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# Effect of Backordering on lot sizing with Work in Progress Inventory

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**Abstract:** *The notable Inventory Management models, for example, Economic Order Quantity and Economic Production Quantity broadly utilized in Production Environment for Calculation of Optimum parcel size of stock. These Models don't consider the nearness of Shortages in Work In Process stock. Which we endure as a Backorder cost in Real life stock. Due to the deficiencies supposition the stock model become unreasonable. In this paper by adopting delay purchase in WIP we strategy the stock model as an increasingly reasonable and present another scientific model.*

**Keywords:** *Backorder, Lot Size, Optimum, Backorder*

## I. INTRODUCTION

Inventory is the Vital section of Human Life. Inventory is to be saved ample for requirements, each in the structure of price in battery or Medicine in health facility or gasoline in car. For a suitable environment, with nil inventory, patron must have to be comfortable with their demand as shortly as possible. However, inventories are required to fulfill the client desires at that time in actual cases. Therefore, Firms / industries / businesses maintain inventory by using the use of ordering super quantity of substances at awesome time of magnificent marvelous with the focusing of intention each to maximize complete predicted income or limit whole estimated outgoing. To make excessive interest businesses do challenging inspection for better high-quality of objects and avoids shortages or restrict the backordering cost. Subassemblies in the structure of Raw Material are obtained and are processed at the manufacturing plant for in a comparable way processing and convent into closing objects as per consumer requirements.

## II. LITERATURE REVIEW

The ordinary beginning location of the Economic Production Quantity (EPQ) Model can be traced again to May 1918 when E.W. Taft [1] made in extension of Economic Order Quantity (EOQ) Model developed by F.W. Harris in February 1914 [2]. The inventory fashions centered on two sorts of inventories, raw materials and carried out gadgets inventory. However, a 1/3 variety of inventory noted as the work-in-process inventory which moreover effecting the business employer agency techniques of modern-day day industries. They have an effect on of work-in-process stock on most appropriate lot dimension used to be first added with the assumption that the gadget produces ideal pinnacle notch merchandise (Boucher, 1984) [3]. The model cited as crew technological knowledge order extent (GTOQ) used to be as quickly as in distinction with EOQ model and its have an effect on used to be determined by way of numerical computation on the closing lot size. Later Barzoki, Jahanbazi, and Bijari (2011) [4] extended this mannequin for imperfect manufacturing methods with the assumption that redecorate merchandise are one hundred percentage qualified. The developed mannequin was diagnosed as crew technological understanding order extent if radically change is considered (GTOQR). This model used to be moreover in contrast with the EOQ and GTOQ models. Based on numerical computation, results of imperfect merchandise below referred to assumptions had been highlighted. These stock models, Boucher (1984) and Barzoki, Jahanbazi, and Bijari (2011), considered work-in-process inventory and its have an influence on on most really useful lot dimension calculation. Misbah Ullah & Chang W. Kang (2014) [5] prolonged the GTOQR mannequin to crew technological facts order extent remodel with inspection (GTOQIR).

## III. MATHEMATICAL MODELING

### A. List of Notation

- Q production lot dimension per cycle (Amount of volume after backorder satisfied)(number of product devices per cycle)
- QB Backorder Production lot size per cycle (number of product unit per cycle)
- D demand cost of true extremely proper product (unit product per unit time)
- s setup time per cycle (unit time per setup)
- m1 machining time per unit for lot dimension Q in vicinity 1. (unit time per unit product)

- mr machining time per unit for radically change merchandise (unit time per unit product)
- P10 percentage of merchandise rejected as terrible first- rate in section 1
- P11 percentage of merchandise licensed as correct super in phase 1
- P21 percentage of merchandise certified as pinnacle superb in segment 2
- P20 percentage of merchandise rejected as bad fine in part 2
- P1r percentage of merchandise redesign in a position in part 1,  $QP1r=Q(P20+P21)$
- Pb percentage of horrific high-quality merchandise at the provide up of cycle
- Tc cycle time
- Tp total processing time
- T average manufacturing time for every product item
- Cm cost of uncooked fabric per unit (\$/unit of product)
- Cp cost of buy per unit of time (\$/unit of time)
- Cs cost of setup per unit of time (\$/unit of time)
- Ci cost of inspection per unit of time (\$/unit of time)
- Cwip work in method defending price per unit of time (\$/unit of time)
- Ch inventory keeping rate per unit of time (\$/unit of time)
- Ct total fee per unit of time (\$/unit of time)
- I average storage inventory
- W average monetary fee of the WIP stock (\$)
- i inventory defending cost per unit of time (\$/unit of time)
- c average unit value of each product price (unit of money (\$) per unit)
- R rate charged per unit of mobile manufacturing time collectively with all overheads, moving cost, loading/unloading cost, etc.(unit of money (\$) per unit of time)

**B. Cost Calculation**

The model will developed by the cost calculation. All cost will be calculated for the lot size (Q) and Back Order (B). The GTOQIR Model will be extended with the backorder cost.

1) Purchase Cost

$$C_p = \frac{(C_m * Q)}{T_c}$$

2) Setup Cost

$$C_s = \left(\frac{A}{T_c}\right)$$

3) Inspection Cost

$$C_i = \left(\frac{I * QB}{T_c}\right) + \left(\frac{I * Qm}{T_c}\right) + \left(\frac{I * Q * (P20 + P21)}{T_c}\right)$$

4) Backorder Cost

$$C_b = \left[\left\{\frac{(QB * D)}{(QB + Q * (1 - Pb))}\right\} * \{Z\}\right]$$

5) Holding Cost

$$I_n = \left(\frac{1}{2}\right) * \left(\frac{QB + Q * (1 - (P10 + P20)) * T_c}{T_c}\right)$$

6) Work in Process Cost

$$C_{wip} = \left[\left\{\left(\frac{1 * Q * QB * T_p}{2 * T_c}\right) * C_m\right\} + \left\{c * \left(\frac{1 * (QB + Q * (1 - Pb)) * T_p}{2 * T_c}\right)\right\} + \left\{c * \left(\frac{Q * (1 - Pb) * T_p}{2 * T_c}\right)\right\}\right]$$

**C. Developed Model**

After Calculation and putting all equation in Ct we get Ct which is new model GTOQIRB

$$C_t = C_p + C_s + C_i + C_b + C_h + C_{wip}$$

$$C_t = \text{GTOQIRB}$$

$$\text{GTOQIRB} = \left\{\frac{(C_m * Q * D)}{(QB + Q * (1 - Pb))}\right\} + \left\{\frac{(A * D)}{(QB + Q * (1 - Pb))}\right\} + \left\{\left(\frac{I * D}{(QB + Q * (1 - Pb))}\right) * (QB + Q * (1 + P1r))\right\} + \left[\left\{\frac{(QB * D)}{(QB + Q * (1 - Pb))}\right\} * \{Z\}\right] +$$

$$i\left[\left\{\left(\frac{1}{2}\right) * \left(\frac{(F1*Q)+(R*S)+(R*Qb)+(R*I*Qb)}{Q}\right)\right\} * \{(Qb + Q(1 - Pb))\}\right] + i\left[\left\{\left(\frac{1}{2}\right) * \left(\frac{(F2*Q*D)+(S*D)+(QB*D)+(I*D*QB)}{(QB+(Q*(1-Pb)))}\right)\right\} * \{(F1 * Q) + (F1 * QB) + (Q * QB * Cm) + (R * S) + (R * QB) + (R * I * QB) + \left(\frac{R*S*QB}{Q}\right) + \left(\frac{R*QB(Square)}{Q}\right) + \left(\frac{R*I*QB(Square)}{Q}\right)\}\right]$$

#### IV. FUTURE DIRECTION

The look up can be in a similar way extended in endless direction. Few areas have been highlighted right here for shut to future extension and order to make stock fashions as for market trends.

- A. The mannequin will be evaluate with GTOQIR model alongside with numerical example.
- B. Solving by Classical Methods
- C. Using Hessian Matrix for Calculation
- D. To make and exhibit the graphs, that how it behave with higher and lower demand and excessive and low backordering.

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