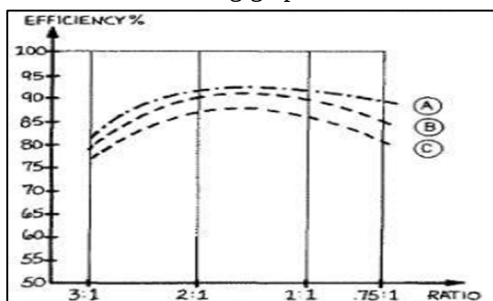


Figure 5: Variation of CVT efficiency with speed ratio [2]

Considering a CVT efficiency of 85% during this phase, the overall system efficiency can be obtained. The acceleration in this phase can be calculated by using equation (15) and (16). The final velocity of the vehicle from the previous phase is used as the initial velocity for this phase. For each time step, the final velocity obtained from equation (9) is used to calculate the engine speed for the next time step using equation (25). The algorithm computes the vehicle performance sequentially as the final kinematic parameters obtained from the simulation are inputs for the next. Hence, the simulation of the low ratio phase of CVT is done immediately after the clutching phase. This phase ends when the engine speed reaches maximum peak power (shift point). The simulation of the overdrive phase (high ratio) can be performed only after the shifting phase has been completed. The high ratio phase also considers the engine maximum revving limitations and stops accelerating the vehicle in case such high engine speeds are reached.

C. CVT Shifting Phase

When the engine reaches peak power, the function of the CVT is to maintain the engine at this speed by changing the overall gearing ratio. By keeping the engine in the maximum power regime of its power curve, the performance of the vehicle can be maximized. This constancy of engine speed is achieved by means of changing the CVT speed ratio, thereby affecting the overall gearing ratio. As the vehicle speeds up, the CVT up-shifts, thereby not allowing the engine speed to increase with the wheel speed. Assuming perfect shift curve, this change in the CVT speed ratio can be mathematically expressed by the following equation.

$$N_{CVT} = \frac{2\pi r N_s}{60 N_{gearbox}} \frac{1}{V} \quad (26)$$

Where N_s is the engine speed at which the CVT shift occurs. This speed is determined by the flyweight masses of the primary spring and the torsion spring stiffness of the secondary pulley spring. Another factor affecting the shifting response of the CVT are the cam profiles used in both the pulleys. For this vehicle, the CVT has been tuned to shift at engine speed of 3600 RPM. Efficiency of the CVT has been assumed to be 90% during this phase (see fig. 5).

Similar to the other phase, acceleration and velocities for each time step are computed using the equations discussed previously. The velocity obtained at the end of each time step is used to back calculate the changed CVT ratio using equation (26). This simulation phase is continued till the CVT reaches its overdrive ratio.

D. Case Of Insufficient Traction

During all of these phases of the CVT simulation, only the power limited performance of the vehicle has been considered. In order to ensure the validity of the simulation, the accelerations obtained at each time step need to be compared with the traction limited acceleration possible at the time step. The traction limited acceleration can be obtained by modifying equation (2) to include the moment of aerodynamic drag forces.

$$W_r = W \left(\frac{b}{L} + \frac{a_x}{g} \frac{h}{L} \right) + \frac{D_A h_a}{L} \quad (27)$$

Solving equation (27) and (3) simultaneously, the maximum traction limited acceleration at any given instant is given by the following equation.

$$a_{x\max} = \frac{Wb + D_A h_a}{L - \mu h} \frac{\mu g}{W} \quad (28)$$

If at any time step, the power limited acceleration given by equation (25) exceeds the traction limited acceleration given by equation (28), macro-slipping of vehicle tire occurs and the vehicle travels with a constant acceleration. This acceleration can be computed by substituting $\mu = \mu_k$ i.e. coefficient of kinetic friction, in equation (28) [15]. Also, the angular acceleration of wheels can be mathematically expressed by modifying equation (13) and replacing tractive force by kinetic frictional force.

$$\alpha_{wheels} = \left(\frac{T_e N_{tf} \eta_{tf} - \mu_k \frac{Wb + D_A h_a}{L - \mu_k h} r}{[(I_e + I_t) N_{tf}^2 + I_w]} \right) \quad (29)$$

This angular acceleration is assumed to be constant during each time step. It can be used to calculate the angular velocity of the driving wheels at the end of the time step. The angular velocity is fed back into the algorithm and is used to either calculate the

engine RPM for the next time step (if wheel slip occurs in clutching or constant speed ratio phases) or the CVT ratio (if wheel slip occurs in the CVT shifting phase). This simulation is continued till power limited acceleration falls below the traction limited value for that particular time step. Then the simulation is continued as per power limited vehicle performance as discussed in the previous cases.

V. RESULTS AND DISCUSSION

The numerical methodology discussed previously has been applied in the form of a MATLAB program. The program takes vehicle parameters such as vehicle, weight, wheelbase, location of center of gravity, location of center of aerodynamic drag force, the speed ratio range for CVT, the gear ratio for which the simulation has to be performed, engine speeds for idling, engagement and maximum power, rotation inertias of transmission components and system efficiencies as inputs. It also gives user the flexibility to change the straight trajectory length which needs to be traversed by the vehicle before termination of the simulation. Also, the numerical parameters of time step duration are kept variable, so that the desired simulation accuracy may be obtained.

The output of the program that is mainly concerned with this optimization study is the plot of vehicle acceleration with respect to time. However, all the simulation parameters are recorded and plots of speed diagram and vehicle velocity and displacement with respect to time or engine speed may also be plotted.

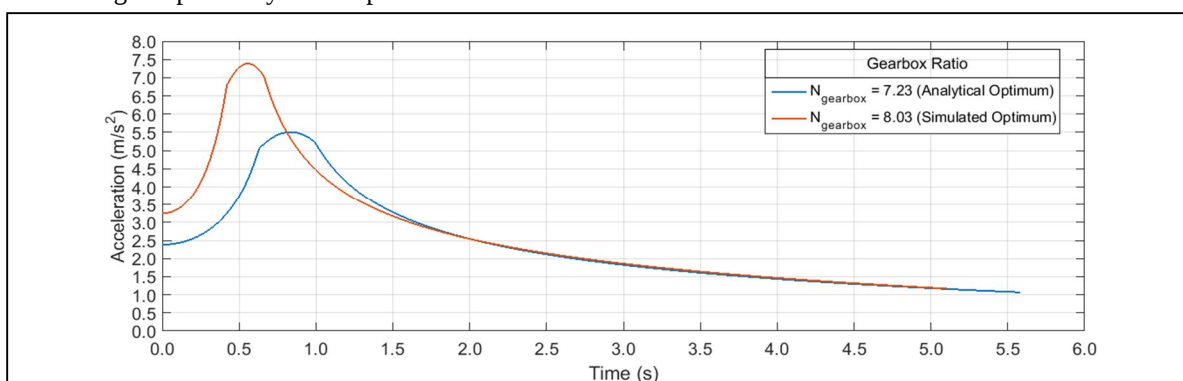


Figure 6: Plot of Acceleration versus Time for different gear ratios.

As it is evident from fig. 6, the analytical calculations estimated a gearbox ratio that does not completely use the available traction. The ratio obtained from the simulation is the most aggressive speed ratio that can be supported by the ground without losing traction. Any speed ratio more aggressive than this would lead to wheel slip and ultimately degrade the acceleration performance and induce directional instability. Such a condition has been avoided for safety considerations. Also, another observation that can be made is that during the shifting phase, the acceleration is almost constant. This is because, power delivery is constant during this phase, and the gear ratio is compensated by CVT speed ratio. In case of a taller ratio, the CVT shifts slowly and vice versa, keeping the overall transmission ratio, and thereby the tractive forces relatively constant. Hence most of the performance improvement is achieved at the start of the simulation.

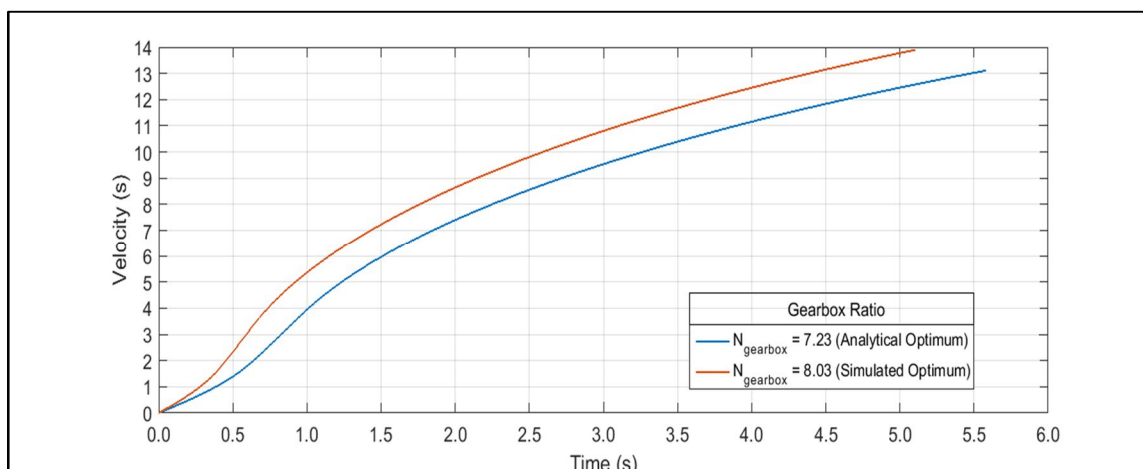


Figure 7: Plot of Velocity versus Time for different gear ratios.

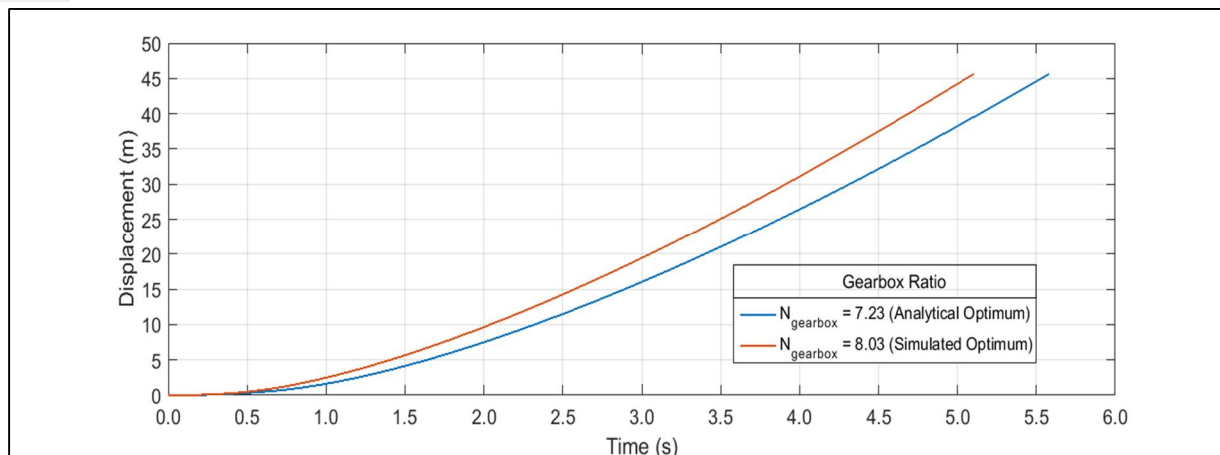


Figure 8: Plot of Displacement versus Time for different gear ratios.

Fig. 7 and 8 illustrate the variation of velocity and displacement with respect to time respectively. It is evident from the graph that although a milder ratio would theoretically achieve a higher top speed for a certain maximum engine rev condition, it takes significantly more time to do so. Hence an aggressive gear ratio proves to be better suited for short sprints and curving tracks, such as those encountered in SAE Baja tracks.

The gearbox ratio has the most significant impact on the top speed of the vehicle and correspondingly on the time and distance required by the vehicle to reach this speed as illustrated by the following table.

Table. I. Variation of vehicle performance parameters with gear ratio.

Gearbox Ratio	Top Speed (m/s)	Distance covered (m)	Time required (s)	150 ft. traversal time
7.23	17.864	161.071	12.851	5.584
8.03	16.084	79.519	7.352	5.107

The table reveals that the vehicle achieves top speed much faster if it were running on the simulated optimum gear ratio. Also, the incurred penalty in terms of maximum achievable speed is reasonably small considering the advantages offered by an aggressive ratio. The time and distance required to achieve top speed is significantly more for the analytical optimum gear ratio as the acceleration of the vehicle approaches zero during the final stages of simulation.

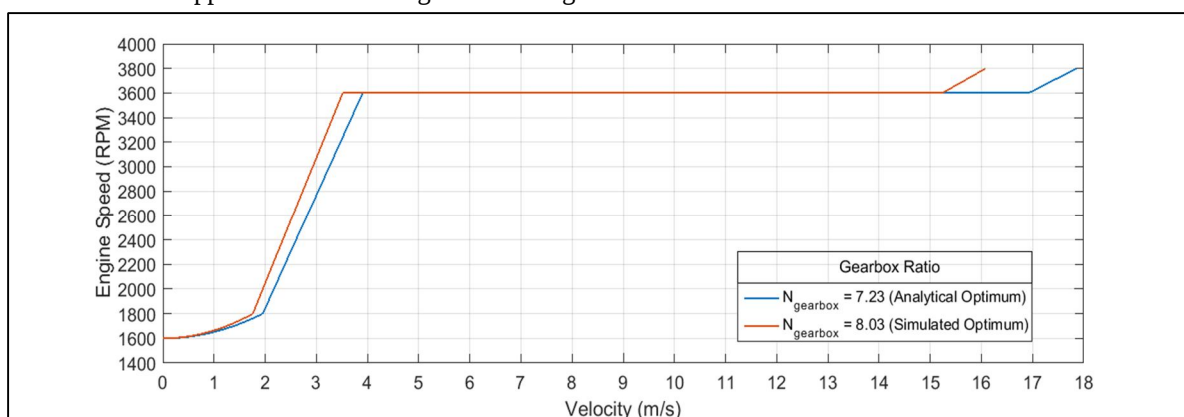


Figure 9: Speed diagram of CVT for different gear ratios.

The plot shown in Fig. 8 shows the speed diagram for analytical optimum and simulated optimum ratio. From the speed diagram it can be observed that as the gearing becomes more aggressive, the graph shifts to the left. Thus, in the pre-engagement and constant ratio phases, the engine speed increases more rapidly with respect to vehicle speed. Also, in the shifting phase, the CVT reaches overdrive ratio first for the most aggressive gearing.

VI. CONCLUSION

As modelling of the wheel slip phase is very crude, the acceleration times predicted by the simulation are not the decisive parameters for gear ratio selection. Also, keeping any gearbox ratio more than that permissible by available traction at the ground results in loss of stability and control of the vehicle. The usefulness of the simulation is in determining the most aggressive ratio beyond which the vehicle starts skidding. This way, the maximum amount of traction is utilized and the best possible acceleration can be obtained. The program accurately considers the loss of torque due to rotational inertia of wheels and transmission components. It also considers the effect of aerodynamic drag on rear axle load. In the vehicle under consideration, the rotational inertia of the wheels is relatively small. This results in only a minor torque loss. Also, the achievable speeds for the vehicle are low, as the engine power is limited to 10 BHP. Owing to these factors, the analytically predicted and simulated optimum ratios are not much far away and their corresponding traversal time for 150 ft. differ by about 8.54%. These results may vary for commercial vehicles.

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