# Geometrical Construction of Solar Eclipse 

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Abstract: Geometrical Construction of annular solar Eclipse on 26 ${ }^{\text {th }}$ December 2019. In this projection of the solar eclipse assumes that observer is at moon, looking down on earth, viewing the moon's shadow as it passes over the earth disc. The earth to him appears as a plane equal to the moon's horizontal parallax.
Keywords: Elements for computations, Graph, observations from the projection, Results from Graph

## I. INTRODUCTION

Solar eclipse occurs when the moon passes between earth and the sun, thereby totally or partially obscuring earth's view of the sun. This configuration can only occur during a new moon when the sun and moon are in conjunction as seen from the earth.


## A. Types of Eclipse

Depending on what part of the shadow you are located in there are three types of eclipse:

1) Total Eclipse: A total eclipse is where the sun is covered completely by the Moon.
2) Annular Eclipse: An annular eclipse is when the moon covers the sun, but the sun can be seen around the edge of the moon.
3) Partial Eclipse: A partial eclipse is where when only a portion of the sun is blocked by the moon.

## When can eclipses occur?

- Solar eclipses can occur only at new moon.
- Solar eclipses can be partial, total, or annular.

B. Some Definitions

Central solar eclipse:
It is an eclipse during which the central line of the umbra touches the Earth's surface. It is possible,
Though extremely rare, that part of the umbra intersects with the Earth (Thus creating an annular or total eclipse), but not its central line. This is then called a non-central total or annular eclipse.

1) Greatest Eclipse: For solar eclipses, Greatest Eclipse (GE) is defined as the instant when the axis of the moon's shadow cone passes closest to Earth's center. The computation of the duration of the total (or annular) phase at this point is typically done using a smooth edge for the Moon that ignores the effects of mountains and valleys along the lunar limb. For total eclipses, the instant of Greatest Eclipse offers a good approximation (typically $\sim 1-2$ seconds) to the Greatest Duration of totality along the entire eclipse path. The instant of Greatest Eclipse is easily calculated for total, annular and partial eclipses, and is the standard time used for comparing different eclipses with each other. For annular eclipses, the instant of Greatest Duration may occur either near the time of Greatest Eclipse or near the sunrise and sunset for lunar eclipses, Greatest Eclipse is defined as the instant when the moon passes closest to the axis of Earth's shadow.
2) Penumbra: Faint outer shadow; partial eclipse are seen from within this shadow
3) Umbra: Dark inner shadow; total eclipse are seen from within this shadow.
4) Node Point: The moon's orbit is inclined about $5^{\circ} 8^{\prime}$ to earth's orbit around the sun. The points where the lunar orbit intersects the plane of earth's orbit are known as the nodes. The moon moves from south to north of earths orbit at the ascending node, and from north to south at the descending node.
5) Declination: The earth's equator is tilted 23.45 degrees with respect to the plane of the earth's orbit around the sun, so at various times during the year, as the earth orbits the sun, declination varies from $\mathbf{2 3 . 4 5}$ degrees north to $\mathbf{2 3 . 4 5}$ degrees south.


Moon's Parallax- It is defined as an angle subtended at the moon by the earth radius.
6) Greenwich Time (GMT): Universal Time is actually based on the mean sidereal time as measured in Greenwich, England. It's also approximately equal to mean solar time from Greenwich.

## II. CONSTRUCTION OF THE GENERAL ECLIPSE

The projection can be drawn on any reasonable size of blank paper but will be very convenient on big graph paper.
A. STEP-1

Find moon's Horizontal Parallax- sun's Horizontal Parallax
$=0^{\circ} 58^{\prime} 44^{\prime}-0^{\circ} 0$ 8.5'
$=58.6(88 \mathrm{~mm})$
(Take a suitable scale $1 ́=1.5 \mathrm{~mm}$ )
Now draw a circle with radius 88 mm with centre as C . Draw a horizontal line BCH passing through C and representing the diameter of the circle.
B. STEP-2

Through C draw line CDPL perpendicular to HB. This line represents the plane of earth's axis as seen from moon.

## C. STEP-3

Draw another circle with radius equal to
Moon's Horizontal Parallax - sun's Horizontal Parallax = a
Sun's semi-diameter + moon's semi-diameter $=\mathrm{b}$
Now take $\mathrm{a}+\mathrm{b}$
$=0^{\circ} 58^{\prime} 35.5^{\prime \prime}+0^{\circ} 31^{\prime} 48.5^{\prime}$
$=1^{\circ} 3023^{\prime}$
$=90.40$
$=135.75 \mathrm{~mm}$
D. STEP-4

From P take PA and PF each equal to obliquity of eclipse $23^{\circ} 26$ and draw a chord AF with AF as the diameter describing semicircle
ALF.
Point A represents Vernal Equinox, F the Autumn Equinox where as D represents the two tropics.
E. STEP-5

Find the distance of sun from the tropic nearest to it.
$274^{\circ} 655.1^{\prime \prime}-90^{\circ}=184^{\circ} 655.1^{\prime \prime}$
$274^{\circ} 655.1^{\prime \prime}-270^{\circ}=4^{\circ} 655.1^{\prime \prime}$
Longitude of sun is nearest to $270^{\circ}$
Take LT equal to $48^{\circ} 21^{\prime} 12^{\prime}$ and draw TE parallel to LC.
F. STEP-6

Draw CG the axis of moon's orbit so that angle GCE is equal to moon's visible path with the ecliptic.
CG is to the left of CE if node is Ascending.
CG is to the right of CE if node is Descending.
Here, we are calculating for $26^{\text {th }}$ December 2019 solar eclipse which is descending node.
G. STEP-7

Take Cn= Moon's latitude. Here, 44.73 mm . Draw a line which passes through $\mathrm{n} \&$ which is perpendicular to CG. Here line k 1 r m n pq.
This line represents the centre of shadow or moon's path across the disc. Join points Ck, C1, C2, Cq

## H. STEP-8

Take moon's semi-diameter as radius $\left(15^{\prime} 33^{\prime}=23.32 \mathrm{~mm}\right)$ and draw moon's disc centered at points $\mathrm{k} \& \mathrm{q}$.
Take sun's semi-diameter as radius $\left(1615.5^{\prime}=24.38 \mathrm{~mm}\right)$ and draw sun's disc centered at points $1 \& 2$.
I. STEP-9

Moon's hourly motion - Sun's hourly motion $=0^{\circ} 30^{\prime} 24.8^{\prime}=45.61 \mathrm{~mm}$

## III. ELEMENTS FOR COMPUTATIONS

The arguments which are required for plotting (projecting) the annular solar eclipses of 26th December 2019 at the time of new moon are...

| Sr no. | Observations | ${\text { Degree }\left({ }^{\circ}\right)}^{\text {) }}$ | Minitues( ' $)$ | Seconds(") |
| :---: | :--- | :---: | :---: | :---: |
| 1 | Longitude of sun | 274 | 6 | 55.1 |
| 2 | Declination of sun | 23 | 22 | 25.4 |
| 3 | Sun's hourly motion in longitude | 0 | 2 | 32.9 |
| 4 | Sun's horiontal parallax | 0 | 0 | 8.5 |
| 5 | Sun's semi diameter | 0 | 16 | 15.5 |
| 6 | Longitude of moon | 274 | 7 | 31.2 |
| 7 | Moon's hourly motion in longitude | 0 | 32 | 57.7 |
| 8 | Moon's horizontal parallax | 0 | 58 | 44 |
| 9 | Moon's semi diameter | 0 | 15 | 33 |
| 10 | Moon's latitude | 0 | 23 | 36 |
| 11 | Moon's hourly motion in latitude | 0 | 3 | 2.35 |
| 12 | Angle of moon's path with eciptic | 5 | 8 | 42 |
| 13 | Node of moon | Decending node |  |  |

## IV. GRAPH



## V. OBSERVATION FROM THE PROJECTION

| $\mathrm{kl}=54 \mathrm{~mm}$ | $1 \mathrm{~h} 6 \mathrm{~m} \mathrm{3s}$ |
| :---: | :---: |
| $\mathrm{Kr}=122 \mathrm{~mm}$ | $2 \mathrm{~h} \mathrm{42m} \mathrm{35s}$ |
| $\mathrm{Km}=133 \mathrm{~mm}$ | 2 h 43 m 49 s |
| $\mathrm{Kn}=129 \mathrm{~mm}$ | $2 \mathrm{~h} \mathrm{38m} \mathrm{53s}$ |
| $\mathrm{Kp}=203 \mathrm{~mm}$ | $4 \mathrm{~h} 10 \mathrm{~m} \mathrm{3s}$ |
| $\mathrm{Kq}=258 \mathrm{~mm}$ | 5 h 17 m 47 s |


| $\mathrm{kl}=54 \mathrm{~mm}$ | $1 \mathrm{~h} 6 \mathrm{~m} \mathrm{3s}$ |
| :---: | :---: |
| $\mathrm{lr}=75 \mathrm{~mm}$ | $1 \mathrm{~h} 32 \mathrm{~m} \mathrm{23s}$ |
| $\mathrm{rm}=1 \mathrm{~mm}$ | $0 \mathrm{~h} \mathrm{43m49s}$ |
| $\mathrm{mn}=4 \mathrm{~mm}$ | $2 \mathrm{~h} 1 \mathrm{~m} \mathrm{13.9s}$ |
| $\mathrm{np}=74 \mathrm{~mm}$ | 0 h 4 m 55 s |
| $\mathrm{pq}=55 \mathrm{~mm}$ | 1 h 7 m 44 s |


| $\angle \mathrm{kCH}=16^{\circ}$ |
| :--- |
| $\angle \mathrm{CH}=28^{\circ}$ |
| $\angle \mathrm{pCB}=35^{\circ}$ |
| $\angle \mathrm{qCB}=24^{\circ}$ |

## VI. RESULTS FROM GRAPH

A. Time Of Conjuction At Greenwich: 5h 15m 29s

| -k to n | $\begin{aligned} & \text { 5H 15M 29S } \\ & 2 \mathrm{H} 38 \mathrm{M} 53 \mathrm{~S} \end{aligned}$ | 2H 36M 36S | FIRST PENUBRAL CONTACT(P1) |
| :---: | :---: | :---: | :---: |
| +k to 1 | 2H 36M 36S <br> 1H 6M 3S | 3H 42M 39S | FIRST UMBRAL CONTACT(U1) |
| +1 to r | $\begin{aligned} & 3 \mathrm{H} 42 \mathrm{M} 39 \mathrm{~S} \\ & 1 \mathrm{H} 32 \mathrm{M} 23 \mathrm{~S} \end{aligned}$ | 4H 74M 62S | GEOCENTRIC CONJUCTION |
| +r to m | $\begin{aligned} & \hline 4 \mathrm{H} 74 \mathrm{M} 62 \mathrm{~S} \\ & 0 \mathrm{H} 1 \mathrm{M} 13.9 \mathrm{~S} \end{aligned}$ | 5H 16M 16S | GREATEST ECLIPSE |
| $\begin{gathered} +\mathrm{m} \text { to } \mathrm{p} \\ (\mathrm{mn}+\mathrm{np}) \end{gathered}$ | $\begin{gathered} \text { 5H 16M 16S } \\ 0 \mathrm{H} 4 \mathrm{M} 55 \mathrm{~S} \\ 1 \mathrm{H} 31 \mathrm{M} 8.8 \mathrm{~S} \end{gathered}$ | 6H 52M 19.8S | LAST UMBRAL CONTACT(U4) |
| +p to q | $\begin{gathered} \hline 6 \mathrm{H} 52 \mathrm{M} 19.8 \mathrm{~S} \\ 1 \mathrm{H} 7 \mathrm{M} 44 \mathrm{~S} \end{gathered}$ | 8H 0M 3.8S | LAST PENUBRAL CONTACT(P4) |

International Journal for Research in Applied Science \& Engineering Technology (IJRASET) ISSN: 2321-9653; IC Value: 45.98; SJ Impact Factor: 7.429 Volume 8 Issue V May 2020- Available at www.ijraset.com

## Annular Solar Eclipse of 2019 Dec 26



## B. Comparison

| Contact Points | Calculated | According to NASA's <br> Eclipse page |
| :---: | :---: | :---: |
| FIRST PENUBRAL |  |  |
| CONTACT(P1) | 2H 36M 36S | 2 H 29M 43.5S |
| LAST PENUBRAL CONTACT(P4) | 8H 0M 3.8S | 8H 5M 36S |
| FIRST UMBRAL CONTACT(U1) | 3H 42M 39S | 3H 34M 24.2S |
| LAST UMBRAL CONTACT(U4) | 6H 52M 19.8S | 7H 00M 53.6S |

## VII.CONCLUSION

A. The experiment for the determination of values of Penumbra and Umbra has been successfully carried out.
B. The results of the experiment performed by geometrical method are in good agreement with the data which are published on website of NASA.

## VIII. ACKNOWLEDGMENTS

I am highly thankful to my project guide professor B.Y. Thakor, P.G. department of physics, Vallabh Vidhyanagar for providing me necessary guidance and help towards the successful completion of the project. He was always helpful throughout my project and guided me about ways to analyze problems. I am grateful to him for giving me an opportunity to learn something in astronomy during my final year.
My thank are also due to professor P.C Vinodkumar, Head of physics P.G. department, Sardar Patel university, Vallabh Vidhyanagar for assigning project work in the final year.
Last but not the least I would like to thank all those who helped me directly or indirectly in completion of my project.

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