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# Implementation of Fractional Order PID Controller for An AVR System Using GA Optimization Technique

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**Abstract:** In recent years, the research and studies on fractional order (FO) modelling of dynamic systems and controllers are quite advancing. To improve the stability and dynamic response of automatic voltage regulation (AVR) system, we presented fractional Order PID (FOPID) controller by employing Genetic Algorithm (GA) technique. We used fractional order tool kit a masked fractional order PID block in MATLAB programming to implement the  $PI^{\alpha}D^{\beta}$  controller for any type of system. Comparisons are made with a PID controller from standpoints of transient response. It is shown that the proposed FOPID controller can improve the performance of the AVR in all the aspects.

## I. INTRODUCTION

Even so much research was developed in soft computing techniques for designing controllers, still these techniques fails areas. Neuro-controllers works according to the training given to them and their performance depends on the availability of vast data set of training inputs and target values of the process. Certainly, there is a probability of missed data in the training set, in such case the controller fails to generate an accurate output. Also, the performance of the fuzzy controllers is purely based on the rule base, selection of membership functions and their range and it was still challenging to decide the fuzzy parameters. Still today most of the control problems are smoothly solved by PID controllers due to simplicity in their design and easy implementation. It has been shown that two extra degrees of freedom from the use of a fractional-order integrator and differentiator make it possible to further improve the performance of traditional PID controllers. Details of past and present progress in the analysis of dynamic systems modeled by Fractional order differential equations (FODEs) can be found in [1–14]. Literature survey gives the fractional controller which was developed by Crone in [3], while [4, 12, 13] presented the  $PD^{\mu}$  controller and [3,14] proposed the  $PI^{\alpha}D^{\mu}$  controller.

We extended the benefits of  $PI^{\alpha}D^{\mu}$  controller for AVR system. In Particular, a masked  $PI^{\alpha}D^{\mu}$  controller is developed in matlab by programming to optimize the parameters based on the recently developed optimization techniques instead of using toolbox which was restrained for using advanced optimization techniques. Genetic Algorithm (GA) technique has already been used to determine optimal solution to several power engineering problems and we employed these algorithms to design an FOPID controller for Automatic voltage regulator (AVR) problem. The proposed controller is simulated within various scenarios and its performance is compared with those of an optimally-designed PID controller. Transient response and performance robustness characteristics of both controllers are studied and superiority of the proposed controller in all two respects is illustrated.

## II. FRACTIONAL MODELING

PID (Proportional-Integral-Derivative) control is one of the earlier control strategies a most popular industrial controller due to its simplicity and the ability to turn a few parameters automatically controller is used in more than 90% of the control loop, flexibility help the design more robust system. The turning of the PID controller is mostly done using Zeigler and Nichols turning method. Fractional Order  $PI^{\alpha}D^{\beta}$  controllers are described by fractional order differential equations, expanding derivatives and integrals to fractional order can adjust control system's frequency response directly and continuously.

### A. Integer Order Approximations

Online real-time, fractional -order differentiation may be required in control system. Using filters is one of the best ways to solve the problems. By using filters, the fractional order transfer function is approximated to integer order.

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### B. Oustaloup's Recursive Filter

Some continuous filter have been summarized in [13]. Among the filters, the well-established Oustaloup recursive filter has a very good fitting to the fractional-order differentiators [14,15]. Assume that the expected fitting range is  $(\omega_b, \omega_h)$ . The filter can be written as

$$G_f(s) = K \prod_{k=-N}^N \frac{s + \omega_k}{s + \omega_k} \quad \dots\dots\dots (1)$$

Where  $\gamma$  is the order of the differentiation and  $N$  is the order of approximation.

$$\omega'_k = \omega_b \left( \frac{\omega_h}{\omega_b} \right)^{\frac{K+N+\frac{1}{2}(1-\gamma)}{2N+1}}, \quad \omega_k = \omega_b \left( \frac{\omega_h}{\omega_b} \right)^{\frac{K+N+\frac{1}{2}(1+\gamma)}{2N+1}}, \quad K = \omega_h^\gamma \quad \dots\dots\dots (2)$$

### C. A Refined Oustaloup Filter

Here we introduce a new approximate realization method for the fractional-order derivative in the frequency range of interest  $[\omega_b, \omega_h]$ . Our proposed method here gives a better approximation than Oustaloup's method with respect to both low frequency and high frequency. Assume that the frequency range to be fit is defined as  $(\omega_b, \omega_h)$ . Within the pre-specified frequency range, the fractional-order operator  $s^\alpha$  can be approximated by the fractional-order transfer function as

$$K(s) = \lim_{N \rightarrow \infty} K_N(s) = \lim_{N \rightarrow \infty} \prod_{k=-N}^N \frac{1 + \frac{s}{\omega_k}}{1 + \frac{s}{\omega_k}} \quad \dots\dots\dots (3)$$

According to the recursive distribution of real zeros and poles, the zero and pole of rank  $k$  can be written as

$$\omega'_k = \left( \frac{d\omega_b}{b} \right)^{\frac{\alpha-2k}{2N+1}}, \quad \omega_k = \left( \frac{b\omega_h}{d} \right)^{\frac{\alpha+2k}{2N+1}} \quad \dots\dots\dots (4)$$

Through confirmation by experimentation and theoretical analysis, the synthesis approximation can obtain the good effect when  $b = 10$  and  $d = 9$ .

## III. FRACTIONAL ORDER PID CONTROLLER

The block diagram of Fractional Order PID Controller is shown in Fig.1

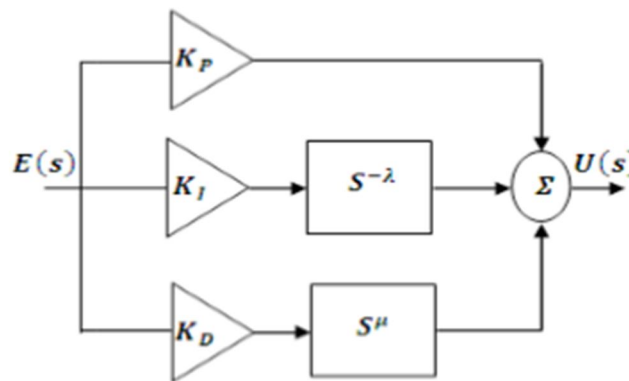


Fig.1. Block Diagram of Fractional Order PID controller

The differential equation of a fractional order  $PI^\lambda D^\mu$  controllers is described by

$$U(t) = K_p e(t) + K_I D_t^{-\lambda} e(t) + K_D D_t^\mu e(t) \quad \dots\dots\dots (5)$$

The continuous transfer function of FOPID is obtained through Laplace transform and is given by

$$G_C(S) = K_p + K_I S^{-\lambda} + K_D S^\mu \quad \dots\dots\dots (6)$$

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Where  $K_p, K_i$  and  $K_d$  are proportional, integrator and derivative gain respectively. Gamma and delta are orders of the integral and derivative part,  $\lambda$  and  $\mu$  respectively.  $\omega_b$  and  $\omega_h$  are lower and upper frequencies respectively for which the fractional order integral and derivative are approximated to integer order. Here, the fractional order by using derivative and integral are approximated to integer order by using oustaloup filter and N is the order of approximation.  $s^{-0.99}$  is approximated to integer order by using oustaloup filter.

The optimization tool, provided in FOMCON, can in practice be used for fractional PID tuning due to its flexibility. The tool can be accessed from the PID design tool menu by typing fpid\_optim. the tool is shown in fig 2

**FPID Optimization Tool**

File View Tools

**Plant model**

LTI system: [ ] Type: [ ]

Approximate as: Oustaloup filter

Within w range: [0.0001; 10000] Of order: 5

☐ Enable zero cancelation for non-proper LTI systems

**Fractional PID controller parameters**

Tune all parameters [v]

	Min	Max
Kp	0	100
Ki	0	100
lam	0.01	1
Kd	0	100
mu	0.01	0.9

Set Gains [v] to 1

**Simulation parameters**

Max. simulation time [s]: 100

Time step (min/max) [s]: 0.01 0.5

☐ Use Simulink for system simulation ☐ Disable warnings

Model: default [v] Edit New

**Optimization and performance settings**

Optimization algorithm: optimize(): Nelder-Mead

Performance metric: ISE

**Gain and phase margin**

☒ Enable gain and phase margin

Gain margin [dB]: 10 ☐ Exact 60 ☐ Exact

**Noise and disturbance rejection**

☐ Enable sensitivity function specifications

$|T(jw)|$  [dB] <= -20 for  $w \geq w_t$  [rad/s]: 10

$|S(jw)|$  [dB] <= -20 for  $w \leq w_s$  [rad/s]: 0.01

**Critical frequency and gain variation robustness**

☐ Enable critical frequency specification

$w_c$  [rad/s]: 0.1 ☒  $w_{high}$  -1

**Control law constraints**

☐ Enable control signal limits ☐ Metric wgt: 0.5

Minimum: 0 Maximum: 100

Optimization setpoint: 1 ☐ Force strict constraints

☐ Generate report ☐ Max number of iter's: 100

Optimize ☐ Simulate only Take values

Fig.2 Fractional PID optimize tool

### IV. AVR DESIGN USING FOPID CONTROLLER

#### A. Linearized Model of Excitation System

The role of an automatic Voltage Regulator (AVR) is to hold the terminal voltage of a synchronous generator at a specified level. We consider an alternator supplied controlled rectifier excitation system [18] for simulation. Five main components, namely



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amplifier, exciter, excitation voltage limiters, generator, measurement and filtering includes in the mathematical model of AVR system by ignoring the saturation and other non-linearities [19]. The transfer function of these components are represented as follows.

### 1) Amplifier model.

The amplifier model is given by

$$\frac{V_R(s)}{V_C(s)} = \frac{K_A}{1+\tau_A(s)} \quad \dots\dots\dots (7)$$

Typical values of  $K_A$  are in the range of 10 to 400. The amplifier time-constant often range from 0.02 to 0.1 s

### 2) Exciter model.

Exciter model and parameters greatly depend on its type. A simplified transfer function of a modern exciter is

$$\frac{V_F(s)}{V_R(s)} = \frac{K_E}{1+\tau_E s} \quad \dots\dots\dots (8)$$

Typical values of  $K_E$  are in the range of 0.8 to 1 and the time constant  $\tau_E$  for an AC exciter in the range of 0.5 to 1.0 s.

### 3) Generator model.

The transfer function relating the generator terminal voltage to its field voltage can be simplified to

$$\frac{V_t(s)}{V_F(s)} = \frac{K_G}{1+\tau_G(s)} \quad \dots\dots\dots (9)$$

The constants are load dependent,  $K_G$  may vary between 0.7 and 1.0, and  $\tau_G$  between 1.0 and 2.0 s from full load to no load.

### 4) Measurement model.

The voltage measurement block, including PT, rectifier and filter, is often modelled with a single time constant.

$$\frac{V_s(s)}{V_t(s)} = \frac{K_R}{1+\tau_R s} \quad \dots\dots\dots (10)$$

$\tau_R$  ranges over 0.001 to 0.06 s.

### 5) Excitation voltage limiters.

AVR and exciter output voltages are limited by windup and non-windup limiters [20]. Also, dedicated over excitation and under excitation limiters are employed to assure safe operation of the generator. Block diagram of the AVR compensated with an FOPID controller is shown in Fig.4. In this figure, the combined effects of these limiters are represented by the upper and lower limits set to three times of the nominal value of the field voltage.

## B. Performance Criterion

In control system design and analysis or for optimal control purposes, performance indices are calculated to be used as quantitative measures to evaluate a system's performance, where a control system is judged as an optimum system when the system parameters are adjusted so that the index used in the design reaches its minimum value, while constraints of the controlled system are respected. The commonly used indices are integral of the square of the error (ISE), integral of the absolute value of the error (IAE), integral of time multiplied by absolute value of the error (ITAE), integral of time multiplied by the squared error (ITSE). The ITAE measure, which will be implemented in this paper, is given by the following equation

$$ITAE = \int_0^{\infty} t |e(t)| dt \quad \dots\dots\dots (11)$$

Therefore, the proposed performance criterion  $J(K)$  is defined as.

$$J(K) = (ITAE) \quad \dots\dots\dots (12)$$

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where  $k$  is  $[K_p, K_i, K_d, \lambda, \mu]$ . The Genetic Algorithm (GA) utilized to design these five controller parameters such that the controlled system exhibits desired response and robust stability as evaluated by the proposed performance criterion.

### V. OPTIMIZATION ALGORITHMS

#### A. Genetic Algorithm

A genetic algorithm is introduced to optimization problems and they consist of proportional gain, integral gain, derivative gain, derivative order and integral order.

Genetic algorithm (GA) is the process of searching the most suitable one of the chromosomes that built the population in the potential solutions space. A search like this, tries to balance two opposite objectives: searching the best solutions (exploit) and expanding the search space. Thus, GA has become a robust optimization tool for solving the problems related to different field of the technical and social sciences, Genetic Algorithms (GA) is global optimizing ones, based on natural selection and genetics mechanisms. They use a parallel procedure and structured strategy, but random, aiming to reinforce searching of high aptitude points. GA can be able to overcome complex non-linear optimization tasks like non-convex problems, non-continuous objective functions iteratively using the three operators in random way but based on the fitness function evolution to perform the basic tasks of copying strings, exchanging portions of strings as well as changing some bits of strings, and finally find and decode the solutions to the problem from the last pool of mature strings.

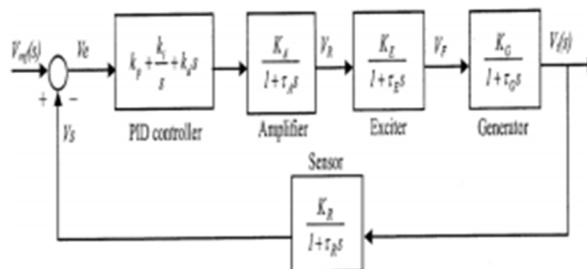


Fig .3 Linearized model of an AVR system

### VI. PROBLEM FORMUATING

The overall transfer function for an AVR system is

$$G_p = \frac{10}{(0.04s^3 + 0.54s^2 + 1.5s + 1)}$$

$$f_b = \frac{1}{1 + 0.01s}$$

By using R-H criterion we got ultimate gain  $K_u$  and ultimate period  $T_u$

$$K_u = 0.09$$

$$T_u = 3.63\text{sec}$$

PID controllers can be turned by using different methodologies. Ziegler Nicholas method is one of the conventional methods used for turning. Due to high overshoot in ZM method some advanced methods are needed which does not need retuning like ZN method.

#### A. Details of FOPID Design Using GA for the AVR

The following parameters are used for carrying out the FOPID design using GA:

- 1) Population size = 95
- 2) Generations=100
- 3) Crossover fraction=0.75
- 4) Population initial range= [0;0.1]

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5) The order of approximation is set to  $N = 5$

Comparision Of The Evaluation Values Between Both Pid And Fopid Controllers

	<b>ZN-PID</b>	<b>GA-PID</b>	<b>FOPID</b>	<b>GAFOPID</b>
$K_p$	0.06	2.505	0.79	4.416
$K_i$	0.01	1.735	1.058	3.04
$K_d$	0.027	0.804	0.4048	1.507
$\lambda$	-	-	0.99	0.99
$\mu$	-	-	0.899	0.937
$t_r$	25sec	0.32	0.17	0.12
$t_p$	50sec	0.44	0.26	0.19
$t_s$	50sec	3.17	0.9	0.85

TABLE.1

Fig. 4. step response of the AVR controller by PID and FOPID in the presence of generator and exciter uncertainties

### VII. CONCLUSION

Performance comparisons of FOPID(GA), FOPID, PID(GA) and PID controller have been reviewed and it is founded that response of FOPID(GA) controller is better than above three methods. The settling time and rise time of the response acquired by FOPID(GA) controller is founded to be less comparison acquired by PID controller the proposed algorithms performed efficient search for the optimal FOPID controller parameters to the practical AVR system. Furthermore, it can be concluded from the above programming that the proposed FOPID controller has more robust stability and performance characteristics than the PID controller applied to the AVR system.

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