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Cost-effective Numerous Kernel Learning Algorithms using Low-Rank Interpretation

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Abstract: ***Special clustering method is used in our project to make use of spectral graph structure for partition of affinty matrix. Affinity matrix is a weighted adjacency matrix of the data .project explain the effective approach to reduce or minimize the local and global noises. We have used MULTIPLE KERNAL LEARNING (MKL) to extract local and global noises. To solve the optimization method block coordinate descent algorithm is used in this project. It is Unsupervised Robust multiple kernal lerning approach Unsupervised approach is done manually so it will decrease the chance of inaccuracy. It does not work on the preset condition. work accordingly given condition. It sets the fuzziness by MKL algorithm . In this paper we will analysis local and global noises and charcterized them accordingly. As we are proposing it manually then result will be valid as compared to supervised approach. We are using numerical values, function(f) ,graph to extract global and local noises from matrix. After extracting local and global noises we can remove corrupted data. We have used total 14 datasets to evaluate the effectiveness of our method. Simultaneously, we learned a consensus kernel by minimizing the disagreement over cleaned kernels.***
Keywords- Unsupervised robust multiple learning, Affinity matrix, Block coordinate descent algorithm.

I. INTRODUCTION

Kernel-based clustering algorithms, which include kernel k-means, have the potential to capture the non-linear inherent shape in lots of real global information sets and thereby commonly attain higher clustering performance than linear partition methods. In real global packages, we are able to construct numerous kernels with the aid of applying extraordinary kernel capabilities. However, the overall performance of clustering quite depends on the choice of kernels. Unfortunately, it's far nevertheless a undertaking to decide appropriate one in all an in depth range of viable kernels for the given information and task in advance. It is more difficult especially in the unsupervised learning tasks such as clustering, because of the absence of labels. To conquer this difficulty, many unsupervised multiple kernel mastering strategies have been proposed, which aim to learn a consensus kernel from a person-defined pool of kernels. Conventional unsupervised a couple of kernel studying strategies learn a consensus kernel by way of linearly combining a hard and fast of candidate kernels. For instance, furnished a multi-view spectral clustering approach which linearly combined spectral embedding to get the final clustering.

It proposed a localized a couple of kernel k means technique for cancer biology applications. Liu et. proposed a multiple kernel gaining knowledge of approach by using mastering the optimal neighborhood for clustering. The above techniques concentrate on combining all candidate kernels, whereas ignore the robustness of the strategies. However, in real world packages, the kernels are frequently infected by using noises. For instance, since the unique information may incorporate noises and outliers, the kernel constructed with these information will also be infected. In addition, despite the fact that the statistics is clean, incorrect kernel features might also introduce noises. To alleviate the effort of noises, currently, some strong a couple of kernel getting to know techniques are proposed. These techniques recognition on the noises resulting from the corrupted instances, while cannot capture the noises caused through kernel features nicely. Note that, a few more than one kernel studying methods assign large weight on the extra suitable kernels can seize the noise brought on by means of kernel functions to some extent. However, in these strategies, the burden is imposed on all elements of the kernel matrix, and it is a bit too rough .For example, some inappropriate kernels May have a totally low weight in those methods, which means all elements which includes the useful parts inside the kernel matrix will share the equal low weight and could no longer be useful to the kernel getting to know. To take care of noises greater comprehensively, in this paper, we suggest a singular Local and Global De-noising Multiple Kernel Learning technique. We examine that the kernel matrix might also comprise styles of noises: one is because of infected instances, and the other is due to beside the point kernel functions. Figures indicates the unique facts set and affords an awesome Gaussian kernel, and the blue shade method the kernel fee is small. For the first kind of noise, once an example is contaminated by means of noises, both the corresponding row and column of the kernel matrix could be also contaminated.

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Since this kind of noises only influences a part of kernel matrix (i.e handiest one row and one column of the kernel matrix), we call them neighborhood noises. We see that the local noises have a few Sparsity. For the second one kind of noises, since the beside the point kernel capabilities may also have an effect on all times most of the kernel values. In this paper, we take these two kinds of noises into consideration, and explicitly extract them to recover easy kernels for a couple of kernel getting to know. For the 2 forms of noises, we first stack noise matrices into tensors and then analys their systems and design regularized phrases to symbolize them, respectively. In our method, we integrate the de-noising and a couple of kernel fusion into a joint gaining knowledge of framework, for the cause that, on one hand, shooting the noises may additionally improve the kernel learning ,and on the other hand ,learning a consensus kernel can also guide to stumble on noise more correctly. Since the goal feature is a joint getting to know framework and contains complicated regularized terms, the optimization is difficult. To resolve it correctly, we first loosen up the goal function and then present a block coordinate descent scheme to optimize it. Atlast, we compare our method with the state of-the-artwork more than one kernel clustering strategies on benchmark statistics sets, and the experimental consequences exhibit the effectiveness of our approach.

II. EXISTING SYSTEM

The present systems are:

A. Cross validation
B. Feature Selection

Cross-validation is a resampling manner used to assess gadget gaining knowledge of models on a limited data pattern. The procedure has a single parameter called k that refers back to the wide variety of corporations that a given information pattern is to be break up into. As such, the method is often known as ok-fold cross-validation.

Feature selection is an vital trouble in system getting to know encouraged with the aid of concerns of elimination of noisy, high-priced and redundant functions, model compression for mastering and predicting on a price range, version interpretability, and so on. In many real international applications, one needs to determine the whole characteristic choice path. i.e. The variation in prediction accuracy as the fraction of decided on functions is numerous from null to team spirit, with a purpose to determine the maximum viable working factor at the route in the context of the given software.

1) Drawbacks of Existing System
a) It is effectively caught into degenerate neighborhood minima when the models of bunches are badly instated.
b) The real number of bunches must be given ahead of time.
c) The Cross Validation prompts higher variety in the testing model
d) The approval set blunder may tend to
e) Overestimate the test blunder for the model fit on the whole informational collection.

III. PROPOSED SYSTEM

Multiple Kernel Learning (MKL) tries to address this issue by learning kernal from training data. Specifically, it centers around how the kernel can be learnt as a linear combination of given base kernels. The proposed system can handle two kinds of noises:

A. Caused by Contaminated Instances
B. Caused by inappropriate kernel functions

Once an instance is contaminated by noises, both the corresponding row and column of the kernel matrix will be also contaminated, since this kind of noises only affects a part of kernel matrix, it is called as local noise.
The inappropriate kernel functions may affect all instances; therefore, it is called as global noise.
The proposed system integrates the de-noising and multiple kernel fusion into a joint learning framework, for the reason that, on one hand, capturing the noises may improve the kernel learning, and on the other hand, learning a consensus kernel may guide to detect noise more accurately.

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IV. ARCHIECTECTURE

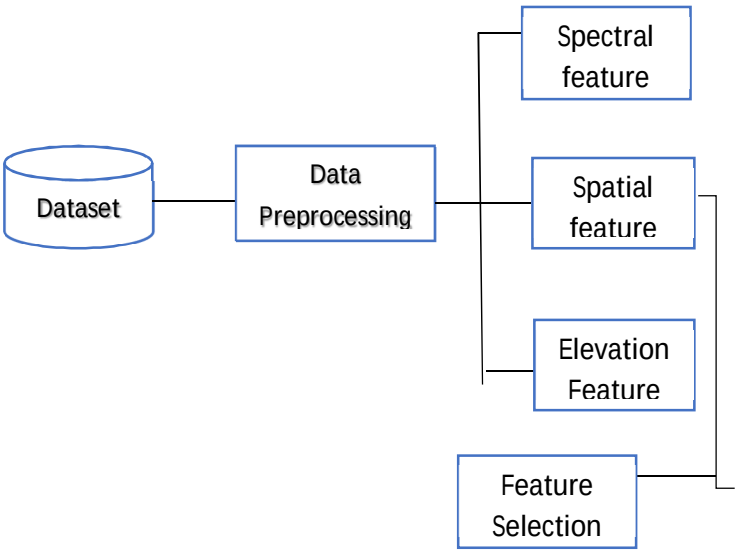

Fig no 4.1

V. RELATED WORK

Multiple kernel learning has been actively studied. Based on the availability of class labels, more than one kernel learning may be classified into two lessons: Supervised algorithms and unsupervised strategies. In supervised gaining knowledge of, labels of times are available, which may be beneficial to analyze a consensus kernel from more than one kernels. For example, integrated radius data into multiple kernel learning to improve the kernel learning performance; extended extreme getting to know system to multiple kernel gaining knowledge of leading to a more than one kernel extreme gaining knowledge of gadget. Although supervised more than one kernel gaining knowledge of has been notably studied, unsupervised algorithm is greater difficult because of the absence of class labels. In unsupervised studying, some methods extend single kernel based clustering technique into a couple of kernel placing. For example, Zhao et al. proposed a more than one kernel fuzzy clustering approach via introducing a matrix-precipitated regularization; Kang et al. furnished a self-weighted multiple kernel getting to know set of rules and carried out it to a graph-primarily based clustering approach.

Since kernel k-means is a famous clustering method, many unsupervised a couple of kernel getting to know techniques were developed in the frame work of it. For example, Tzortzisetal advanced weighted multiple kernel k-means and multiview spectral clustering, respectively. Yu et al. proposed a multiple kernel k-means in which the kernel combinational coefficients are optimized automatically. Huang et al presented a couple of kernel k-means approach and prolonged it to fuzzy k-means. Liu et al proposed a multiple kernel ok-manner method which focused on integrating incomplete kernels after which they prolonged it to multi-view clustering. Recently, Liu et al improved the work in for efficiency consideration. Zhu et al proposed a a couple of kernel k-method for incomplete kernels which took the nearby structure among statistics into attention. Due to the connection between kernel okay-way and spectral clustering, the latter has also been extended to deal with multiple kernels. Kumar et al present Edaco - training technique for multi-view spectral clustering by using bootstrapping the clustering of different views. They also proposed two co-regularization based strategies for multi-view spectral clustering by enforcing the clustering hypotheses on different views to believe every other. Huang et al aggregated kernels with distinctive weights right into a unified one for spectral clustering. By resorting to the spectral approach, Gönen et al also proposed to clear up a a couple of kernel okay-manner associated with two-layer weights. Similar to [10], Liu et al first provided a a couple of kernel k-means approach which considered the kernel correlations,and then depending on the effects in, they switch the kernel okay-way to spectral methods and gain the clustering consequences from eigenvalue decomposition. Liu et al proposed a multiple kernel gaining knowledge of technique to enhance the representability of the top-quality kernel and enhance the negotiation between kernel getting to know and clustering. The above methods do no longer don't forget the noises at the kernels. To alleviate the effort of noises,some robust multiple kernel getting to know strategies are proposed. Xia et al. proposed a strong multi-view spectral clustering method which learns a consensus matrix from a hard and fast of probabilistic transition matrices. Note that, they extracted the sparse noises on the transition matrices rather than the kernel

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matrix. However, the noises at the kernel matrix are frequently more sophisticated so that as parse constraint is too simple to signify the complicated noises. Different from Du et al and Zhou et al tried to symbolize the noises on the kernel matrices directly. Du et al gift a strong a couple of kernel k-approach technique the usage of 2,1 loss. Zhou et al extracted the structural noises as a result of corrupted instances. Nevertheless, these techniques recognition at the noises caused by the corrupted times, while cannot seize the noises brought on with the aid of kernel features nicely.

VI. NOTATIONS AND PRELIMINARIES

Since this paper will contain some tensor and matrix operations, we first introduce some important notions and preliminaries about them in this phase.

An m × n matrix is denoted as M ∈ Rm×n, and its(i,j)-th element is denoted as Mij. A tensor of order N is denoted as T ∈ RI1×···×IN. The element of T is denoted as Ti1···iN. The mode-n vectors of the tensor T are the In dimensional vectors obtained from T by varying index in while keeping the others fixed. The unfolding matrix T(n) = unfoldn(T) ∈ RIn×(I1×···×IN) is composed by taking the mode-n vectors of T as its columns. The unfolding matrices along the n-th mode can be transformed back to the tensor by T = foldn(T(n)). The mode-n product of a tensor T ∈ RI1×···×In×···×IN by a matrix M ∈ RJn×In, denoted by T ×n M, is an N-order tensor C ∈ RI1×···×Jn×···×IN, with entries: Ci1···in−1jnin+1···iN = Pin Ti1···in···iN Mjnin. It is easy to verify that unfoldn(T ×n M) = MT(n). (1) The Frobenius norm of the matrix M is denoted by ||M||F and ||M||F. Similarly, the Frobenius norm of the tensor T is denoted by ||T||F. ||T||F0 is the `0 norm of T which means the number of non-zero elements in T. Given the tensor T, its Tucker decomposition [27] can be denoted by :

T = S×1 U1 ×2 ···×N UN

where S ∈ Rr1×···×rN is called the core tensor, and Ui ∈ RIi×ri is composed by the ri orthogonal bases along the i-th mode of T.

VII. LOCAL AND GLOBAL DE-NOISING MULTIPLE KERNEL LEARNING

In this segment, we present the framework and algorithm of our local and global de-noising a couple of kernel getting to know.

A. Formulation

Given a data set with n instances, we construct m kernels K(1),··· ,K(m) which are n × n matrices. The task of multiple kernel learning is to learn a consensus kernel matrix K∗ ∈Rn×n from K(1),··· ,K(m). As introduced before, the candidate kernels K(1),··· ,K(m) may be contaminated by two kinds of noises: local noises, the noises only appear in a small amount of elements of the kernel matrix and is often induced by outliers or corrupted instances; global noises, the noises which appear in most of the elements of the kernel matrix, and is often induced by inappropriate kernels. To obtain the clean consensus kernel, we will handle these two kinds of noises respectively. For the local noises, we know that, if the j-th instance is corrupted with noises, both the j-th row and the j-th column of the kernel matrix are simultaneously contaminated. To extract this kind of noises,we use arow-wise sparse matrix E(i) ∈Rn×n to capture the noises on the rows of the i-th kernel. The transpose E(i) T is a columnwises parse matrix which captures the noises on the columns. As a result, the symmetric matrix E(i) + E(i)T denotes the local noises on the i-th kernel.

For the global noises, we additionally introduce m noise matrices

$\hat{}$ $E^{(i)} \in R^{n*n}$ to seize them. Since those noises are caused by kernel features, the noise matrices of the kernels calculated by way of the similar kernel functions can have the similar shape (see Figure 1(e) and Figure 1(f)). To characterize the similarity, we stack the m noise matrices $\hat{}$ $E^{(i)}$ into an n ×n × m tensor $\hat{}$ E. Since the rank of a tensor reflects the relativity of all the slices inside the tensor, we make the noise tensor $\hat{}$ E low rank to symbolize the similarity of m noise matrices.

Up to now, we introduce a few noise matrices and noise tensor to capture the local and worldwide noises. Then we are able to introduce the formulation of our multiple kernel gaining knowledge of method. Since we use a tensor to capture the global noises, for the simplicity of notation, we also stack the candidate kernels into an n × n × m tensor K, where the i-th slice of K is $K^{(i)}$. Similarly, we stack $E^{(i)}$s into a E tensor and denotes $E^{(T)}$ as the tensor obtained by means of stacking $E^{(i)T}$s. At ultimate, we replicate the consensus kernel matrix K^* m instances and also stack the min to an n ×n ×m tensor K^* where each slice of it's miles K∗. Since E +ET denotes the nearby noises and $\hat{}$ E denotes the global noises, the cleaned kernel tensor may be characterized by K−(E +ET)− $\hat{}$ E, i.e., the cleaned kernels are received by subtracting the noises form the candidate kernels. To research the consensus kernel, we want to reduce the disagreement among the consensus kernel and all of the wiped clean kernels. So we limit the following method

$$\min_{k^*,E,\hat{E}} \quad \| K - (E + E^T) - \hat{E} - K^* \|_f^2 + \lambda_1 \Omega_1(E) + \lambda_2 \Omega_2(\hat{E}),$$

$$\text{s.t. } K^* = K^{*T}, K^* \geq 0.$$

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Wherein t is a tradeoff parameter and is ready to 10 as advised in [28].
Taking Ω (•) and Ω (•) into Eq.(3), we get the objective
Up to now, we introduce some noise matrices and noise 1 2 tensor to capture the neighborhood and global noises. Then we can introduce the formulation of our more than one kernel learning feature of our neighborhood and international de-noising more than one kernel mastering approach technique. Since we use a tensor to seize the worldwide noises,
Up to now, we introduce some noise matrices and noise tensor to seize the nearby and international noises. Then we can introduce the system of our more than one kernel getting to know approach. Since we use a tensor to capture the worldwide noises, for the simplicity of notation, we additionally stack the candidate kernels into an n × n × m tensor K, where the i-th slice of K is K. Similarly, we stack Es into a tensor E and denotes ET because the tensor received by using stacking E(i)T s. At final, we replicate the consensus kernel matrix K∗ m instances and also stack themin toan n×n×m tensor K∗ where each slice of it's far K∗. Since E +ET denotes the local noises and ˆ E denotes the worldwide noises, the cleaned kernel tensor may be characterised by K−(E +ET)− ˆ E, i.e., the wiped clean kernels are received by using subtracting the noises form the candidate kernels. To examine the consensus kernel, we desire to minimize the confrontation among the consensus kernel and all the wiped clean kernels. So we decrease the following system:

$$\text{Min} \ \| K-(E+ET)-\hat{E}-K* \|+ {}_{\Omega 1}(E) + \lambda 2\Omega 2(\hat{E}),$$
$$K*,E,\hat{E}$$
$$\text{s.t .} \ K* = K*T, K*>/0. \quad (3)$$

Where the constraints make sure that the consensus kernel K∗ is a valid kernel matrix which is symmetric and positive semi definite. The regularized time period $\Omega_1(E)$ makes the nearby noise matrix row sparse and $\Omega_2(\hat{E})$ makes the global noise tensor low rank. and λ_2 are two balancing parameters. Figure 2 illustrates the framework of our approach. Now we introduce the regularized phrases. For the $\Omega_1(\cdot)$, for the reason that we wish to make $E^{(i)}$ row sparse, we observe the well-known `2,1-norm on the E, which leads to $\Omega_1(E) = \sum_{i=1}^{m} \| E^{(i)} \|_{2,1.}$

For the low rank regularized term$\Omega_2(\cdot)$,we use the similar regularized term as in [28], [29]. In more information, given the tensor $\hat{E} \in R^{n*n*m}$ its Tucker decomposition is written as follows:

$$\hat{E} = S *_1 U_{1*2} U_{2*3} \ldots\ldots\ldots\ldots (4)$$

where $S \in R^{r1*r2*r3}$, $U1 \in R^{n*r1}$, $U2 \in R^{n*r2}$, and $U3 \in .R^{m*r3}$

ri(i = 1,2,3) is the number of orthogonal bases along the i-th mode of ˆ E. To make the tensor ˆ E low rank, we wish its core tensor as sparse as possible, i.e., we

minimize$\|S\|_0$. Besides constraining the sparsity of the core tensor, we should also constrain the size of the core tensor. Considering the unfolding matrix ˆ E(i) = $\text{unfold}_i(\hat{E}) \in {}^{Ii*(I*....*I*)}$ size of core tensor can be constrained byQ3 i=1 rankˆ E(i)according to [28], [29]. To sum up, the low rank term in our formulation can be defined as follows:

$$\Omega_2(\hat{E}) = \|S\|_0 + t \sum_{i=1}^{3} \pi \, \text{rank}(\hat{E}_{(i)}) \ldots\ldots..5$$

where t is a tradeoff parameter and is set to 10 as suggested in [28]. Taking Ω1(·) and Ω2(·) into Eq.(3), we get the objective function of our local and global de-noising multiple kernel learning method:

$$\min \quad \| K-(E+E^t)-\hat{E}-K^* \|_f^{2} + \lambda_1 \sum_{i=1}^{m} \|E^{(i)}\|_{2,1}$$
$$k^*,E,\hat{E}$$
$$+\lambda_2(\| s\|_0 + t \prod_{i=1}^{3} rank(\hat{E}_{(i)})),$$
$$\text{s.t.} \ K* = K*^{T},K* \geq 0.$$

Note that the important thing of our method is the express characterization of the neighborhood noises E+ET and the worldwide noises E,which make sit more robust .By optimizing Eq.(6),we can de-noise and research the consensus kernel jointly.

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B. Optimization

In this we tell how to optimize eqn (6).

1) Relaxation: Note that the L0-norm and rank norm Eq.(6) are non convex and irregular, and make it difficult to illuminate. We along these lines loosen up them as a log-aggregate structure to disentangle the advancement. Rather than advancing Eq.(6) straight forwardly, we optimize the following relaxation problem:

Min $\|K - (E+E^T) - \hat{E} - K^*\|_F^2 + \lambda_1 \sum_{i=1}^{m} \|E^{(i)}\|_{2,1}$

$K^*, E, \hat{E}$

$+\lambda_2(P_2(S)+t\prod_{i+1}^{3} P_2(\hat{E}_{(i)}))$,

s.t. $K^* = K^{*T}$, $K^* \geq 0$……..(7)

where $P_1(\mathcal{S}) = \sum_{i_1,i_2,i_3} \log\left(\frac{|S_{i_1 i_2 i_3}|+\epsilon}{\epsilon}\right)$ is the approximation of l_0-norm on S where S_{i1i2i3}s are all elements in S and E is a small constant (2^{-52} as the default value in Matlab. $P_2\left(\hat{\mathbf{E}}_{(i)}\right) = \sum_j \log\left(\frac{\sigma_j(\hat{\mathbf{E}}_{(i)})+\epsilon}{\epsilon}\right)$ where $\sigma_j\left(\hat{\mathbf{E}}_{(i)}\right)$ denotes the *j*-th singular value of $\hat{\mathbf{E}}_{(i)}$.

It is easy to verify that $P_2(\cdot)$ approximates the rank norm. We present a block coordinate descent to optimize Eq.(7), that is we optimize the objective w.r.t. one variable while fixing other variables.

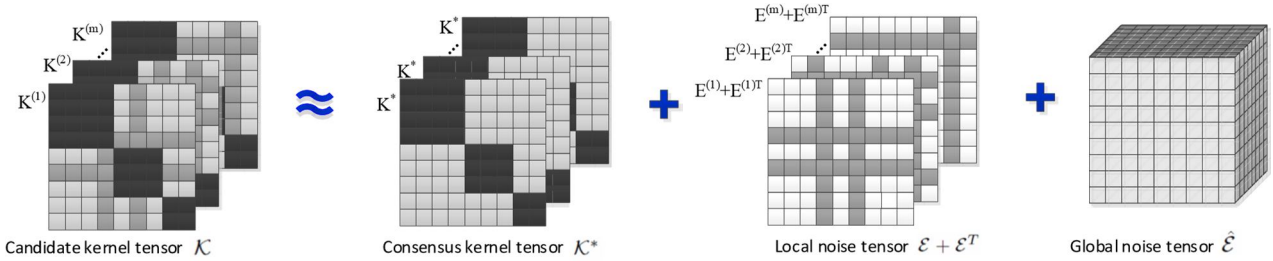

Fig 7.1. Framework of Method

2) Optimize $\hat{E}$

$$\min_{\mathcal{S},\mathbf{U}_i} \quad \|\mathcal{A} - \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3\|_F^2 \quad \text{.....(8)}$$
$$+\lambda_2\left(\mathrm{P}_1(\mathcal{S}) + t\prod_{i=1}^{3}\mathrm{P}_2\left(\hat{\mathbf{E}}_{(i)}\right)\right)$$
$$s.t. \quad \mathbf{U}_i^T\mathbf{U}_i = \mathbf{I}, \quad i = 1,2,3.$$

$\mathcal{A} = \mathcal{K} - (\mathcal{E} + \mathcal{E}^T) - \mathcal{K}^*$.

To solve Eqn(8), we introduce 3 auxiliary tensors $\mathcal{M}_i$(i = 1,2,3) and observe Alternating Direction Method of Multipliers (ADMM) [30] to optimize.

Rewrite Eq.(8) as following equivalent formula:

$$\mathcal{Q} = \mathcal{O} \times_1 \mathbf{U}_1^T \times_2 \mathbf{U}_2^T \times_3 \mathbf{U}_3^T$$

(9)

$$\min_{\mathcal{S},\mathbf{U}_i,\mathcal{M}_i} \quad \|\mathcal{A} - \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3\|_F^2$$
$$+\lambda_2\left(\mathrm{P}_1(\mathcal{S}) + t\prod_{i=1}^{3}\mathrm{P}_2 \quad \mathbf{M}_{i(i)}\right)$$
$$s.t. \quad \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 = \mathcal{M}_i, \ \mathbf{U}_i^T\mathbf{U}_i = \mathbf{I}$$

where $\mathbf{M}_{i(i)}$ = unfold$_i$(M_i). The augmented Lagrangian function of Eqn. (9) is:

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$$L = \|\mathcal{A} - \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3\|_F^2 \quad \text{.....(10)}$$
$$+\lambda_2 \left(\mathrm{P}_1(\mathcal{S}) + t \prod_{i=1}^{3} \mathrm{P}_2 \ \mathbf{M}_{i(i)}) \right)$$
$$+ \sum_{i=1}^{3} \langle \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 - \mathcal{M}_i, \mathcal{P}_i \rangle$$
$$+ \sum_{i=1}^{3} \frac{\mu}{2} \|\mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 - \mathcal{M}_i\|_F^2$$

where P_is are Lagrange multipliers, μ is a positive scalar, and h·,·i denotes the inner production. Then we introduce how to solve S, $\mathbf{U}_i$, M_i and update P_i for i= 1,2,3.

Solving S. When optimizing S with other variables fixed, we rewrite Eqn.(10) as:

$$\min_{\mathcal{S}} \quad \|\mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 - \mathcal{O}\|_F^2 + b\mathrm{P}_1(\mathcal{S}). \quad (11)$$

where $\mathcal{O} = \frac{1}{2+3\mu} \left(2\mathcal{A} + \mu \sum_{i=1}^{3} \mathcal{M}_i - \sum_{i=1}^{3} \mathcal{P}_i \right)$, and $b = \frac{2\lambda_2}{2+3\mu}$. Since for any tensor D and any Orthogonal matrix **U**

where $\mathbf{U}^T\mathbf{U} = \mathbf{I}$, we have

$$\|\mathrm{D} \times_i \mathbf{U}\|_F^2 = \|\mathrm{D}\|_F^2 \text{.....(12)}$$

by mode-i producting $\mathbf{U}_i^T$ on each mode we can rewrite eqn(11) as eqn(13) that is:

$$\min_{\mathcal{S}} \quad \|\mathcal{S} - \mathcal{Q}\|_F^2 + b\mathrm{P}_1(\mathcal{S})$$

Taking P1(.) into in and setting the derivative of it w.r.t. $S_{i1,i2,i3}$ to 0, we get closed form solution:, where $D_{b,E}(\cdot)$ is the thresholding operator defined as:

$$\mathcal{S} = \mathrm{D}_{b,\epsilon}(\mathcal{Q})$$

$$\mathrm{D}_{b,e}(x) = \begin{cases} \sin(x) = \left(\frac{c1+\sqrt{c2}}{2}\right) & c2 > 0 \\ 0, & c2 \le 0 \end{cases} \quad \text{.....(14)}$$

where $c_1 = |x| - E$ and $c_2 = c_1^2 - 4(b - E|x|)$

On solving $\mathbf{U}_i$. After optimizing $\mathbf{U}_1$ with other variables, we will optimize the subproblem: $\min \quad \|\mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 - \mathcal{O}\|_F^2 \quad s.t. \quad \mathbf{U}_1^T\mathbf{U}_1 = \mathbf{I}$ (15)

by unfolding the Frobenius norm, we get:

$$\min_{\mathbf{U}_1} \quad \|\mathcal{S} \times_1 \mathbf{U}_1 \ _2\mathbf{U}_2 \ _3\mathbf{U}_3 - \mathcal{O}\|_F^2$$
$$= \min_{\mathbf{U}_1} \quad \|\mathrm{S} \times 1\, \mathbf{U}1 \times 2\, \mathbf{U}2 \times 3\, \mathbf{U}3\|_F^2$$
$$- 2 \langle \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3, \mathcal{O} \rangle$$

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$$= \max_{\mathbf{U}_1} (S \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3, O) \quad (16)$$

The second equality is because that we have

$$\|\mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3\|_F^2 = \|\mathcal{S}\|_F^2 \quad (17)$$

If $\mathbf{U}_i$ (i = 1,2,3) is orthogonal according to Eq.(12).

Due to Eq.(1), we have

$$\text{unfold}_1 (S \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3) = U_1 \text{unfold}_1 (S \times_2 U_2 \times_3 U_3). \quad (18)$$

Therefore, we can rewrite Eq.(15) as:

$$\max_{U_1} (B_1, U_1), \quad s.t. \quad \mathbf{U}_1^T \mathbf{U}_1 = I \quad \ldots\ldots\ldots\ldots\ldots\ldots (19)$$

where $B_1 = O_{(1)} (\text{unfold}_1 (S \times_2 U_2 \times_3 U_3))^T$. Eq.(19) can be solved by the following Theorem.

Theorem 1. *Let the Singular Value Decomposition (SVD) of* B_1 *be* $B_1 = L\Sigma R^T$, *then the optima of Eq.*(19) *is* $U_1 = LR^T$.

Proof. According to Von Neumanns trace inequality, we have $tr(\mathbf{B}_1 \mathbf{U}_1^T) \leq tr(\mathbf{\Sigma})$. So we get

$$\langle \mathbf{B}_1, \mathbf{U}_1 \rangle = tr(\mathbf{B}_1 \mathbf{U}_1^T) = tr(L\Sigma R^T \mathbf{U}_1^T)$$
$$= tr(\mathbf{\Sigma} \mathbf{R}^T \mathbf{U}_1^T \mathbf{L}) \leq tr(\mathbf{\Sigma}) \quad (20)$$

If $tr(\cdot)$ is the trace of a matrix. Therefore, (B_1, U_1) takes the maximum value when $R^T \mathbf{U}_1^T \mathbf{L} = I$, which means $U_1 = LR^T$.

For performance attention, we use the randomized truncated SVD [31] all through this paper. The optimization of U2 and U3 is similar.

Solving M_i. When optimizing M_1 with other variable fixed, we need to optimize the following formula:

$$\min_{\mathcal{M}_1} \|\mathcal{M}_1 - \mathcal{F}\|_F^2 + a P_2(\mathbf{M}_{1(1)}) \quad (21)$$

where $\mathcal{F} = \mathcal{S} \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 + \frac{1}{\mu}\mathcal{P}_1$ and $a = \frac{\lambda}{\frac{2}{\mu} 2t} P_2(\mathbf{M}_{2(2)}) P_2(\mathbf{M}_{3(3)})$.

Observe that Eq.(21) is similar to Eq.(13), we use the similar method to solve it. First, we get $\mathbf{F}_{(1)}$ by unfolding F by the mode-1, and calculate its SVD decomposition $\mathbf{F}_{(1)} = \mathbf{V}_1 \text{diag}(\sigma_1, \cdots, \sigma_n) \mathbf{V}_2^T$. Then we construct diagonal matrix $\mathbf{\Sigma}_M = \text{diag}(D_{a,\epsilon}(\sigma_1), \cdots, D_{a,\epsilon}(\sigma_n))$, where $D_{a,\epsilon}(\cdot)$ is the thresholding operator defined before. At last, we calculate $M_1 = \text{fold}_1(\mathbf{V}_1 \mathbf{\Sigma}_M \mathbf{V}_2^T)$. The calculation of M_2 and M_3 is similar.

We update the Lagrange multipliers P_i (i = 1,2,3) as follows:

$$P_i = P_i + \mu(S \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3 - M_i) \quad (22)$$

and update $\mu = 1.2\mu$.

After using the ADMM algorithm, we obtain $\hat{E} = S \times_1 \mathbf{U}_1 \times_2 \mathbf{U}_2 \times_3 \mathbf{U}_3$. Since the kernel matrix is symmetric, we wish the noise matrix on the kernel is also symmetric.

So we get $\hat{\mathbf{E}}^{(i)}$s as m slices of $\hat{E}$, and update $\hat{\mathbf{E}}^{(i)} = \left(\hat{\mathbf{E}}^{(i)} + \hat{\mathbf{E}}^{(i)T}\right)/2$. Finally, we stack them back to $\hat{E}$.

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3) Optimize E: When K* and Ê are fixed, Eq.(7) can be decoupled into *m* independent subproblems, where each subproblem involves only one $E^{(i)}$. Consider the *i*-th one:

$$\min_{(i)} \left\|\mathbf{G} - \mathbf{E}^{(i)} - \mathbf{E}^{(i)T}\right\|_F^2 + \lambda_1 \left\|\mathbf{E}^{(i)}\right\|_{2,1} \quad (23)$$

where $G = K^{(i)} - K^* - \hat{E}^{(i)}$. It is easy to verify that G is symmetric.

We introduce a diagonal matrix H, where its *j*-th diagonal element is $\frac{1}{2\left\|E_j^{(i)}\right\|_2}$, and $\left\|E_j^{(i)}\right\|_2$ is the l_2-norm of the *j*- th row of $E^{(i)}$.

Then we try to minimize the auxiliary function:

$$\min_{(i)} \left\|\mathbf{G} - \mathbf{E}^{(i)} - \mathbf{E}^{(i)T}\right\|_F^2 + \lambda_1 tr\left(\mathbf{E}^{(i)T}\mathbf{H}\mathbf{E}^{(i)}\right). \quad (24)$$

By setting its derivative w.r.t. $E^{(i)}$ to zero, we obtain

$$(I + \lambda_1 H)E(i) + E(i)T = GT \quad (25)$$

Denote H_{jj} as the (*j*,*j*)-th element of H, $E_{jk}^{(i)}$ as the (*j*,*k*)th element in $E^{(i)}$, and $G_{jk}^{(i)}$ as the (*j*,*k*)-th element in G.

Considering the (*j*,*k*)-th element and (*k*,*j*)-th element on both sides of Eq.(25), we obtain

$$\begin{aligned} &(1 + \lambda 1 H^{(i)}_{jj})E^{(i)}_{jk}) + E^{(i)}_{kj} = G^{(i)}_{jk} \\ &(1 + \lambda 1 H^{(i)}_{kk})E^{(i)}_{kj}) + E^{(i)}_{jk} = G^{(i)}_{kj} \end{aligned} \quad (26)$$

Since G is symmetric, we can get the result by solving Eq.(26) as:

$$E_{kj}^{(i)} = \frac{H_{jj}^{(i)} G_{kj}^{(i)}}{\lambda_1 H_{kk}^{(i)} H_{jj}^{(i)} + H_{kk}^{(i)} + H_{jj}^{(i)}}. \quad (27)$$

Theorem 2. *Applying Eqn.*(27) *to update* E *monotonically decreases the objective function Eqn.*(23).

Proof. The proof is similar as that in eq.[32].

4) Optimize K*

When E and Ê are fixed, Eq.(7) can be rewritten as:

$$\min_{K^*} \|J - K^*\|_F^2 \quad (28)$$

s.t. $K^* = K^{*T}$, $K^* \succeq 0$.

where $J = K - (E + E^T) - \hat{E}$.

Since K* is obtained by stacking *m* K*s, we slice J into *m* $n \times n$ matrices: $J^{(1)}, \cdots, J^{(n)}$, and denote $J = \frac{1}{m}\sum_{i=1}^{m} \mathbf{J}^{(i)}$. Then we rewrite Eq.(28) as:

$$\min_{K^*} \|K^* - J\|2F \ , \quad (29)$$

s.t. $K^* = K^{*T}$, $K^* \succeq 0$.

The closed-form solution of Eq.(29) can be obtained by the following Theorem.

Theorem 3. Let the eigenvalue decomposition of J is $J = W\Theta W^T$ where W contains the eigen vectors of J and Θ is a diagonal matrix whose diagonal elements are the eigen values of J. Then we set the negative eigenvalues to zero and obtain a new diagonal matrix $\tilde{\Theta}$. The closed-form solution of Eq.(29) is $K* = W\tilde{\Theta}W^T$.

Proof. Let the SVD decomposition of K* is $K^* = U_K \Sigma_K V^T_K$.

Then we have $\|K^* - J\|^2_F = tr(\Sigma^2_K) - 2tr(K^*J) + tr(JJ^T)$ ……..(30)

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According to Von Neumanns trace inequality, we have $tr(K^*J) \leq tr(\Sigma_K\Theta)$. Then

$tr(U_K\Sigma_K V_K J) = tr(K^*J) \leq tr(\Sigma_K\Theta)$

$=tr(W\Sigma_K W^T W\Theta W^T) = tr(W\Sigma_K W^T J)$ (31)

which leads to

$\|K*-J\|^2_F \geq \|W\Sigma_K W^T - J\|^2_F$ (32) Therefore, to minimize Eq.(29), we should set $U_K = V_K = W$. Taking it back to Eq.(29), we obtain:

$$\min_{K^*} \|K^*-J\|^2_F = \min_{\sum K \geq 0} \|\Sigma_K-\Theta\|^2_F \quad (33)$$

Obviously, the solution of Eq.(33) is that $\Sigma K = \tilde{} \Theta$. It is easy to verify that $K* = W \tilde{}\Theta W^T$ satisfies the positive semi definite and symmetric constraints.

To sum up, the closed-form solution of Eq.(29) is $K* = W \tilde{}\Theta WT$.

C. Convergence Analysis

As introduced above, updating E and K∗ could make the goal characteristic decrease monotonically. However, the convergence of the ADMM used to update Eˆ is tough to research due to the non-convexity of our version. Fortunately, [29] offers a weak convergence result of the ADMM set of rules as follows:

Theorem 4. *[29] Let* $\mathcal{S}^{(l)}$, $\mathbf{U}_i^{(l)}$, $\mathcal{M}_i^{(l)}$ *denote the value of* S,U_i, M_i *in the l-th iteration of the inner while cycle (Lines 6-12) in Algorithm 1, respectively. Then, we denote* $\hat{E}^{(l)} = S^{(l)} x_1 U^{(l)}_1 x_2 U^{(l)}_2 x_3 U^{(l)}_3$ *We have:*

$$\left\|\hat{\mathcal{E}}^{(l)} - \mathcal{M}_i^{(l)}\right\|_F = O\left(\mu^{(0)}/1.2^{l/2}\right)$$
$$\left\|\hat{\mathcal{E}}^{(l+1)} - \hat{\mathcal{E}}^{(l)}\right\|_F = O\left(\mu^{(0)}/1.2^{l/2}\right)$$

It implies that the difference of Eˆ(l) in adjacent iterations turns into smaller and smaller. In addition, with iterations, $S \times_1 U_1 \times_2 U_2 \times_3 U_3$ is an increasing number of in the direction of M_i.

D. Time And Space Complexity

When updating E, we need to compute n×n×m values in E by means of Eq.(27) which charges $O(n^2m)$ time. When optimizing K^*, we need to compute the SVD of an n × n matrix J which costs $O(n^3)$ time. In the ADMM step, when updating S, the most expensive step is computing $\mathcal{Q} = \mathcal{O} \times_1 \mathbf{U}_1^T \times_2 \mathbf{U}_2^T \times_3 \mathbf{U}_3^T$, whose time complexity is $O(r_1mn^2 + r_1r_2mn + r_1r_2r_3m)$. When optimizing $\mathbf{U}_1$, we first compute $\mathbf{B}_1$ in Eq.(19) in $O(r_1mn^2 + (r_1r_2r_3 + r_1r_3m)n)$ time, and then compute the SVD of $\mathbf{B}_1$ (an $n \times r_1$ matrix) in $O(nr_1^2)$ time. Moreover, we can use randomize truncated SVD to lessen the time complexity to $O(nr_1log(k) + k^2(n + r_1))$ in which k is the quantity of singular values retained to truncate the approximate SVD and satisfies $k \ll r_1$. The complexity of solving U_2 and U_3 is similar. When optimizing M_1, the main cost lies in computing the SVD of $\mathbf{F}_{(1)}$ (an $n \times (mn)$ matrix), which charges $O(n^3m)$ time and if we use randomized truncated SVD, the time complexity is decreased to O(mn2log(k) + k2mn). The complexity of computing M_2 and M_3 is similar. In addition, SVD may be deployed on a distributed platform. For instance, the MLlib affords a particularly scalable and green implementation on Spark1. Obviously, tensor and matrix multiplications also can without problems be implemented on a dispensed platform.

Since we need to keep and technique numerous n × n × m tensors, the distance complexity of our method is $O(n^2m)$.

VIII. IMPLEMENTATION

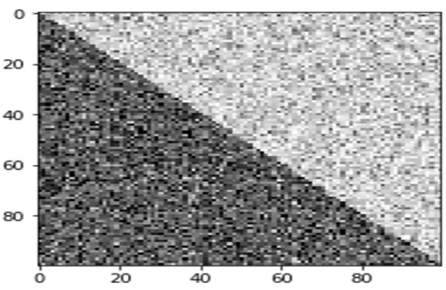

Fig 8.1

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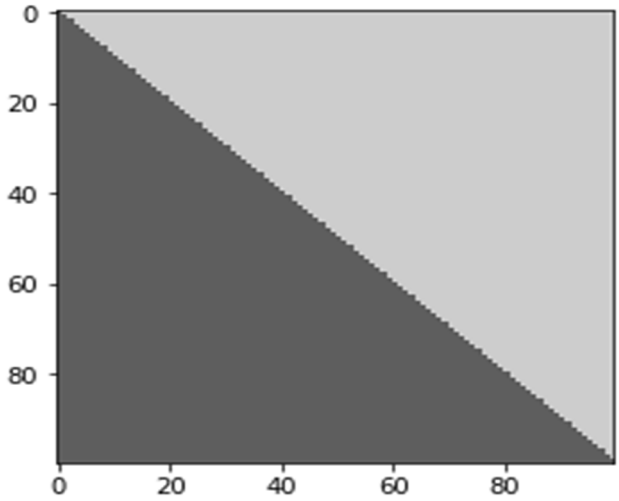

Fig 8.2

A. Compared Method

To evaluate the quality of the learned consensus kernel, we apply two famous kernel based clustering methods (kernel k-means and spectral clustering) on the learned kernels, and we refer them as Ours-KKM and Ours-SC, respectively. We compare them with the following kernel k-means based and spectral clustering based methods, respectively.

1) *Single Kernel Methods:* We run kernel k-means and spectral clustering on each kernel separately. We report the best and the average results over all kernels, which are referred to as KKM-b, KKM-a, SC-b, and SC-a, respectively. "KKM" refers to kernel k-means, "SC" refers to spectral clustering, "b" refers to the best result, and "a" refers to the average result.
2) *Equal Weighted Methods:* We linearly combine all input kernels into a single kernel with equal weights, and then apply kernel k-means and spectral clustering on it. The results are referred to as KKM-ew and SC-ew.
3) *MKKM:* MKKM (Multiple Kernel K-Means) is proposed in which extend kernel k-means in multiple kernel setting.
4) *CoregSC:* CoregSC is a co-regularized multi-view spectral clustering is proposed.
5) *LMKKM:* LMKKM is proposed in depending on the results in [1], it transfers the kernel k-means to spectral methods and obtains the clustering results from eigenvalue decomposition. Thus it is a spectral based method in fact.
6) *RMSC:* RMSC (Robust Multi-view Spectral Clustering) is proposed in [11]. We first transform the kernels into probabilistic transition matrices following [11], and then apply RMSC to get the final clustering results.
7) *RMKKM:* RMKKM (Robust multiple kernel k-means) is proposed in [12], which uses `2,1 loss to replace the `2 loss in the multiple kernel k-means.
8) *RMKC:* RMKC (Robust Multiple Kernel Clustering) is proposed in [6]. It also learns a consensus kernel matrix. We apply kernel k-means and spectral clustering on it, which are referred to as RMKC-KKM and RMKC-SC, respectively.
9) *ONKC:* ONKC (Optimal Neighborhood Kernel Clustering) is proposed in [8] which learns the optimal neighborhood for clustering.

B. Experimental Setup

Flowing the similar experimental protocol of [6], we apply 8 different kernel functions as candidate kernels. These kernels are 5 Gaussian kernels $K(xi , xj) = \exp(-\| xi - xj\|^2 / 2t^2)$ with $t = t_0 \times d_m a_x$, where $d_m a_x$ is the maximal distance between samples and t_0 varies in the range of {0.01, 0.1, 1, 10, 100}, 2 polynomial kernels $K(xi , xj) = (x_i{}^t x_j)^a$ with a = 2, 4 and a linear kernel. All kernels are normalized to normalized-cut weighted form as [33] did and rescaled to [0, 1]. The number of clusters is set to the true number of classes for all algorithms and all data sets. We independently repeat the experiments for 10 times and report the average results and t-test results.

In our method, we tune λ_1 and λ_2 in $[10^{-2}, 10^2]$ by grid search. For other compared methods, we tune the parameters as suggested in their papers. Two clustering evaluation metrics are adopted to measure the clustering performance, including clustering Accuracy (ACC) and Purity. All experiments are conducted using Matlab on a PC computer with Windows 10, 4.2 GHz CPU and 32GB memory.

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C. Results

1)

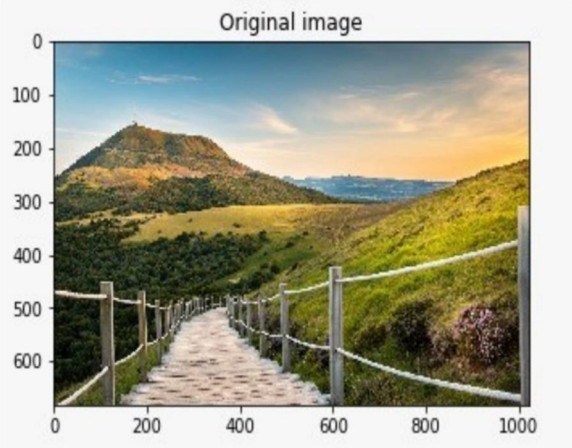

Fig 8.3 Original image

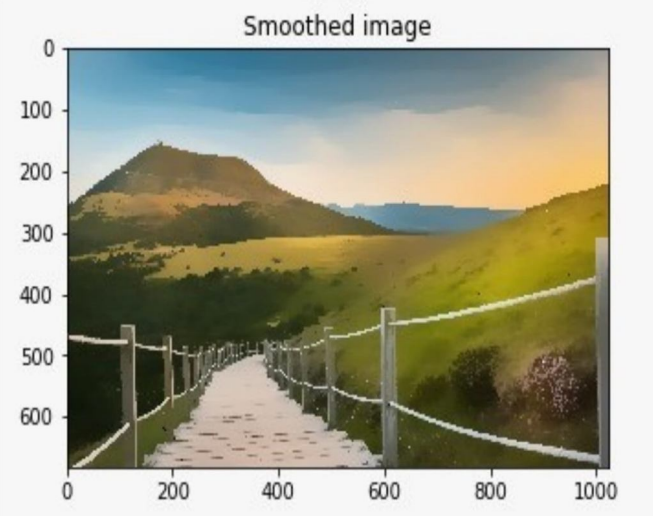

Fig 8.4. smoothed image

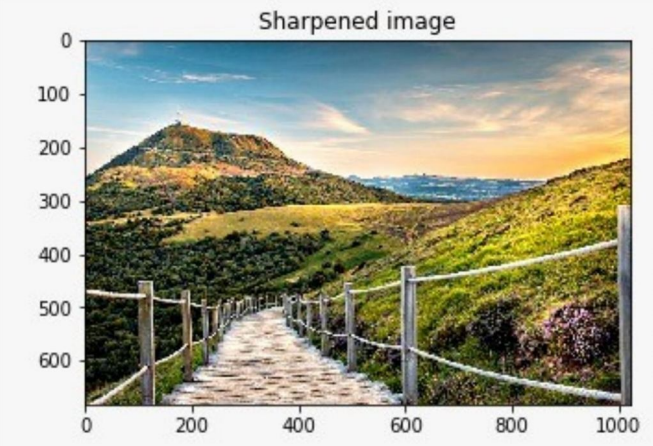

Fig 8.5. Sharpened image

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2)

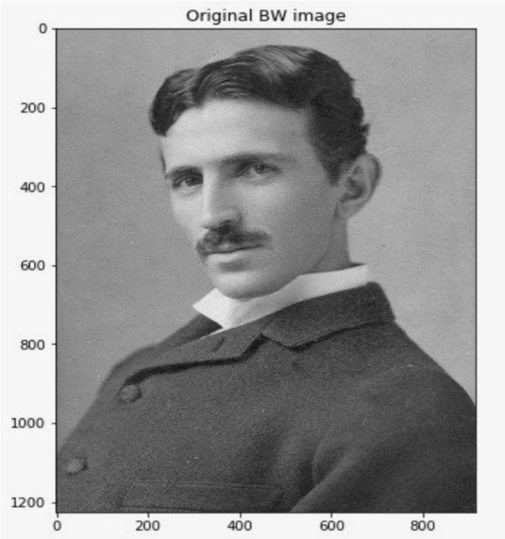

Fig 8.6. Original BW image

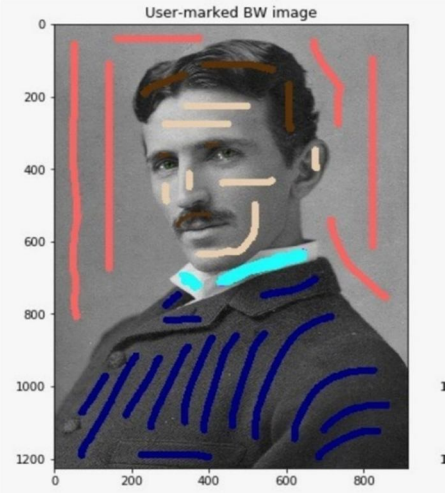

Fig 8.7. User- marked BW image

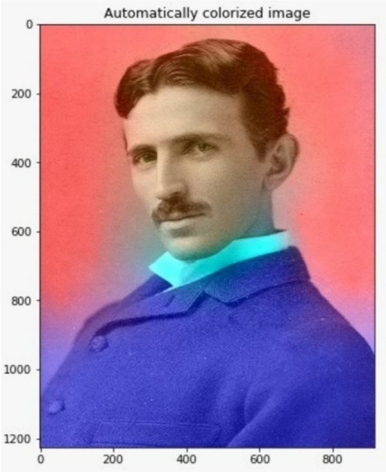

Fig 8.8. Automatically colorized image

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IX. CONCLUSION AND FUTURE WORK

In this paper, we proposed a novel unsupervised strong more than one kernel gaining knowledge of approach. By watching that there are types of noises at the kernel matrix, i.e., local noises and global noises, we analyzed the shape of every kind of noises and designed regularized terms to symbolize them. Simultaneously, we found out a consensus kernel with the aid of minimizing the disagreement over cleaned kernels. Then, a block coordinate descent algorithm was proposed to clear up the optimization trouble. Experimental outcomes on benchmark information units display that our approach outperform the state- of-the-art unsupervised a couple of kernel getting to know techniques. Our technique includes a few complicated tensor operation which makes it now not appropriate for huge statistics. In the future, we are able to take a look at the scalability difficulty and use it to deal with large facts.

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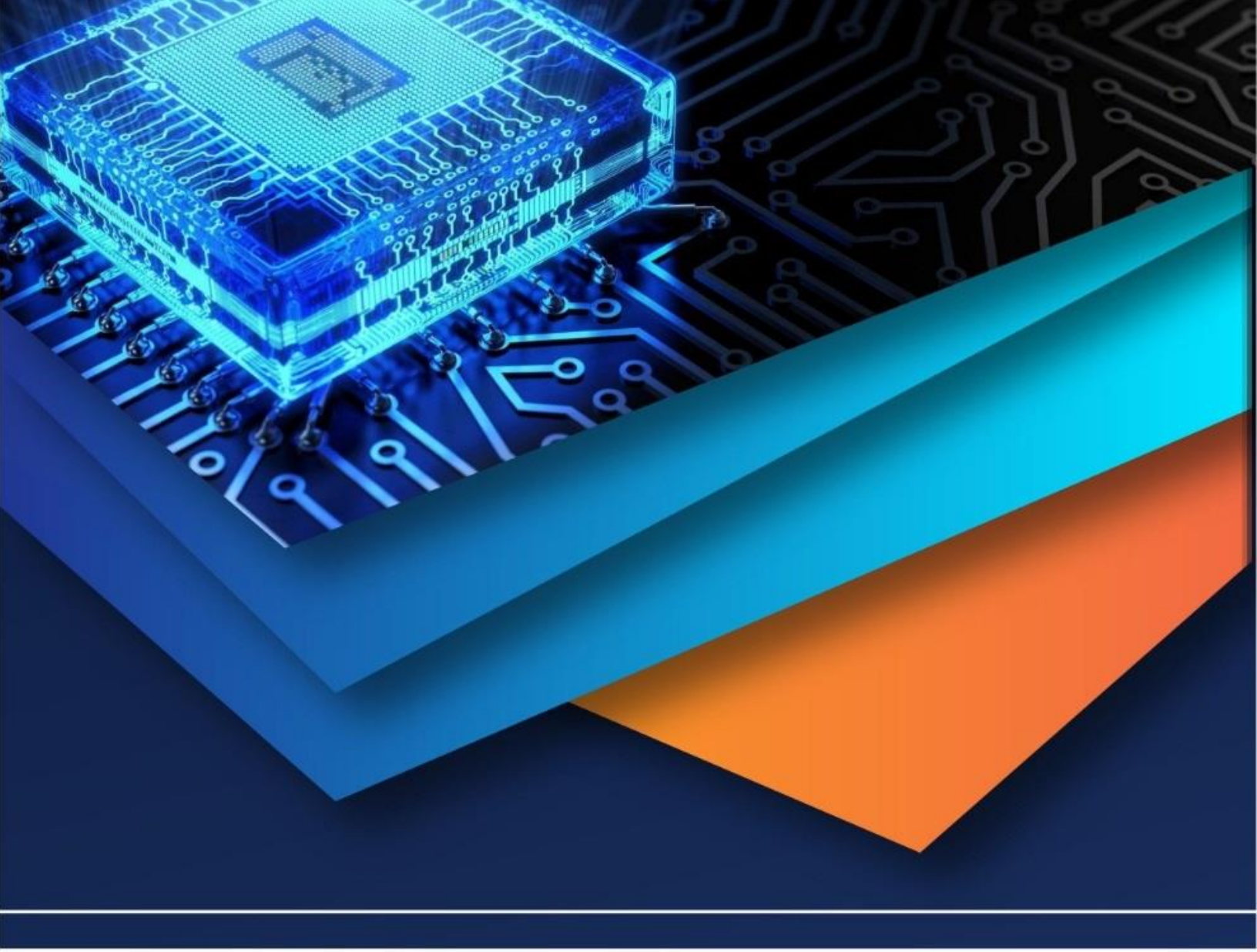

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